

# FROM LUSTRE TO C: A PROOF-CARRYING APPROACH TO VERIFIED COMPILATION

AID MEETING – *ESSAIM DE DRONES*

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## CONTEXT

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## EMBEDDED SYSTEMS DESIGN

### Embedded systems

- computer systems within physical systems that interact with the real world, often with real-time constraints
- software usually written in low-level languages: C, Ada, Assembly



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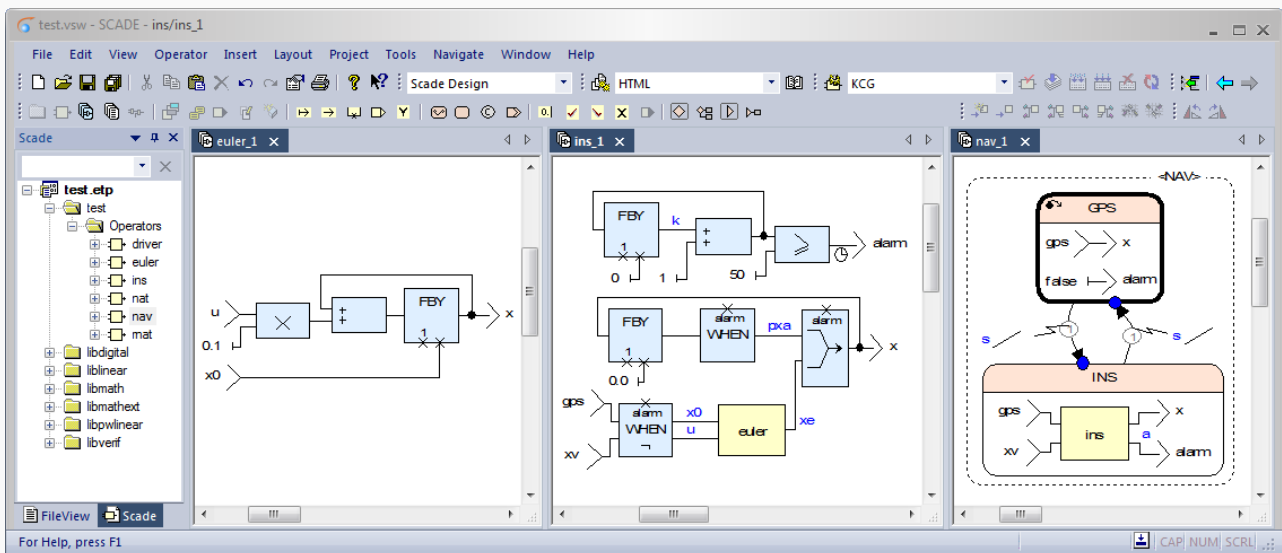
### Model-Based Design

Executable high-level abstract specifications



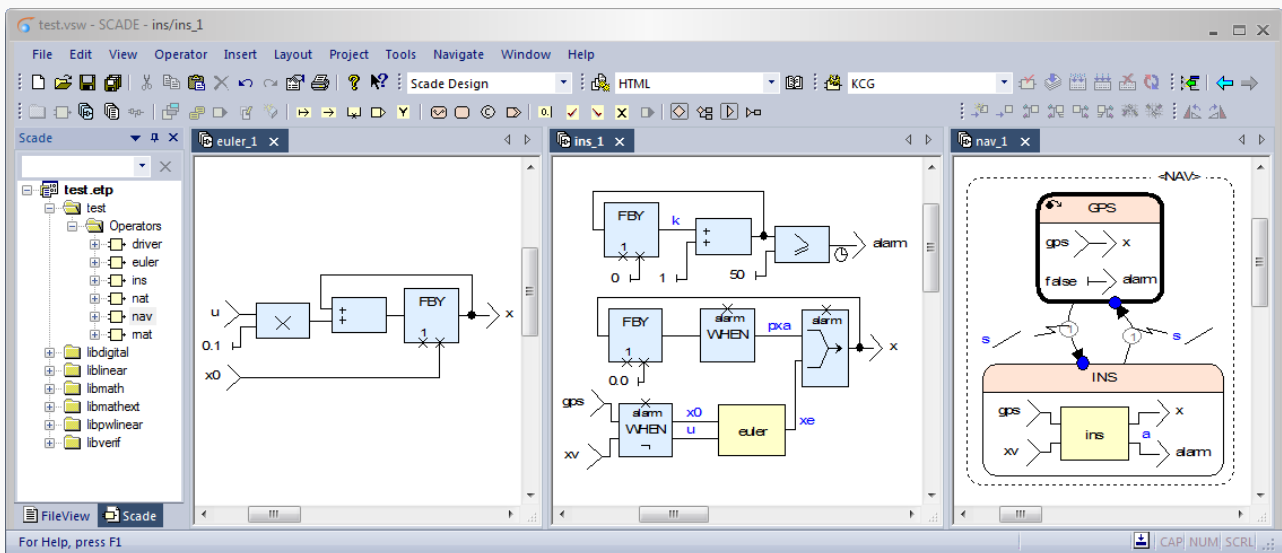
## MODEL-BASED DESIGN IN SCADE SUITE

[www.ansys.com/products/embedded-software/ansys-scade-suite](http://www.ansys.com/products/embedded-software/ansys-scade-suite)



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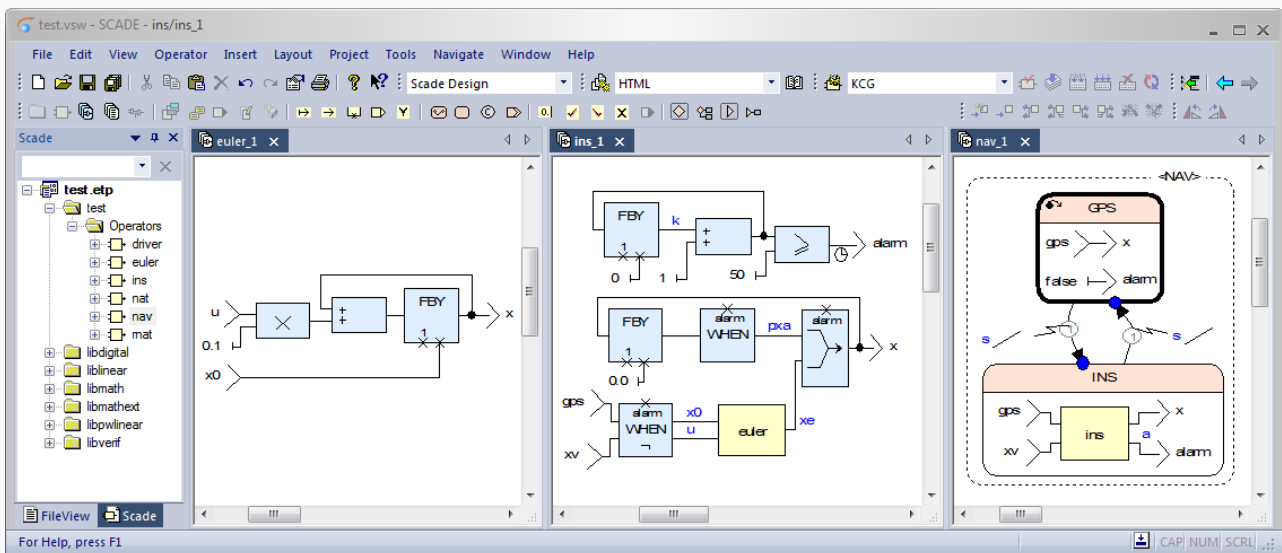


block / node = system

line = signal

## MODEL-BASED DESIGN IN SCADE SUITE

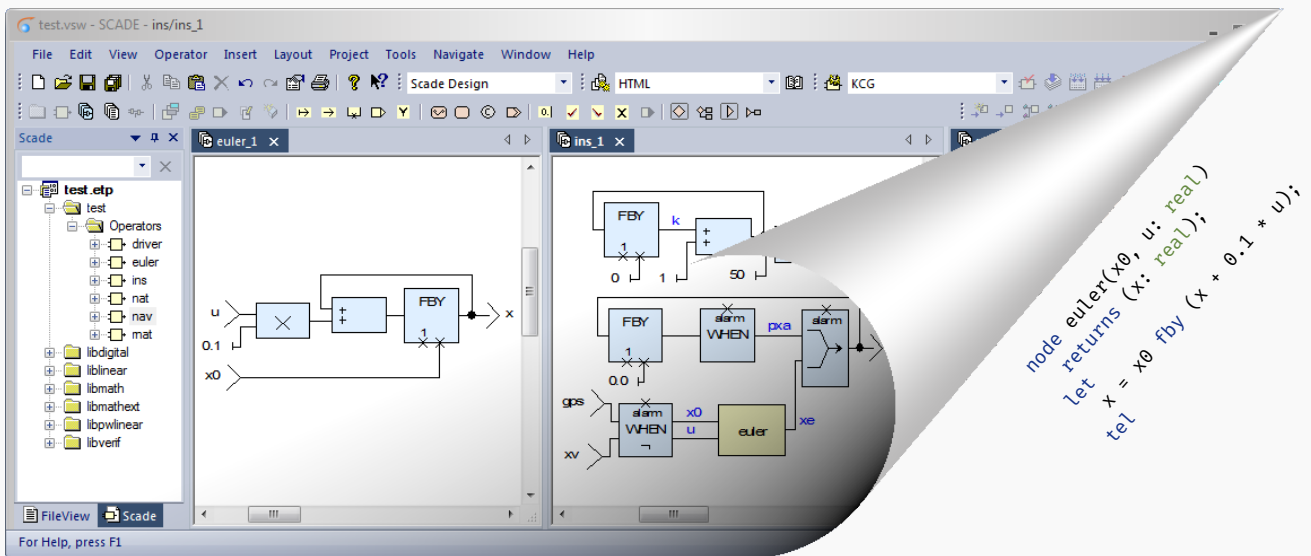
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block / node = system = stream function  
 line = signal = stream of values

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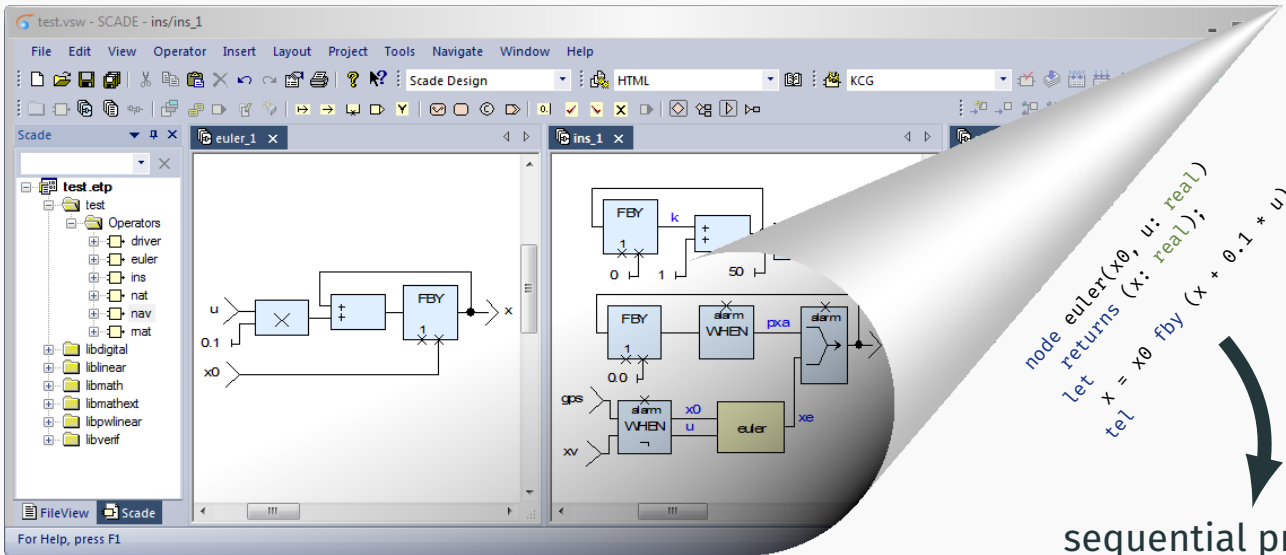


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block / node = system = stream function  
 line = signal = stream of values

sequential program  
 (C, Ada, assembly)

## CRITICALITY

### Systems that must not fail

- Flight control systems
- Automated train systems
- Power plant monitoring software



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**State of the art:** **industrial certification** of the development process, sometimes using *formal methods*, eg. SCADE

### Scientific questions:

- Can we produce an **end-to-end correctness proof**?
- Can verification performed at high-level be **transported and replayed at low-level**?

