



CAPSID

Computational Algorithms for Protein Structures and Interactions David Ritchie + Isaure Chauvot de Beauchêne Inria Nancy – Grand Est

Structural Bioinformatics Tools and Techniques

In-House Software

- Hex- protein docking by spherical polar FFT
- Sam spherical polar FFT docking of symmetrical complexes
- gEMfitter cryo-EM protein density fitting by FFT on GPU
- KBDOCK database of 3D domain-domain interactions
- Kpax multiple flexible protein structure alignment

External Tools

• Molecular dynamics simulation & modeling: NAMD, Modeller, ...



"Hex" – Spherical Polar Fourier Protein Docking



- SPF approach => analytic translational + rotational correlations
- Shape-based scoring function (surface skin overlap volume)
- Can cover 6D search space using 1D, 3D, or 5D rotational FFTs...
- "Easy" to accelerate the 1D FFTs on highly parallel GPUs ...



Sam/Hex: Spherical Polar Fourier Basis Functions

• Represent protein shape as a 3D shape-density function...

$$\tau(\underline{r}) = \sum_{nlm}^{N} a_{nlm}^{\tau} R_{nl}(r) y_{lm}(\theta, \phi)$$

• ...using spherical harmonic, $y_{lm}(\theta, \phi)$, and radial, $R_{nl}(r)$, basis functions





Coordinate Operators and Docking Equations

• Polar Fourier basis is "natural" for rotational search problems



Describe search space using operators

- Rotation: $\hat{R}(\alpha, \beta, \gamma) = \hat{R}_z(\alpha)\hat{R}_y(\beta)\hat{R}_z(\gamma)$
- Translation: $\hat{T}_z(R)$

Describe interaction as an "equation"

• $\hat{R}(0, \beta_A, \gamma_A)A(\underline{r}) \longleftrightarrow \hat{T}_z(R)\hat{R}(\alpha_B, \beta_B, \gamma_B)B(\underline{r})$

Can re-write this in many ways, e.g.

• $\hat{R}(\alpha_B, \beta_B, 0)^{-1} \hat{T}_z(R)^{-1} \hat{R}(0, \beta_A, \gamma_A) A(\underline{r}) \longleftrightarrow \hat{R}_z(\gamma_B) B(\underline{r})$

• Ultimately, operators transform coefficients in "simple" ways, e.g.

Score:
$$S_{AB}(\gamma_B) = \sum_{nlmp} [A'_{nlm}] \cdot [B^*_{nlp}e^{-ip\gamma_B}].$$



The Docking Equation for Cyclic Symmetries (C_n)

• C_n systems are planar, with symmetry operator $\hat{R}_y(\omega=2\pi/n)$



- $\hat{R}_{y}(\omega)\hat{T}_{z}(D)\hat{R}(\alpha,\beta,\gamma)A(\underline{r})\longleftrightarrow \hat{T}_{z}(D)\hat{R}(\alpha,\beta,\gamma)A(\underline{r})$
- After some working, we get a Fourier series in α : $S_{AB}(\alpha) = \sum_{nlmp} A_{nlm}(\beta, \gamma) A_{nlp}(D, \beta, \gamma)^* d_{mp}^{(l)}(\omega) e^{-i(p-m)\alpha}$



Sam Results – Examples of Each Symmetry Type



- All except 2 solutions are rank-1, RMSD < 3 Å w.r.t. crystal structure
- Main limitation is size of monomer (approx 500 residue limit)

Ritchie and Grudinin (2016), J Appl. Cryst., 49, 158–167

"gEMfitter" – GPU-Accelerated Cryo-EM Density Fitting

- Representation: 3D shape-density in Cartesian grid
- Search: brute force search with FFT acceleration
- Scoring: normalised cross correlation with Laplacian filter





- Calculates 3D translations using Cartesian FFT
- Calculates 3D rotations in GPU texture memory



Kpax – Protein Structure Alignements

• For the first time: exploit the tetrahedral geometry of C_{α} atoms to superpose pairs of residues without doing least-squares fitting



 Score similarity of local environment of residues (*i*, *j*) as product of 3D Gaussians between up-stream and down-stream C_α pairs:

$$K_{i,j} = \prod_{k=-n}^{n} e^{-\beta_k R_{i+k,j+k}^2/4\sigma_k^2}$$

• Gives a very fast way to score local 3D similarity of all residue pairs



Results – Comparing Rigid and Flexible Alignments
Example: methyl dehydroxygenase / galactose oxidase
PDB codes: 4AAH (572 AA; green/orange) and 1GOF (388 AA; blue/red)



- all red/orange regions are structurally aligned
- left: rigid; 267 pairs,
 3.3 Å RMSD (20 identities)
- right: flexible; 308 pairs,
 2.2 Å RMSD (23 identities)

• Compare with TM-Align (rigid only):

- TM-Align: 366 pairs, 5.4 Å RMSD (19 identities)
- Δ(TM-Align, Kpax): 11.6 Å RMSD



Applications – PDB-Wide Structure Comparison

KBDOCK¹ – database of 3D domain-domain interactions

• Allows us to identify "Domain Family Binding Sites" (DFBSs)



QsBio² – identifying biologically relevant quaternary structures

• Allows us to predict QS by homology and to fix wrong annotations in PDB



Ghoorah *et al.* (2014), Nucleic Acids Research, 42, D389–D395
 Dey, Ritchie, Levy (2017), in press



Thank You!

http://capsid.loria.fr/

http://hex.loria.fr/ http://sam.loria.fr/ http://gem.loria.fr/ http://kpax.loria.fr/ http://kbdock.loria.fr/



Fragment-based ssRNA docking



Fragment-based ssRNA docking



Docking



$$N_{fwd}(k,i) = \sum_{\substack{i' \in neigbors(i) \\ i' \in neigbors(i) }} N_{fwd}(k+1,i')}$$
$$N_{bwd}(k,i) = \sum_{\substack{i' tq \ i \in neigbors(i') \\ N_{bwd}(k,i) = N_{fwd}(k,i) \times N_{bwd}(k-1,i')}}$$
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frag k

Stochastic backtracking => enumerate chains



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Weighten by Boltzmann equation



Conformational energy



Probabilistic connectivity



 $E(i, j) = [E_{score}(i) \times E_{conf}(i) + E_{score}(j) \times E_{conf}(j)] \times connect(i, j)$

$$Docking scores$$

$$Z_{fwd}(k,i) = \sum_{j/connect(j,i)} \exp(\frac{E(i,j)}{RT}) \times Z_{fwd}(k-1,j)$$

$$P(k,i) = \frac{Z_{fwd}(k,i) \times Z_{bwd}(k,i)}{\sum_{j} P(k,j)}$$

Avoid clashes

Color coding [Noga Alon 1995]

Self-avoiding walks in oriented graph using dynamic programming

O(nk(2e)k) complexity



collab Y. Ponty, AMIBio, LIX