**CompCert** a verified C compiler in Coq

**VST** a C verification toolset based on CompCert

**seL4** a verified micro-kernel in Isabelle

**CakeML** a verified compiler for a functional language in HOL

**VeriPhy** a verified pipeline from CPS to controllers, using KeYmaera X, HOL4 and Isabelle

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**Vélus** a verified Lustre compiler in Coq, based on CompCert

## THE LUSTREC PROJECT

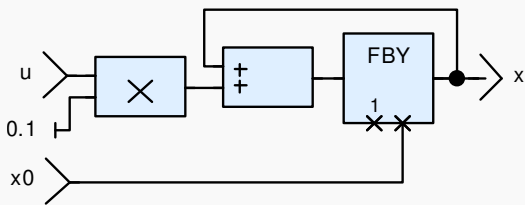
An academic Lustre compiler with several backends and verification abilities

- Generation of **ACSL specification**, along with the C code
- Encoding of the **correctness result**, to be proven by solvers
- Automatic **contract translation**



Software Analyzers

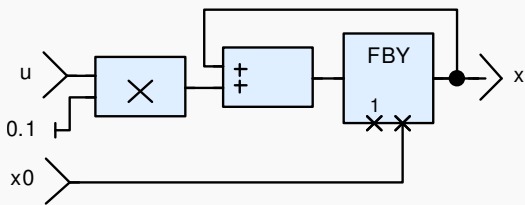
## EXAMPLE



```
node euler(x0, u: real)
  returns (x: real);
let
  x = x0 fby (x + 0.1 * u);
tel
```

$x_0$	0.00	1.55	3.62	5.46	...
$u$	15.00	20.00	17.00	12.00	...
$x + 0.1 \times u$	1.50	3.50	5.20	6.70	...
$x$	0.00	1.50	3.50	5.20	...

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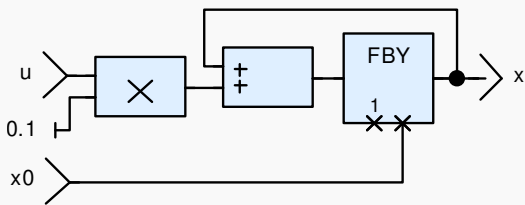


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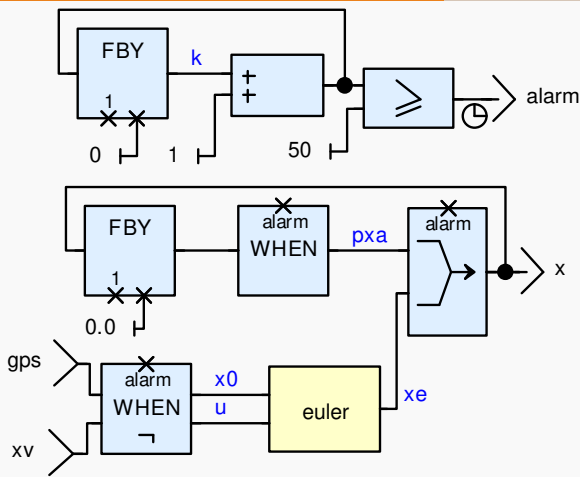
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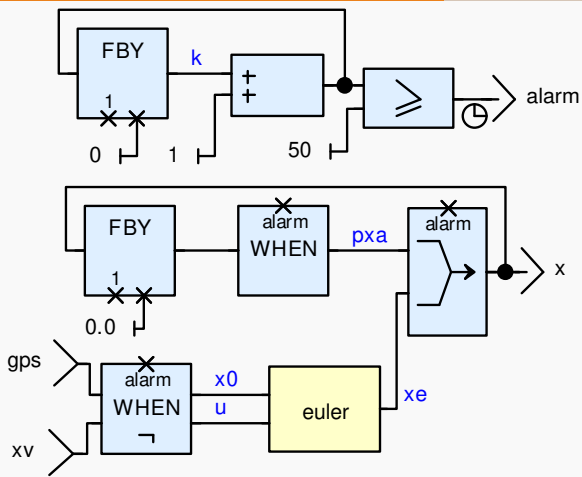
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  var pxa, xe: real; k: int;
  let
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    alarm = (k >= 50);
    xe = euler((gps, xv) when not alarm);
    pxa = (0. fby x) when alarm;
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k	0	1	2	3	...	49	50	51	...
alarm	F	F	F	F	...	F	T	T	...
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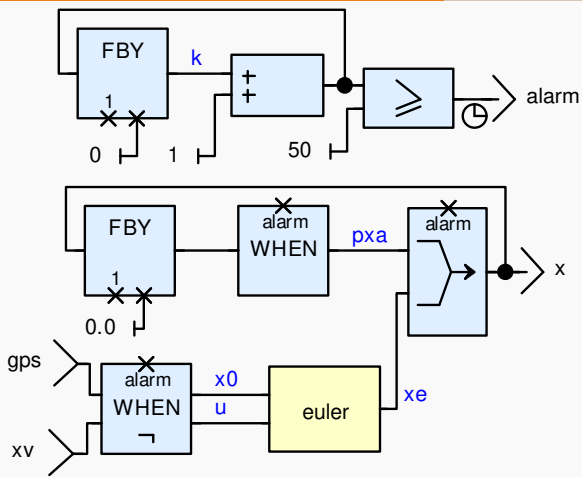
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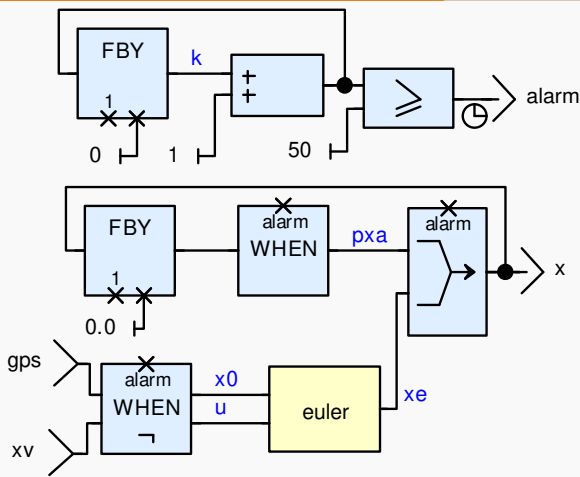


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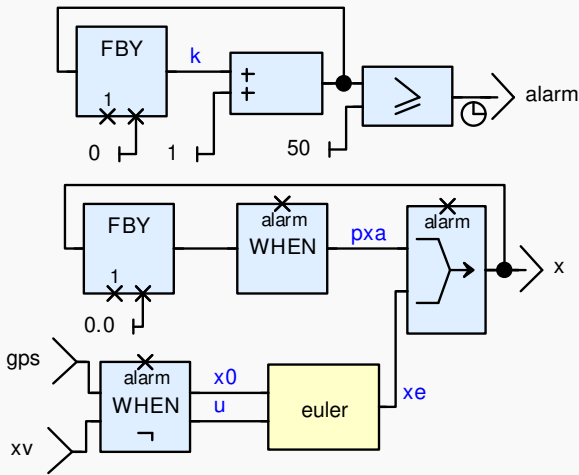
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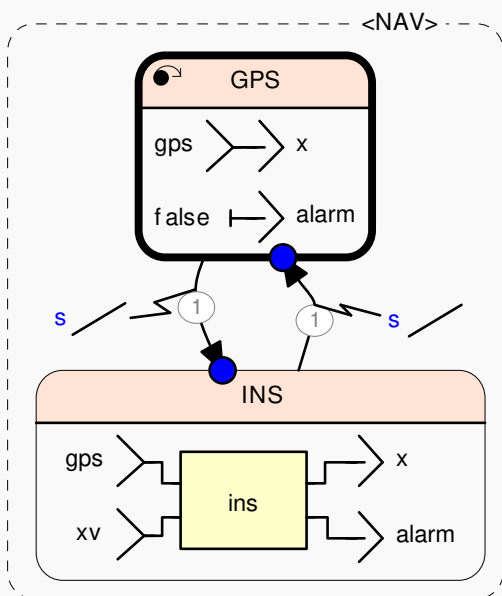
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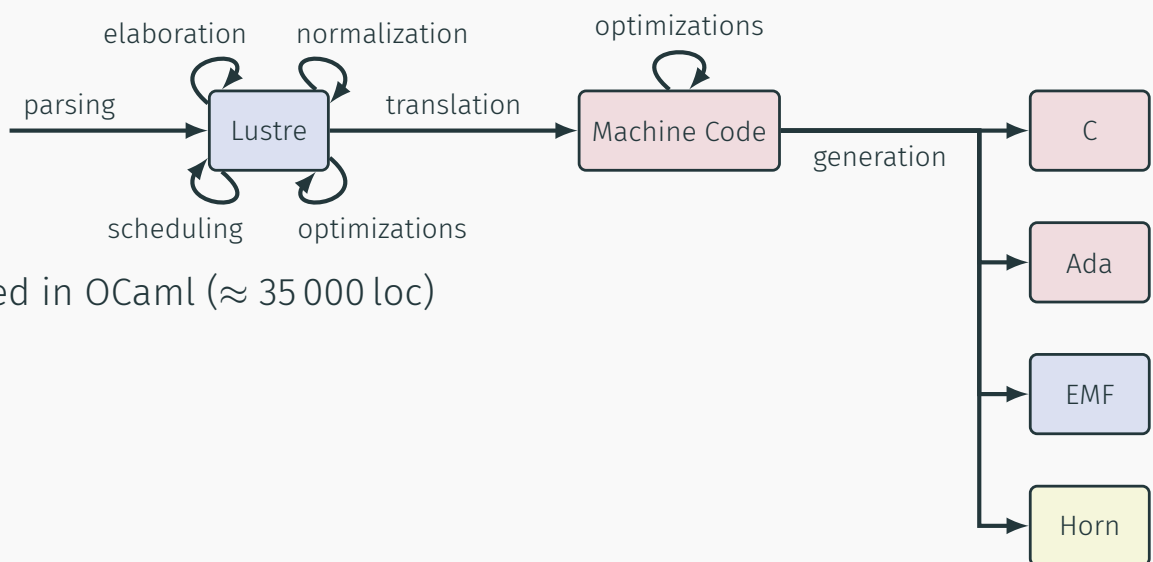


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  automaton a
    state GPS:
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        x = gps;
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        tel until s restart INS
    state INS:
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        tel until s resume GPS
  tel

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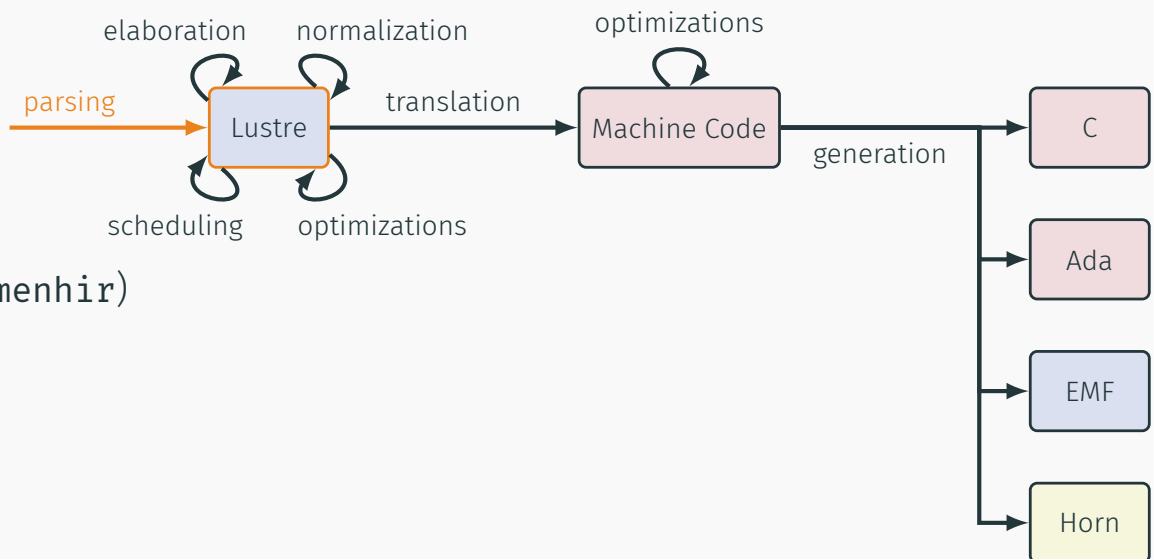
## LUSTREC: A LUSTRE COMPILER



Implemented in OCaml ( $\approx 35\,000$  loc)

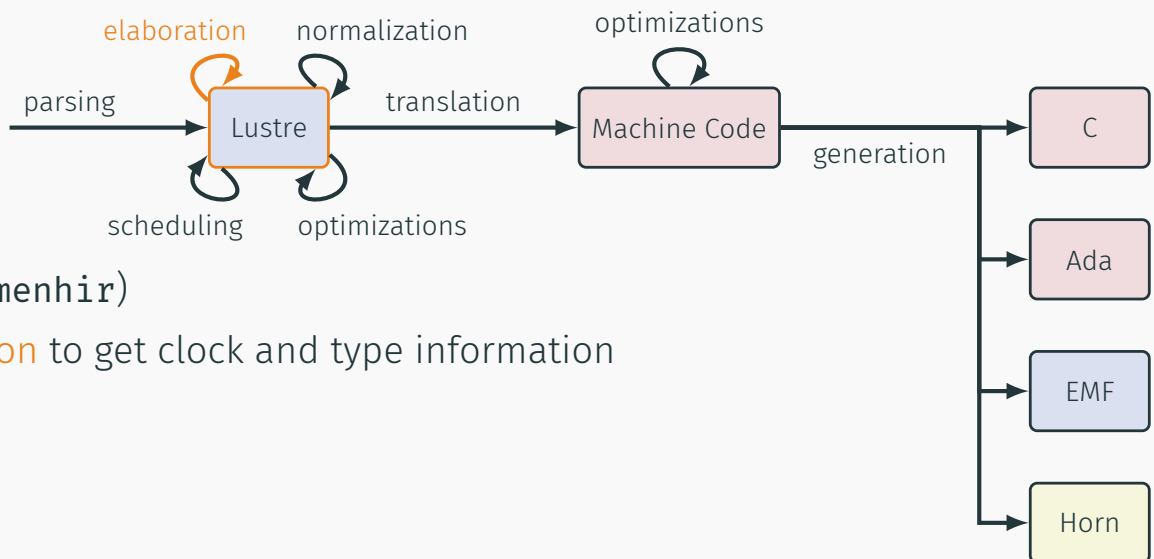


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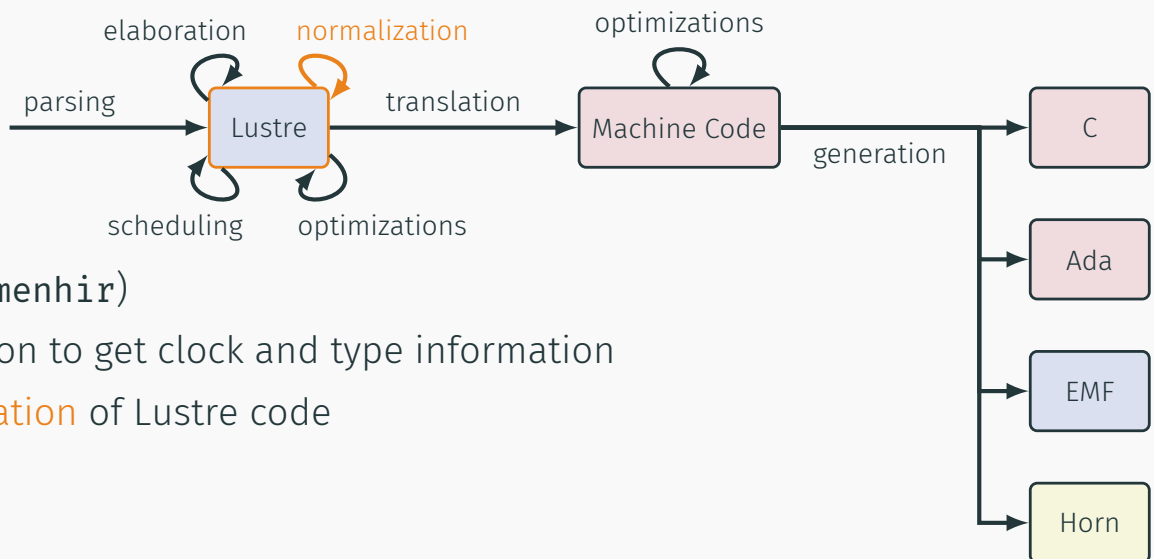
- parsing (menhir)

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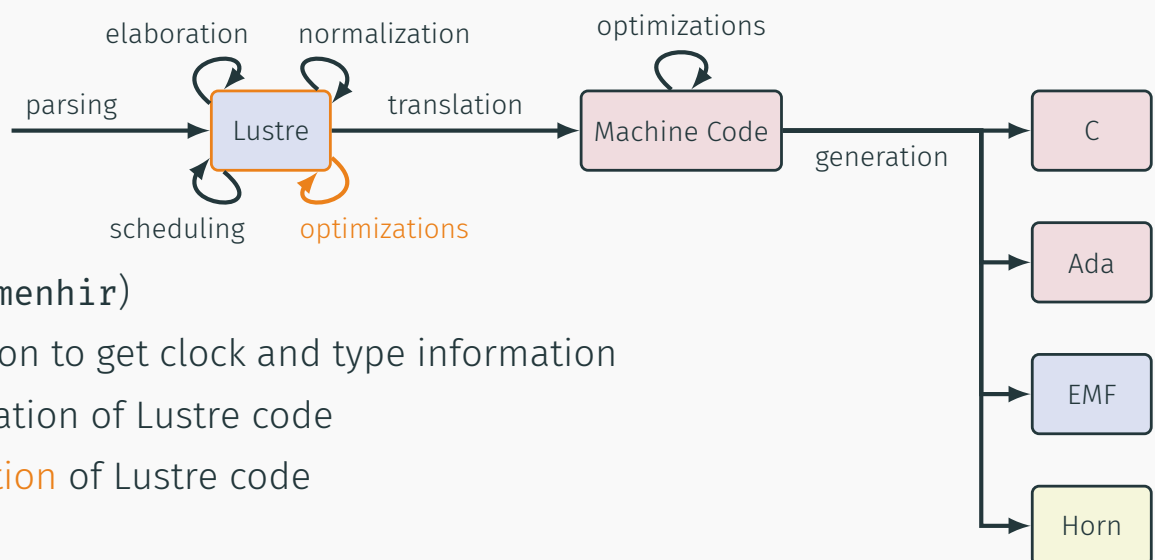
- parsing (menhir)
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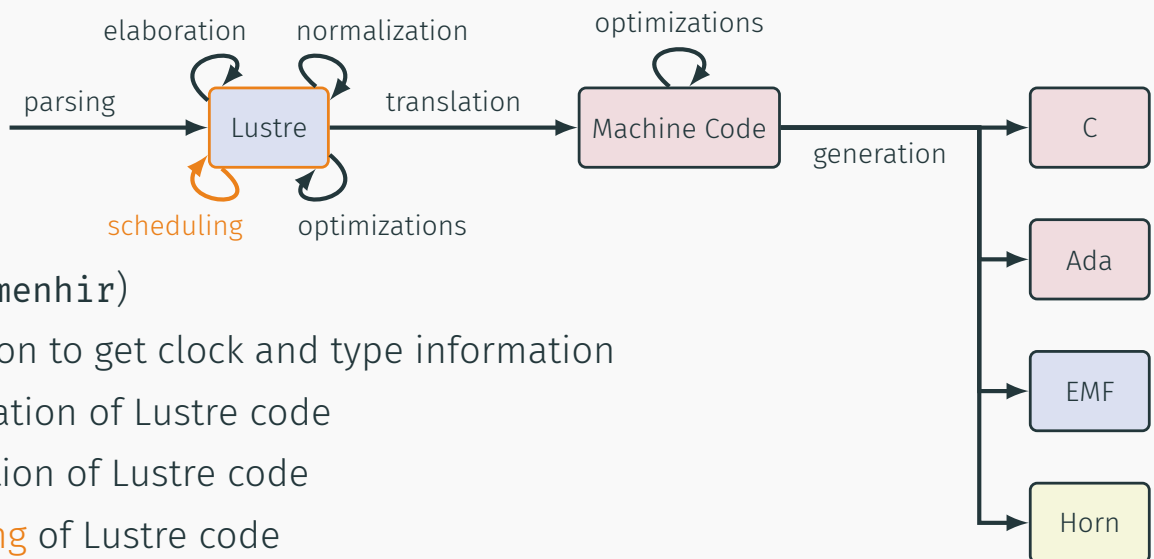
- parsing (menhir)
- elaboration to get clock and type information
- **normalization** of Lustre code

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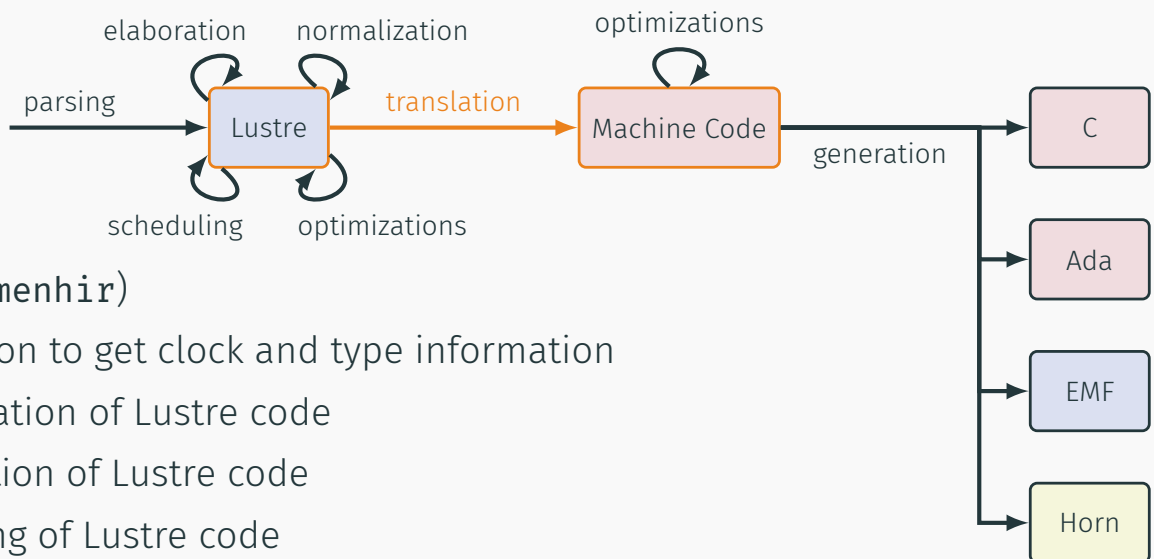
- parsing (menhir)
- elaboration to get clock and type information
- normalization of Lustre code
- **optimization** of Lustre code

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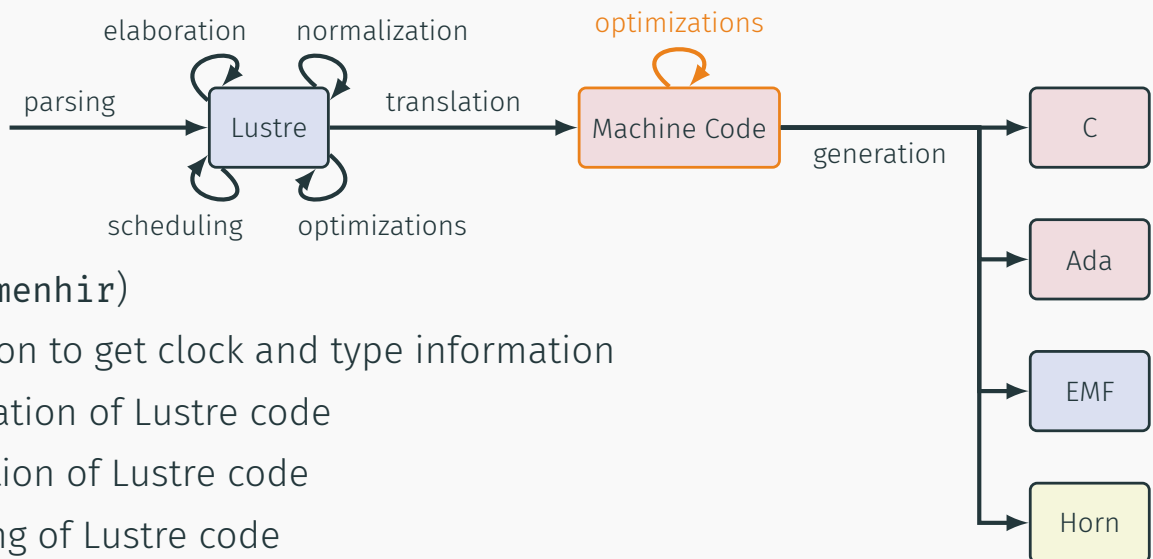
- parsing (menhir)
- elaboration to get clock and type information
- normalization of Lustre code
- optimization of Lustre code
- **scheduling** of Lustre code

## LUSTREC: A LUSTRE COMPILER



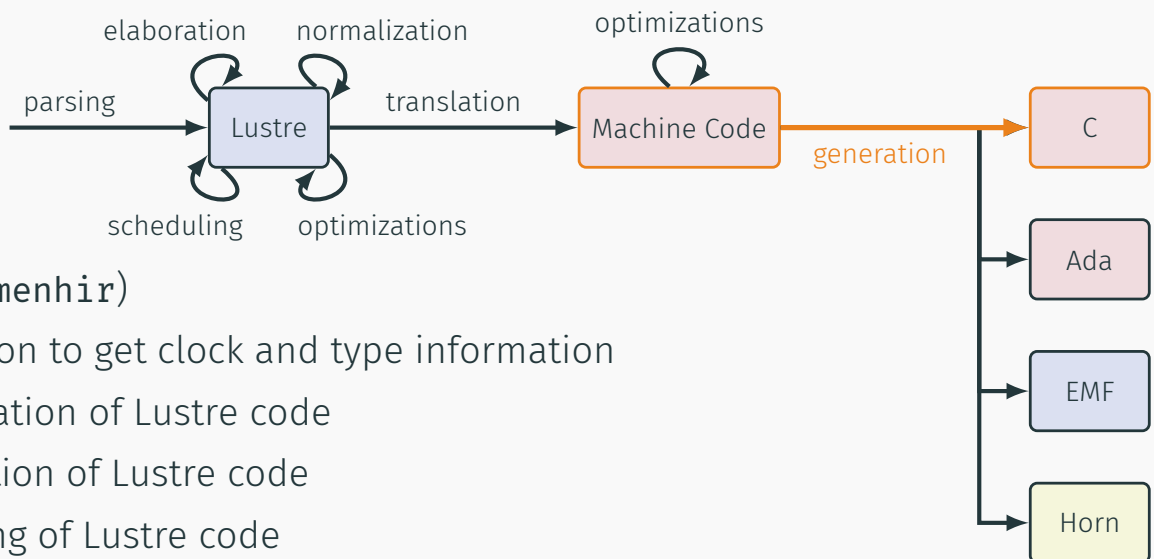
- parsing (**menhir**)
- elaboration to get clock and type information
- normalization of Lustre code
- optimization of Lustre code
- scheduling of Lustre code
- **translation** to Machine code

## LUSTREC: A LUSTRE COMPILER



- parsing (**menhir**)
- elaboration to get clock and type information
- normalization of Lustre code
- optimization of Lustre code
- scheduling of Lustre code
- translation to Machine code
- **optimisation** of Machine code

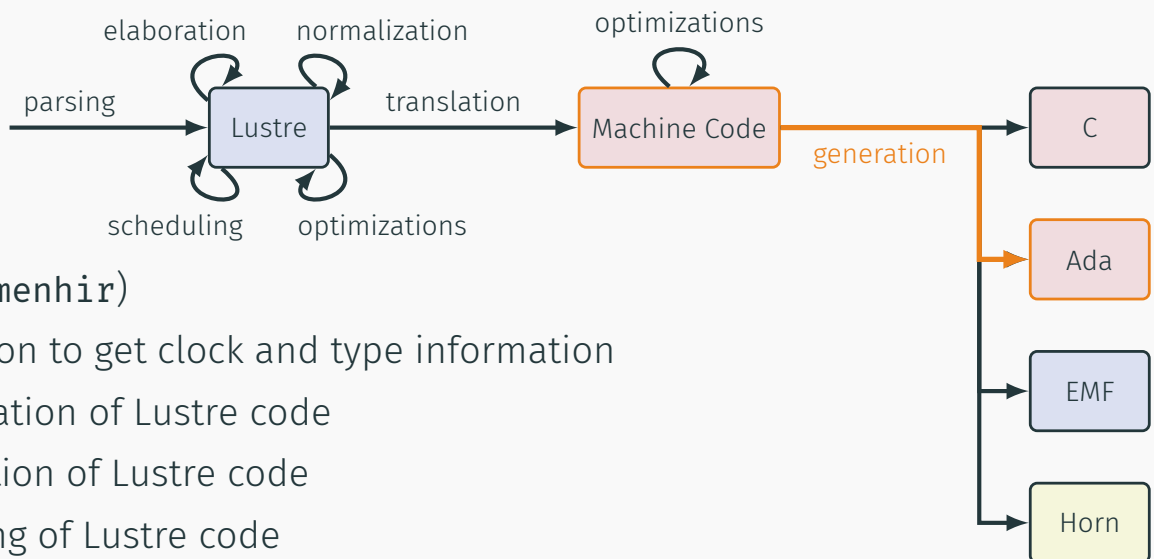
## LUSTREC: A LUSTRE COMPILER



- parsing (**menhir**)
- elaboration to get clock and type information
- normalization of Lustre code
- optimization of Lustre code
- scheduling of Lustre code
- translation to Machine code
- optimisation of Machine code
- **generation** of C code

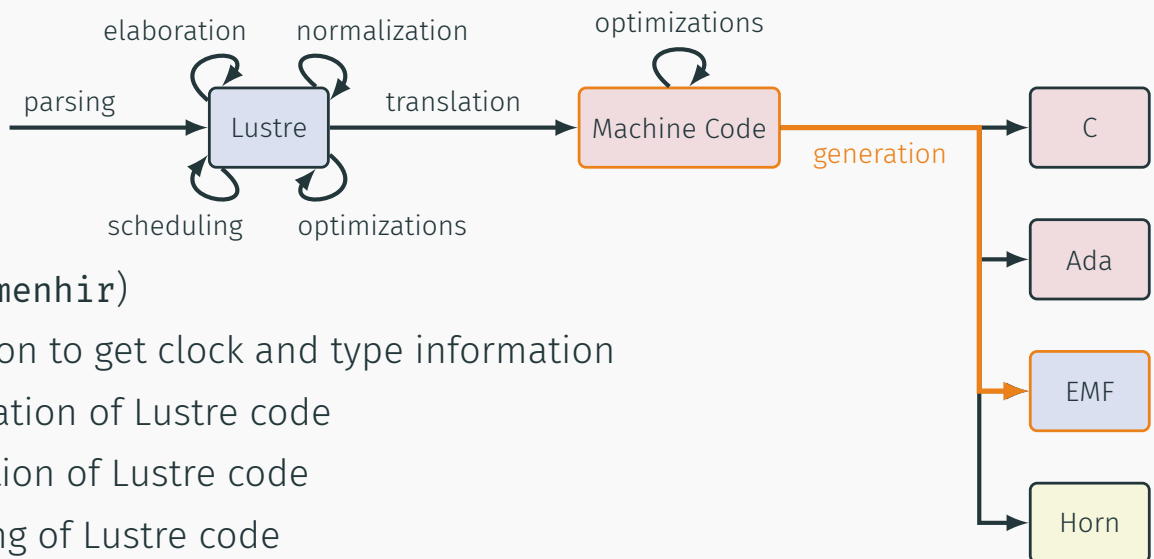


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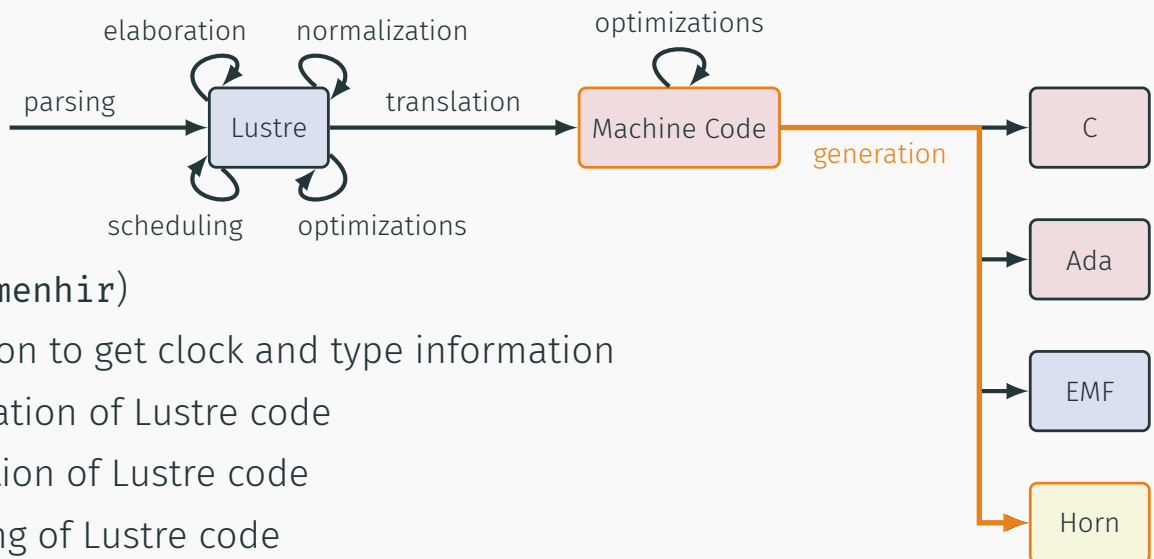
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- normalization of Lustre code
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- scheduling of Lustre code
- translation to Machine code
- optimisation of Machine code
- **generation** of **Ada** code

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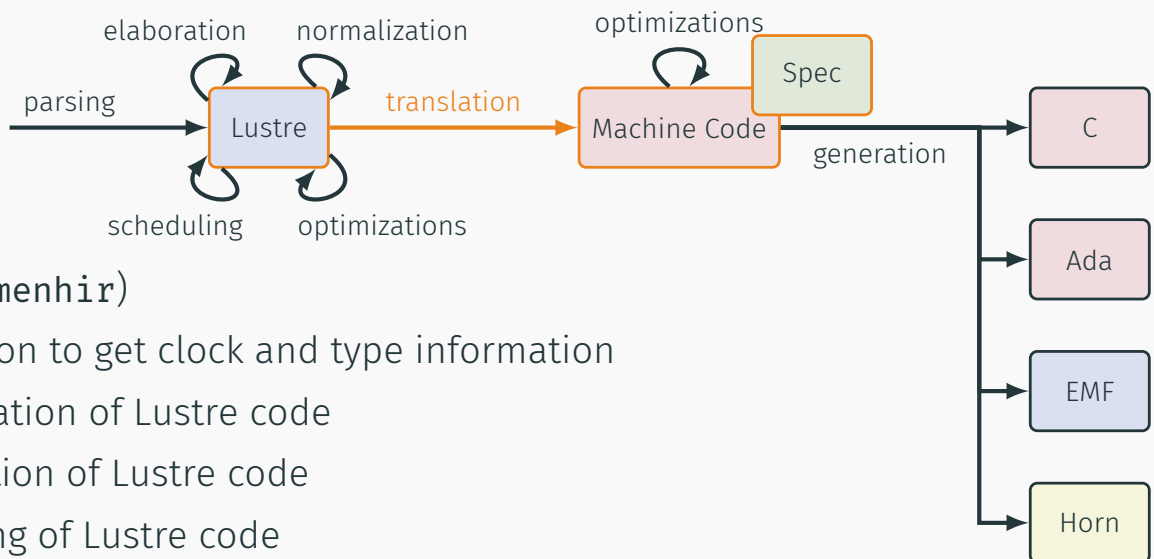
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- **generation** of **EMF** code

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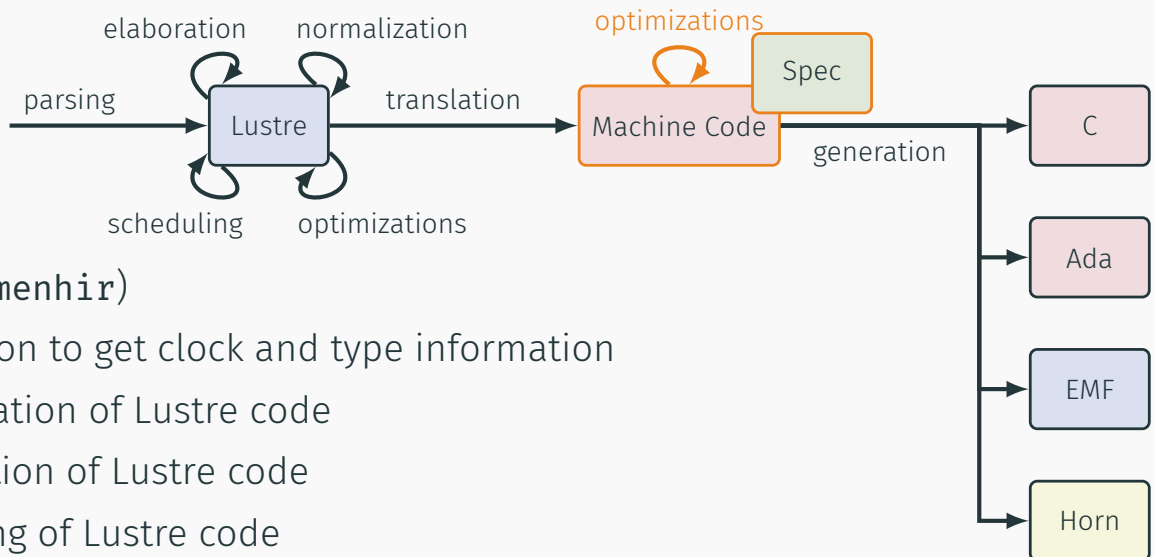
- parsing (**menhir**)
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- normalization of Lustre code
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- optimisation of Machine code
- **generation** of **Horn clauses**

## LUSTREC: A CERTIFYING LUSTRE COMPILER



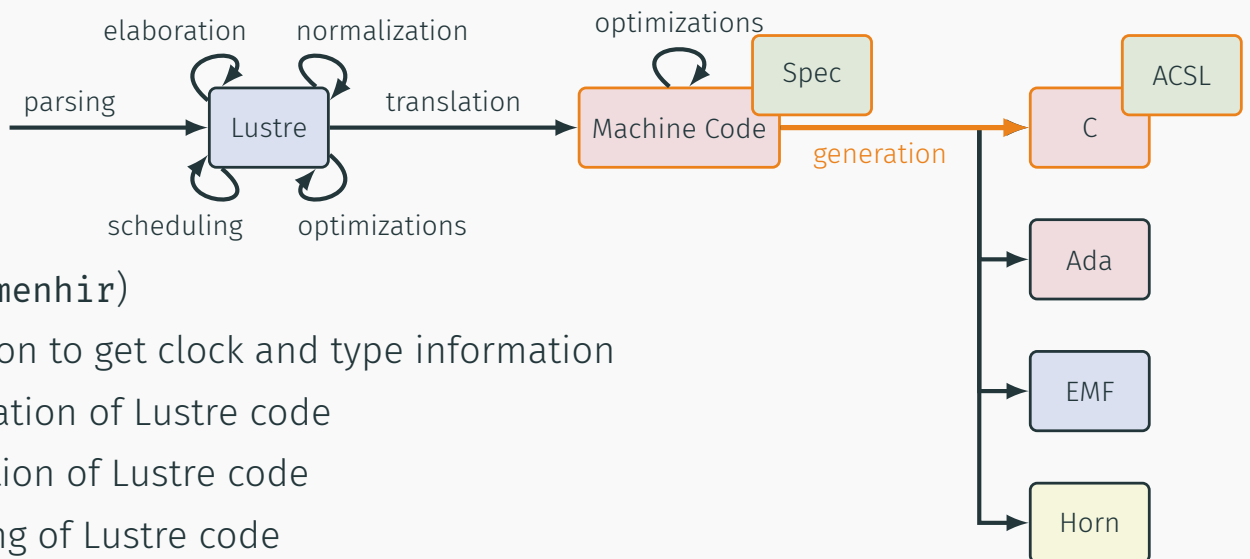
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- translation to Machine code
- **optimisation** of Machine code
- generation of C code

## LUSTREC: A CERTIFYING LUSTRE COMPILER



- parsing (**menhir**)
- elaboration to get clock and type information
- normalization of Lustre code
- optimization of Lustre code
- scheduling of Lustre code
- translation to Machine code
- optimisation of Machine code
- **generation** of C code + **ACSL** specification

# LUSTRE

```
node euler(x0, u: real)
  returns (x: real);
let
  x = x0 fby (x + 0.1 * u);
tel

node ins(gps, xv: real)
  returns (x: real, alarm: bool)
  var pxa, xe: real; k: int;
let
  k = 0 fby (k + 1);
  alarm = (k >= 50);
  xe = euler((gps, xv) when not alarm);
  pxa = (0. fby x) when alarm;
  x = merge alarm pxa xe;
tel

node nav(gps, xv: real, s: bool)
  returns (x: real, alarm: bool)
let
  automaton a
    state GPS:
      let
        x = gps;
        alarm = false;
      tel until s restart INS
    state INS:
      let
        (x, alarm) = ins(gps, xv);
      tel until s resume GPS
tel
```

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node euler(x0, u: real)
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```

#include <assert.h>
#include "lustre.h"
...
node euler(x0, u: real)
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# LUSTRE

# C

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```
#include <assert.h>
#include "lustre.h"

/* ===== automaton ===== */
struct node {
  bool alarm;
  double x;
  double xv;
  double pxa;
  double xe;
  int k;
};

struct ins {
  bool alarm;
  double x;
  double xv;
  double pxa;
  double xe;
  int k;
};

struct nav {
  bool alarm;
  double x;
  double xv;
  double pxa;
  double xe;
  int k;
};

/* ===== main ===== */
int main(int argc, char **argv) {
  struct node node;
  struct ins ins;
  struct nav nav;
  node.x = 0;
  node.xv = 0;
  node.pxa = 0;
  node.xe = 0;
  node.k = 0;
  ins.x = 0;
  ins.xv = 0;
  ins.pxa = 0;
  ins.xe = 0;
  ins.k = 0;
  nav.x = 0;
  nav.xv = 0;
  nav.pxa = 0;
  nav.xe = 0;
  nav.k = 0;
  while (1) {
    /* ===== euler ===== */
    node.xe = euler(node.x, node.xv);
    /* ===== ins ===== */
    (node.x, node.alarm) = ins(node.x, node.xv);
    /* ===== nav ===== */
    (node.x, node.alarm) = nav(node.x, node.xv);
  }
}
```

+ separated code  
for the main loop

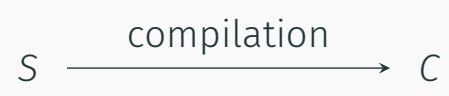
```
node euler(x0, u: real)
  returns (x: real);
let
  x = x0 fby (x + 0.1 * u);
tel

node ins(gps, xv: real)
  returns (x: real, alarm: bool)
  var pxa, xe: real; k: int;
let
  k = 0 fby (k + 1);
  alarm = (k >= 50);
  xe = euler((gps, xv) when not alarm);
  pxa = (0. fby x) when alarm;
  x = merge alarm pxa xe;
tel

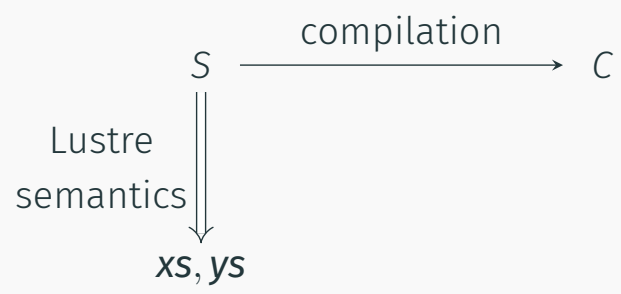
node nav(gps, xv: real, s: bool)
  returns (x: real, alarm: bool)
let
  automaton a
  state GPS:
    let
      x = gps;
      alarm = false;
    tel until s restart INS
  state INS:
    let
      (x, alarm) = ins(gps, xv);
    tel until s resume GPS
tel
```



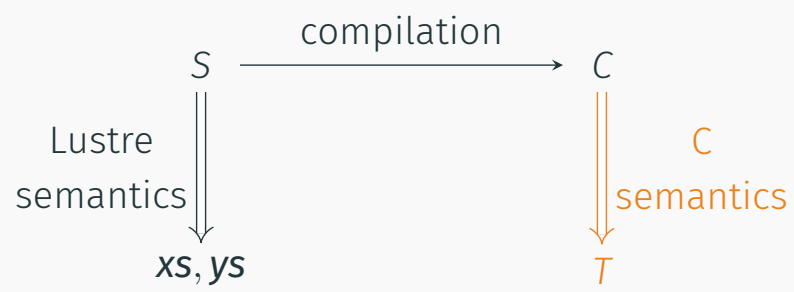
## CORRECTNESS?



## CORRECTNESS?



## CORRECTNESS?



## CORRECTNESS?



## CORRECTNESS?



### LustreC:

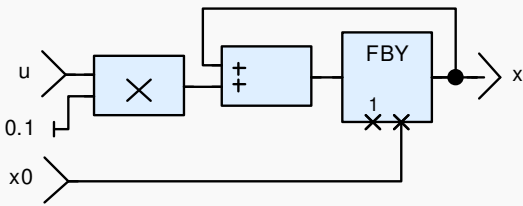
- no easy way to model streams in ACSL
- encoding of a state / transition semantics
- the simulation result is expressed as contracts

## THE COMPILATION SCHEME

---



## EXAMPLE



```
node euler(x0, u: real)
  returns (x: real);
let
  x = x0 fby (x + 0.1 * u);
tel
```

## EXAMPLE: NORMALIZATION

```
node euler(x0, u: real)
  returns (x: real);
let
  x = x0 fby (x + 0.1 * u);
tel
```

```
node euler (x0: real; u: real)
  returns (x: real)
var euler_2: real; euler_1: bool;
let
  x = if euler_1 then x0 else euler_2;
  euler_2 = pre (x + 0.1 * u);
  euler_1 = true -> false;
tel
```

## EXAMPLE: SCHEDULING

```
node euler (x0: real; u: real)
  returns (x: real)
var euler_2: real; euler_1: bool;
let
  x = if euler_1 then x0 else euler_2;
  euler_2 = pre (x + 0.1 * u);
  euler_1 = true -> false;
tel
```

```
node euler (x0: real; u: real)
  returns (x: real)
var euler_2: real; euler_1: bool;
let
  euler_1 = true -> false;
  x = if euler_1 then x0 else euler_2;
  euler_2 = pre (x + 0.1 * u);
tel
```

## EXAMPLE: MACHINE CODE GENERATION

```
node euler (x0: real; u: real)
  returns (x: real)
var euler_2: real; euler_1: bool;
let
  euler_1 = true -> false;
  x = if euler_1 then x0 else euler_2;
  euler_2 = pre (x + 0.1 * u);
tel
```

```
machine euler {
  mem euler_2: real;
  instance ni_0: arrow<>;

  step(x0, u: real) returns (x: double)
  var euler_1: bool;
  {
    euler_1 := ni_0(true, false);
    if euler_1 {
      x := x0
    } else {
      x := euler_2
    };
    euler_2 := x + 0.1 * u;
  }
}
```

## EXAMPLE: C CODE GENERATION

```
machine euler {
  mem euler_2: real;
  instance ni_0: arrow<>;

  step(x0, u: real) returns (x: double)
  var euler_1: bool;
  {
    euler_1 := ni_0(true, false);
    if euler_1 {
      x := x0
    } else {
      x := euler_2
    };
    euler_2 := x + 0.1 * u;
  }
}
```

```
struct _arrow_mem {
  struct _arrow_reg {_Bool _first; } _reg;
};

#define _arrow_reset(self) \
  {(self)->_reg._first = 1;}

_Bool _arrow_step(struct _arrow_mem *self) {
  if (self->_reg._first) {
    self->_reg._first = 0;
    return 1;
  }
  return 0;
}
```

## EXAMPLE: C CODE GENERATION

```
machine euler {
  mem euler_2: real;
  instance ni_0: arrow<>;

  step(x0, u: real) returns (x: double)
  var euler_1: bool;
  {
    euler_1 := ni_0(true, false);
    if euler_1 {
      x := x0
    } else {
      x := euler_2
    };
    euler_2 := x + 0.1 * u;
  }
}
```

```
struct euler_mem {
  _Bool _reset;
  struct euler_reg {double euler_2;} _reg;
  struct _arrow_mem *ni_0;
};
```

## EXAMPLE: C CODE GENERATION

```
machine euler {
  mem euler_2: real;
  instance ni_0: arrow<>;

  step(x0, u: real) returns (x: double)
  var euler_1: bool;
  {
    euler_1 := ni_0(true, false);
    if euler_1 {
      x := x0
    } else {
      x := euler_2
    };
    euler_2 := x + 0.1 * u;
  }
}
```

```
void euler_clear_reset
(struct euler_mem *self)
{
  if (self->_reset) {
    self->_reset = 0;
    _arrow_reset(self->ni_0);
  }
  return;
}

void euler_set_reset
(struct euler_mem *self)
{
  self->_reset = 1;
  return;
}
```

## EXAMPLE: C CODE GENERATION

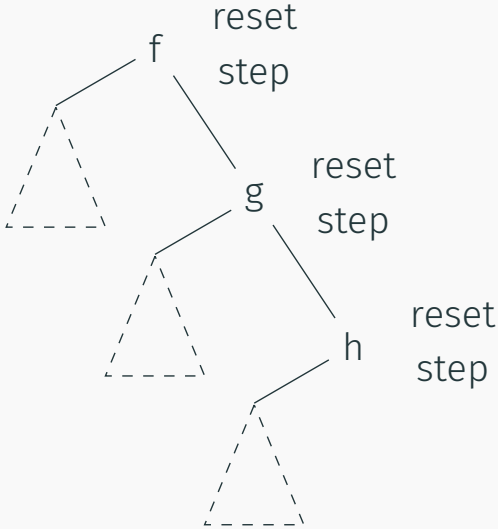
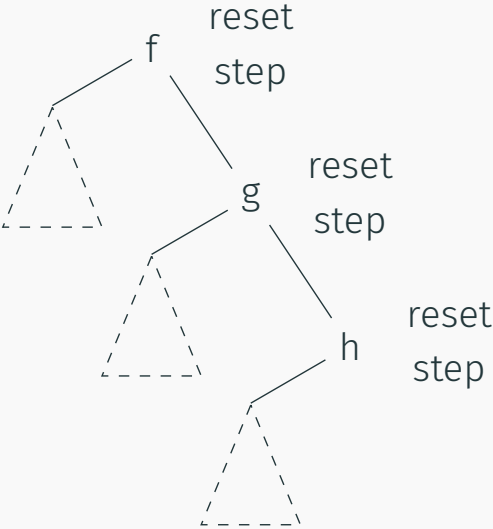
```
machine euler {
  mem euler_2: real;
  instance ni_0: arrow<>;

  step(x0, u: real) returns (x: double)
  var euler_1: bool;
  {
    euler_1 := ni_0(true, false);
    if euler_1 {
      x := x0
    } else {
      x := euler_2
    };
    euler_2 := x + 0.1 * u;
  }
}
```

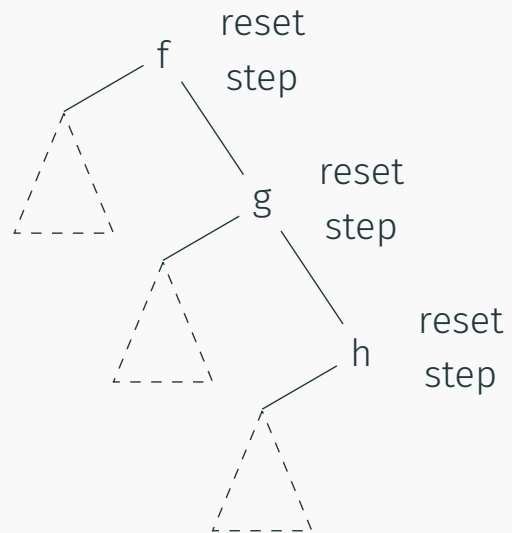
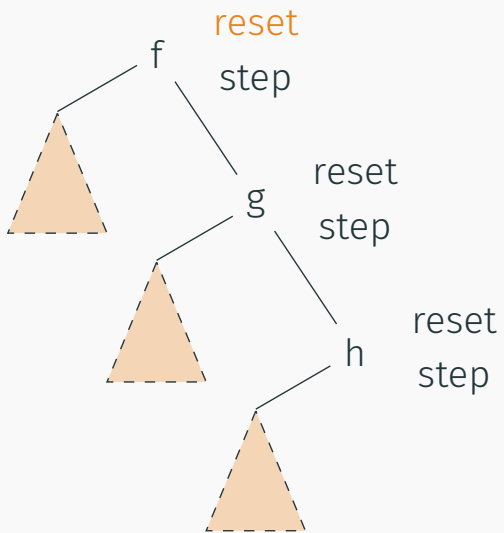
```
void euler_step(double x0, double u,
                double *x,
                struct euler_mem *self) {
  _Bool euler_1;
  euler_clear_reset(self);
  Reset:
  euler_1 = _arrow_step(self->ni_0);
  if (euler_1) {
    *x = x0;
  } else {
    *x = self->_reg.euler_2;
  }
  self->_reg.euler_2 = *x + 0.1 * u;
  return;
}
```



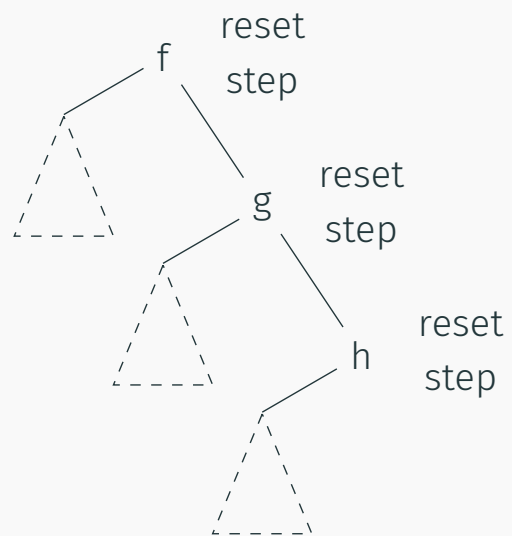
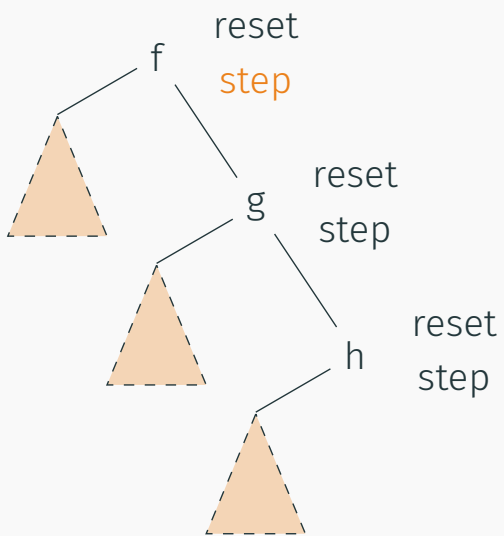
# SCADE-LIKE RESET COMPILATION SCHEME



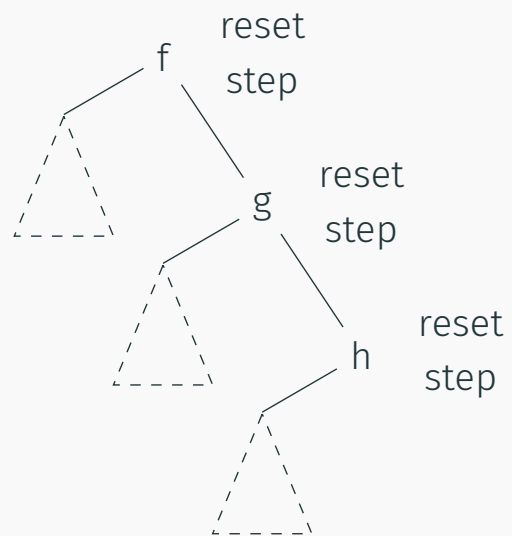
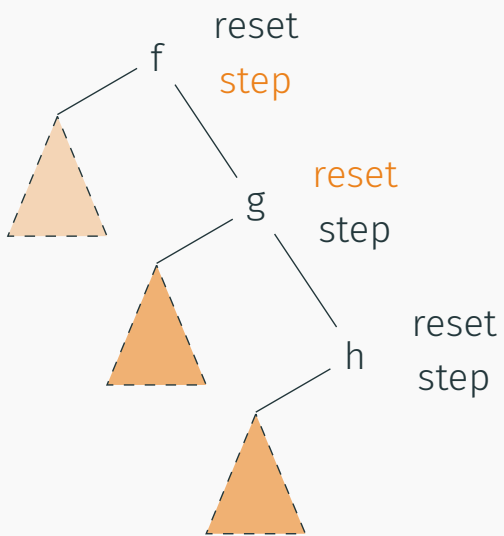
## SCADE-LIKE RESET COMPILATION SCHEME



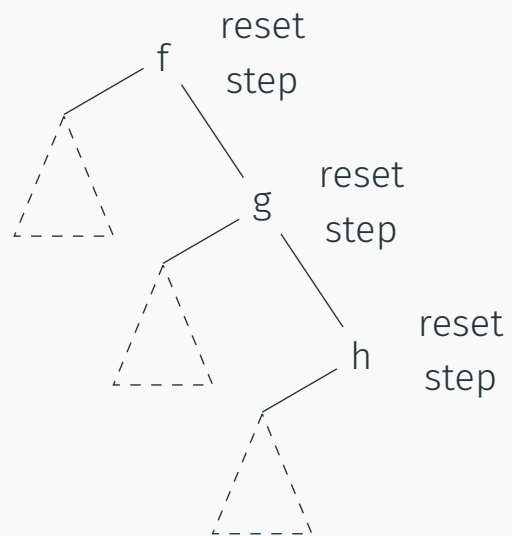
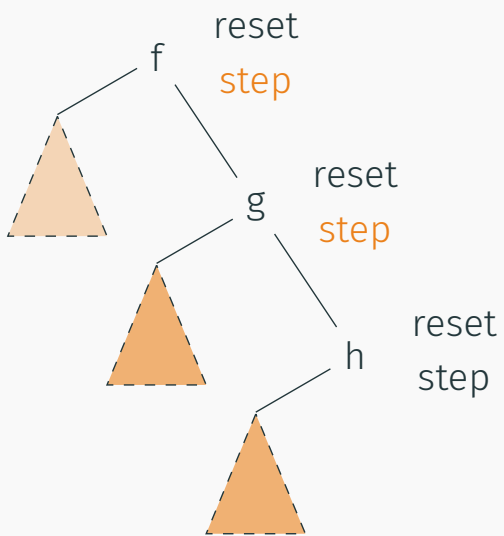
## SCADE-LIKE RESET COMPILATION SCHEME



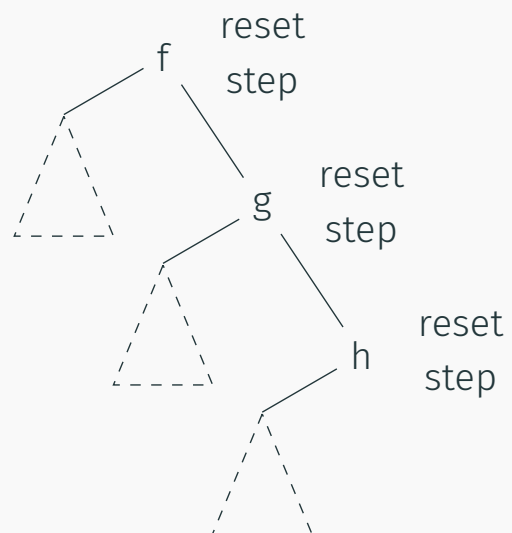
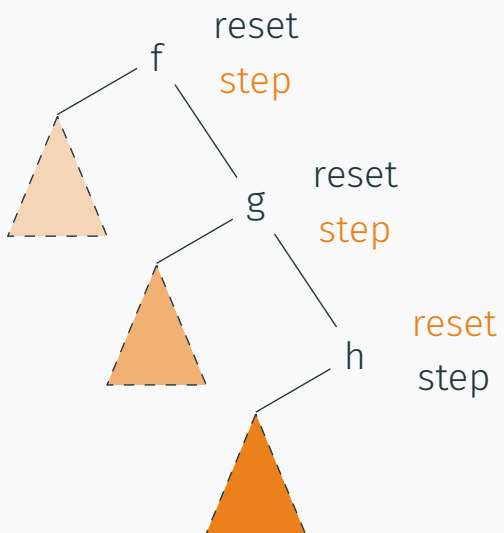
## SCADE-LIKE RESET COMPILATION SCHEME



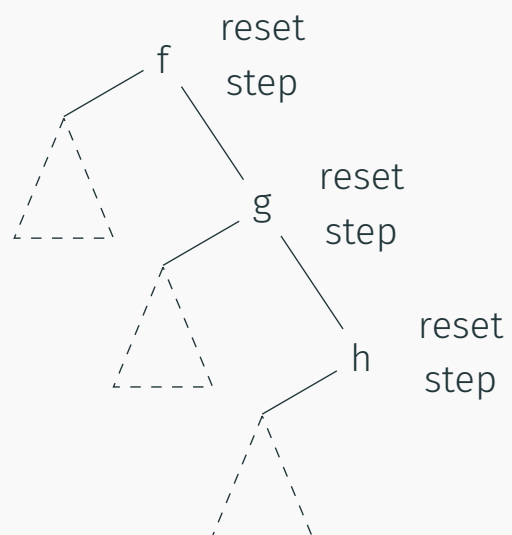
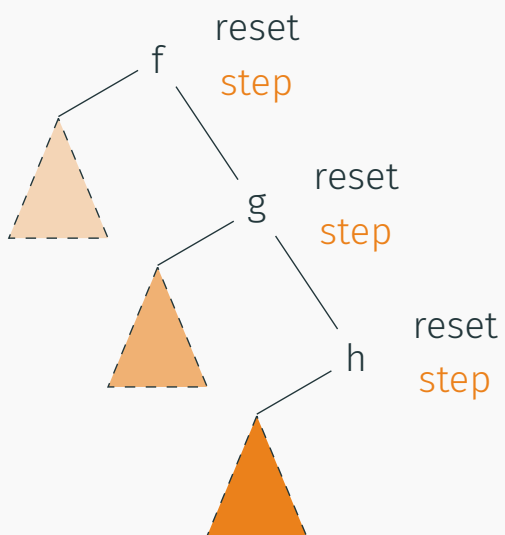
## SCADE-LIKE RESET COMPILATION SCHEME



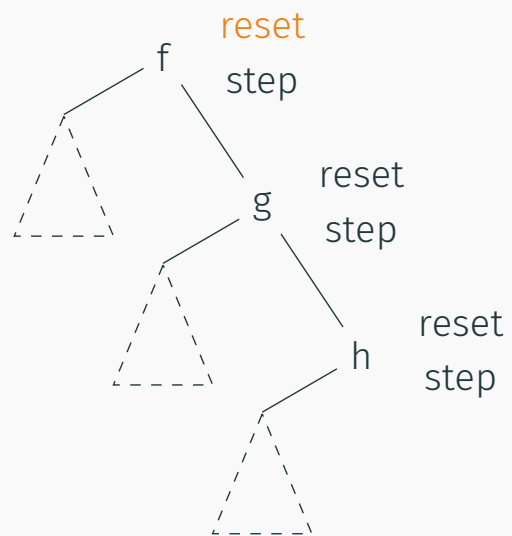
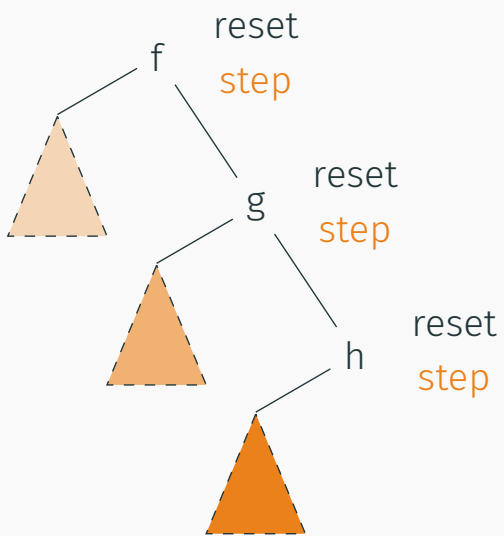
## SCADE-LIKE RESET COMPILATION SCHEME



## SCADE-LIKE RESET COMPILATION SCHEME

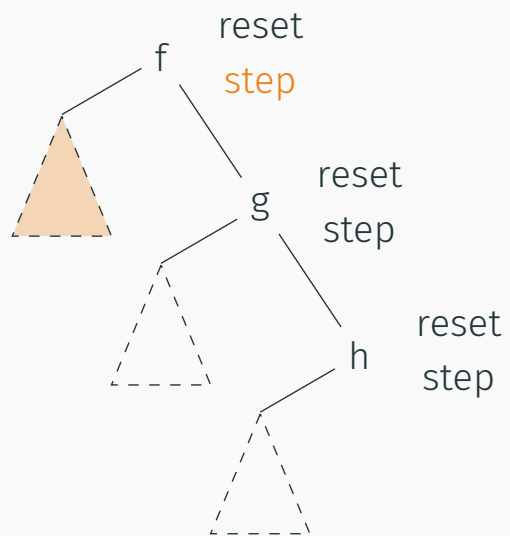
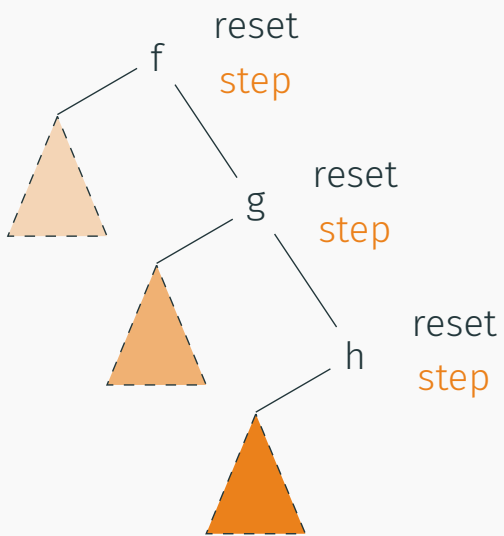


## SCADE-LIKE RESET COMPILATION SCHEME

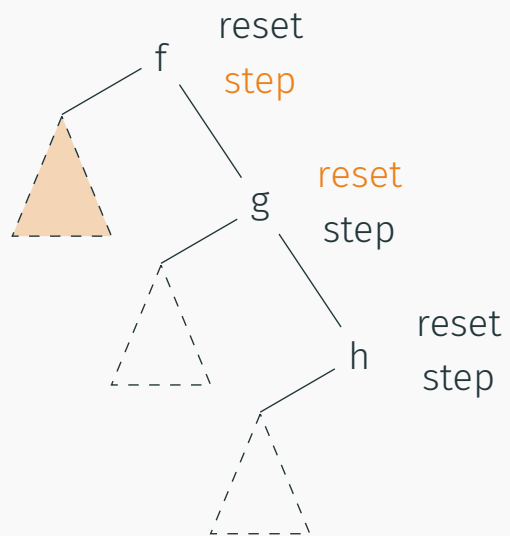
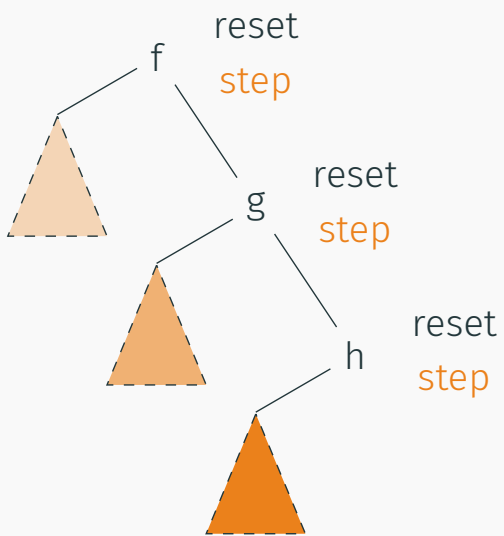




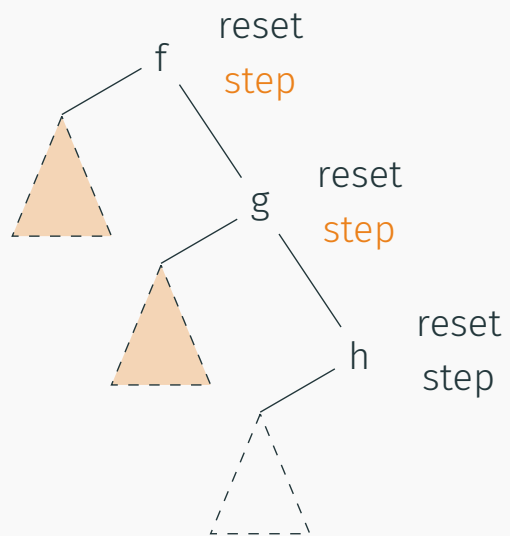
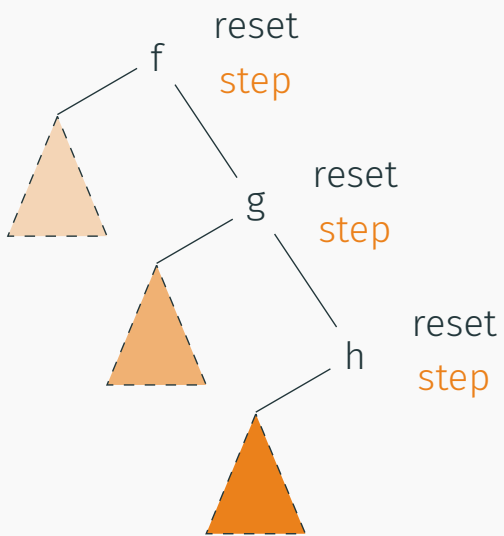
## SCADE-LIKE RESET COMPILATION SCHEME



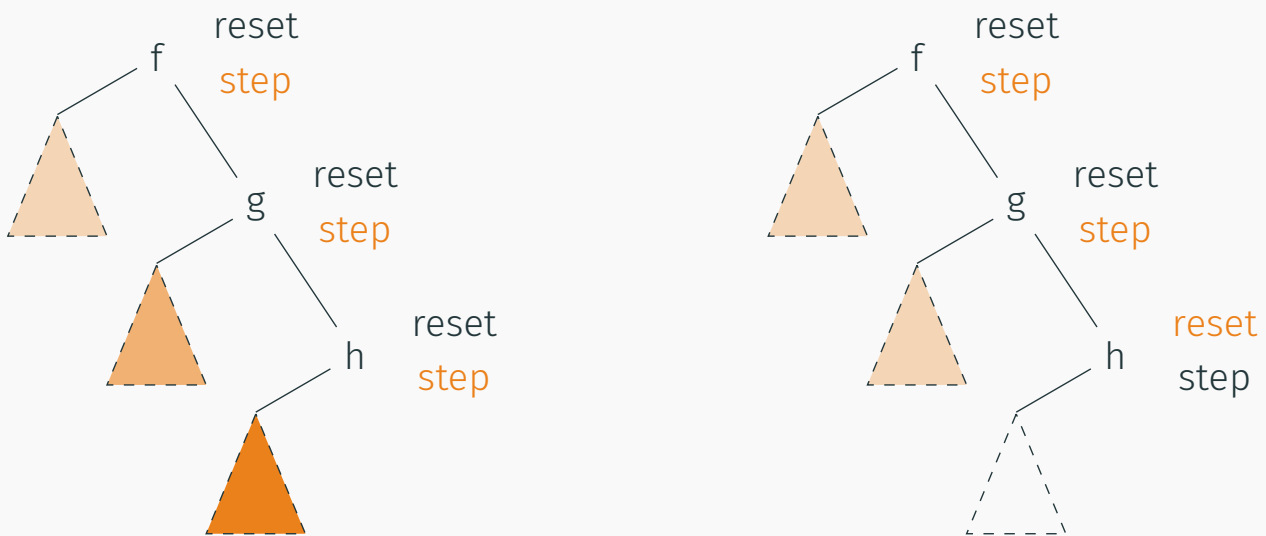
## SCADE-LIKE RESET COMPILATION SCHEME



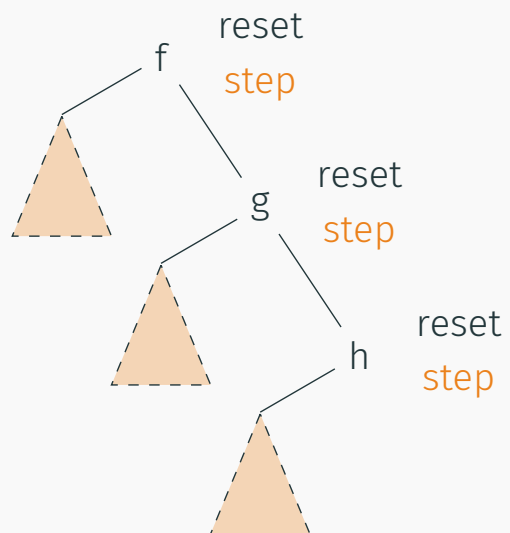
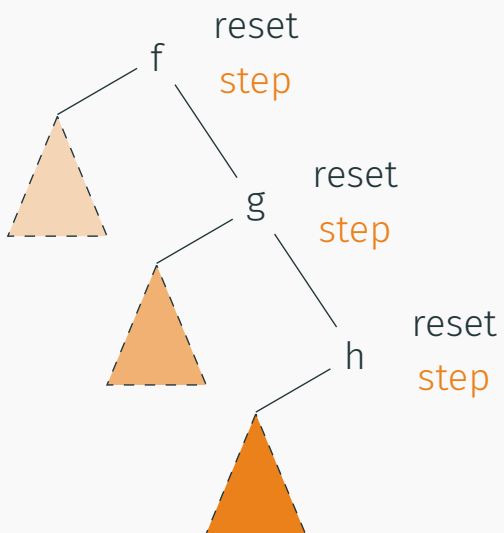
## SCADE-LIKE RESET COMPILATION SCHEME



## SCADE-LIKE RESET COMPILATION SCHEME



## SCADE-LIKE RESET COMPILATION SCHEME



## ENCODING OF THE SEMANTICS

---

## STATE / TRANSITION SEMANTICS

```
node euler (x0: real; u: real)
  returns (x: real)
var euler_2: real; euler_1: bool;
let
  euler_1 = true -> false;
  x = if euler_1 then x0 else euler_2;
  euler_2 = pre (x + 0.1 * u);
tel
```

$euler\_init(S) =$

$arrow\_init(S[ni_0])$

$euler\_reset(S, S') =$

$S(\_reset) \rightarrow S'(\_reset) = false$

$\wedge euler\_init(S')$

$\wedge \neg S(\_reset) \rightarrow S' = S$

## STATE / TRANSITION SEMANTICS

```
node euler (x0: real; u: real)
  returns (x: real)
var euler_2: real; euler_1: bool;
let
  euler_1 = true -> false;
  x = if euler_1 then x0 else euler_2;
  euler_2 = pre (x + 0.1 * u);
tel
```

$$\begin{aligned} euler\_tr(S, x_0, u, x, S') = & \\ & \exists S_r, \\ & euler\_reset(S, S_r) \\ & \wedge S'(\_reset) = S_r(\_reset) \\ & \wedge \exists euler_1, \\ & \quad arrow\_tr(S_r[ni_0], euler_1, S'[ni_0]) \\ & \quad \wedge euler_1 \rightarrow x = x_0 \\ & \quad \wedge \neg euler_1 \rightarrow x = S_r(euler_2) \\ & \quad \wedge S'(euler_2) = x + 0.1 \times u \end{aligned}$$



## MACHINE CODE SPECIFICATION GENERATION

- Internal AST for an ad-hoc first order logic
- Generation from each Lustre equation
- Optimizations

## ACSL GENERATION: MEMORY CORRESPONDENCE

Notion of state in ACSL: same C structures, *flattened*

```
struct _arrow_mem {
    struct _arrow_reg {_Bool _first; } _reg;
};

struct euler_mem {
    _Bool _reset;
    struct euler_reg {double euler_2;} _reg;
    struct _arrow_mem *ni_0;
};

/*@ ghost struct _arrow_mem_ghost {
    struct _arrow_reg _reg;
};
*/

/*@ ghost struct euler_mem_ghost {
    _Bool _reset;
    struct euler_reg _reg;
    struct _arrow_mem_ghost ni_0;
};
*/
```

## ACSL GENERATION: MEMORY CORRESPONDENCE

```
/*@ predicate euler_pack0(struct euler_mem_ghost mem, struct euler_mem *self) =
    mem._reset == self->_reset
    && mem._reset == 0;
*/
/*@ predicate euler_pack1(struct euler_mem_ghost mem, struct euler_mem *self) =
    euler_pack0(mem, self)
    && _arrow_pack(mem.ni_0, self->ni_0);
*/
/*@ predicate euler_pack2(struct euler_mem_ghost mem, struct euler_mem *self) =
    euler_pack1(mem, self);
*/
/*@ predicate euler_pack3(struct euler_mem_ghost mem, struct euler_mem *self) =
    euler_pack2(mem, self)
    && !_arrow_initialization(mem.ni_0) ==> mem._reg.euler_2 == self->_reg.euler_2;
*/
/*@ predicate euler_pack(struct euler_mem_ghost mem, struct euler_mem *self) =
    (mem._reset ? mem._reset == self->_reset : euler_pack3(mem, self));
*/
```

## ACSL GENERATION: TRANSITION RELATION

```
euler_init(S) =
  arrow_init(S[ni_0])

euler_reset(S, S') =
  S(_reset) → S'(_reset) = false
  ∧ euler_init(S')
  ∧ ¬S(_reset) → S' = S

/*@ predicate euler_init(struct euler_mem_ghost mem_in) =
    _arrow_init(mem_in.ni_0);
*/

/*@ predicate euler_reset(struct euler_mem_ghost mem_in,
    struct euler_mem_ghost mem_out) =
    mem_in._reset ? mem_out._reset == 0
    && euler_init(mem_out)
    : mem_out == mem_in;
*/
```

## ACSL GENERATION: TRANSITION RELATION

```
euler_tr(S, x0, u, x, S') =  
  ∃S_r,  
    euler_reset(S, S_r)                                /*@ predicate euler_tr(struct euler_mem_ghost mem_in,  
    ∧ S'(_reset) = S_r(_reset)                          double x0, double u, double x,  
    ∧ ∃euler_1,                                         struct euler_mem_ghost mem_out) =  
    ∧ arrow_tr(S_r[ni0], euler_1, S'[ni0])             \exists struct euler_mem_ghost mem_reset;  
    ∧ euler_1 → x = x0                                  euler_reset(mem_in, mem_reset)  
    ∧ ¬euler_1 → x = S_r(euler_2)                       && euler_tr3(mem_reset, x0, u, x, mem_out);  
    ∧ S'(euler_2) = x + 0.1 × u                          */
```

## ACSL GENERATION: TRANSITION RELATION

```
euler_tr (S, x0, u, x, S') =  
  ∃S_r,  
    euler_reset (S, S_r)                               /*@ predicate euler_tr3(struct euler_mem_ghost mem_in,  
    ∧ S'(_reset) = S_r(_reset)                          double x0, double u, double x,  
    ∧ ∃euler_1,                                          struct euler_mem_ghost mem_out) =  
    ∧ arrow_tr (S_r[ni0], euler_1, S'[ni0])            euler_tr2(mem_in, x0, u, x, mem_out)  
    /*                                                    && mem_out._reg.euler_2 == x + 0.1 * u;  
    ∧ euler_1 → x = x0  
    ∧ ¬euler_1 → x = S_r(euler_2)  
    ∧ S'(euler_2) = x + 0.1 × u
```

## ACSL GENERATION: TRANSITION RELATION

```
euler_tr (S, x0, u, x, S') =  
  ∃S_r,                                     /*@ predicate euler_tr2(struct euler_mem_ghost mem_in,  
    euler_reset (S, S_r)                    double x0, double u, double x,  
    ∧ S'(_reset) = S_r(_reset)              struct euler_mem_ghost mem_out) =  
    ∧ ∃euler_1,                             \exists _Bool euler_1;  
      ∧ arrow_tr (S_r[ni_0], euler_1, S'[ni_0])  euler_tr1(mem_in, x0, u, euler_1, mem_out)  
      ∧ euler_1 → x = x0                       && euler_1 ? x == x0  
      ∧ ¬euler_1 → x = S_r(euler_2)           : !_arrow_init(mem_in.ni_0) ==>  
      ∧ S'(euler_2) = x + 0.1 × u              x == mem_in._reg.euler_2;  
*/
```

## ACSL GENERATION: TRANSITION RELATION

$euler\_tr(S, x_0, u, x, S') =$

$\exists S_r,$

$euler\_reset(S, S_r)$

$\wedge S'(\_reset) = S_r(\_reset)$

$\wedge \exists euler_1,$

$\wedge \text{arrow\_tr}(S_r[ni_0], euler_1, S'[ni_0])$  *\*/*

$\wedge euler_1 \rightarrow x = x_0$

$\wedge \neg euler_1 \rightarrow x = S_r(euler_2)$

$\wedge S'(euler_2) = x + 0.1 \times u$

```
/*@ predicate euler_tr1(struct euler_mem_ghost mem_in,  
                        double x0, double u, _Bool euler_1,  
                        struct euler_mem_ghost mem_out) =  
    euler_tr0(mem_in, x0, u, mem_out)  
    && _arrow_tr(mem_in.ni_0, euler_1, mem_out.ni_0);
```



## ACSL GENERATION: TRANSITION RELATION

```
euler_tr (S, x0, u, x, S') =  
  ∃S_r,  
    euler_reset (S, S_r)                               /*@ predicate euler_tr0(struct euler_mem_ghost mem_in,  
    ∧ S'(_reset) = S_r(_reset)                          double x0, double u,  
    ∧ ∃euler_1,                                         struct euler_mem_ghost mem_out) =  
    ∧ arrow_tr (S_r[ni0], euler_1, S'[ni0]) */         mem_out._reset == mem_in._reset;  
    ∧ euler_1 → x = x0  
    ∧ ¬euler_1 → x = S_r(euler_2)  
    ∧ S'(euler_2) = x + 0.1 × u
```

## ACSL GENERATION: CONTRACTS AND ASSERTIONS

```
/*@ requires euler_valid(self);
   requires \separated(self, mem,
                       self->ni_0);
   requires euler_pack(*mem, self);
   ensures euler_pack3(*mem, self);
   assigns self->_reset, self->ni_0->_reg,
           mem->_reset, mem->ni_0._reg;
   behavior reset:
       assumes mem->_reset == 1;
       ensures euler_init(*mem);
   behavior no_reset:
       assumes mem->_reset == 0;
       ensures *mem == \old(*mem);
   complete behaviors;
   disjoint behaviors;
*/

void euler_clear_reset
(struct euler_mem *self)
/*@ ghost
 (struct euler_mem_ghost \ghost *mem) */
{
    if (self->_reset) {
        self->_reset = 0;
        //@ ghost mem->_reset = 0;
        _arrow_reset(self->ni_0);
        //@ ghost _arrow_reset_ghost(mem->ni_0);
    }
    return;
}
```

## ACSL GENERATION: CONTRACTS AND ASSERTIONS

```
/*@ ensures euler_pack(*mem, self);
   ensures mem->_reset == 1;
   assigns self->_reset, mem->_reset;
*/
void euler_set_reset(struct euler_mem *self)
/*@ ghost (struct euler_mem_ghost \ghost *mem) */ {
    self->_reset = 1;
    //@ ghost mem->_reset = 1;
    return;
}
```

## ACSL GENERATION: CONTRACTS AND ASSERTIONS

```
/*@ requires \valid(x);
   requires euler_valid(self);
   requires \separated(self, mem, self->ni_0, x);
   requires euler_pack(*mem, self);
   ensures euler_pack(*mem, self);
   ensures euler_tr(\old(*mem), x0, u, *x, *mem);
   assigns *x, self->_reg, self->_reset, self->ni_0->_reg,
          mem->_reg, mem->_reset, mem->ni_0._reg;
*/
```

## ACSL GENERATION: CONTRACTS AND ASSERTIONS

```
void euler_step(double x0, double u,
               double *x,
               struct euler_mem *self)
/*@ ghost
 (struct euler_mem_ghost \ghost *mem) */
{
  _Bool euler_1;
  euler_clear_reset(self)/*@ ghost (mem) */;
  Reset:
  //@ assert euler_pack0(*mem, self);
  //@ assert euler_tr0
    (\at(*mem, Reset), x0, u, *mem); */
  euler_1 = _arrow_step(self->ni_0)
    /*@ ghost (&mem->ni_0) */;
  //@ assert euler_pack1(*mem, self);
  //@ assert euler_tr1
    (\at(*mem, Reset),
     x0, u, euler_1, *mem); */

  if (euler_1) {
    *x = x0;
  } else {
    *x = self->_reg.euler_2;
  }
  //@ assert euler_pack2((*mem), self);
  //@ assert euler_tr2
    (\at(*mem, Reset), x0, u, *x, *mem); */
  self->_reg.euler_2 = *x + 0.1 * u;
  //@ ghost mem->_reg.euler_2 = *x + 0.1 * u;
  //@ assert euler_pack3(*mem, self);
  //@ assert euler_tr3
    (\at(*mem, Reset), x0, u, *x, *mem); */
  return;
}
```

# FRAMA-C

File Project Analyses Help

Name

- euler\_step
- euler\_transition
- euler\_transition0
- euler\_transition1
- euler\_transition1\_footprint
- euler\_transition2
- euler\_transition2\_footprint
- euler\_transition3
- euler\_valid
- ins\_clear\_reset
- ins\_initialization
- ins\_pack
- ins\_pack0
- ins\_pack1
- ins\_pack10
- ins\_pack2
- ins\_pack3
- ins\_pack4
- ins\_pack5
- ins\_pack6
- ins\_pack7
- ins\_pack8
- ins\_pack9
- ins\_reset\_cleared
- ins\_set\_reset
- ins\_step

WP

60 - + timeout

16 - + process

Model... Provers... Update

- Occurrence
- Metrics
- Impact
- Slicing
- Eva

```

1442 /*@ requires \valid(x);
1443 /*@ requires euler_valid(self);
1444 /*@ requires \separated(self, mem, self->ni_7, x);
1445 /*@ requires euler_pack(*mem, self);
1446 /*@ ensures euler_pack(*old(mem), \old(self));
1447 /*@ ensures
1448     euler_transition(\old(*mem), \old(x0), \old(u), *old(x), *old(mem));
1449 /*@ assigns *x, self->reg.__euler_2, self->_reset, (self->ni_7)->reg.__first,
1450     mem->reg.__euler_2, mem->_reset, mem->ni_7.__reg.__first;
1451 */
1452 void euler_step(double x0, double u, double *x, struct euler_mem *self)
1453 /*@ ghost (struct euler_mem_ghost \ghost *mem) */
1454 {
1455     Bool __euler_1;
1456     euler_clear_reset(self) /*@ ghost (mem) */;
1457     Reset: /*@ assert euler_pack0(*mem, self); */;
1458     /*@ assert euler_transition0(\at(*mem, Reset), x0, u, *mem); */;
1459     __euler_1 = __arrow_step(self->ni_7) /*@ ghost (&mem->ni_7) */;
1460     /*@ assert euler_pack1(*mem, self); */;
1461     /*@ assert euler_transition1(\at(*mem, Reset), x0, u, __euler_1, *mem); */;
1462     if ( __euler_1 ) {
1463         *x = x0;
1464     }
1465     else {
1466         *x = self->reg.__euler_2;
1467     }
1468     /*@ assert euler_pack2(*mem, self); */;
1469 }

```

nav\_automaton.c

```

1442
1443     assigns mem->reg.__euler_2;
1444     assigns mem->_reset;
1445
1446     assigns mem->ni_7.__reg.__first;
1447
1448 */
1449 void euler_step (double x0, double u,
1450                 double (*x),
1451                 struct euler_mem *self)
1452 /*@ ghost (struct euler_mem_ghost \ghost *mem) */ {
1453     Bool __euler_1;
1454     euler_clear_reset(self) /*@ ghost (mem) */;
1455     Reset:
1456     /*@ assert euler_pack0(*mem, self); */
1457     /*@ assert euler_transition0(\at(*mem, Reset), x0, u, (*mem)); */
1458     __euler_1 = __arrow_step(self->ni_7) /*@ ghost (&mem->ni_7) */;
1459     /*@ assert euler_pack1(*mem, self); */
1460     /*@ assert euler_transition1(\at(*mem, Reset), x0, u, __euler_1,
1461                                *x); */
1462     if ( __euler_1 ) {
1463         *x = x0;
1464     }
1465     else {
1466         *x = self->reg.__euler_2;
1467     }
1468     /*@ assert euler_pack2(*mem, self); */
1469 }

```

Information Messages (19) Console Properties Values Red Alarms WP Goals

Global All Goals Provers... Clear

Module	Goal	Model	Qed	Script	Alt-Ergo 2.4.1	CVC4 1.6	Z3 4.8.6
euler_set_reset	Assigns ...	Typed (Ref) (Real)	●	-			
euler_step	Post-condition	Typed (Ref) (Real)	-	-	●	●	
euler_step	Post-condition	Typed (Ref) (Real)	-	-		●	
euler_step	Assertion	Typed (Ref) (Real)	-	-	●	●	●
euler_step	Assertion	Typed (Ref) (Real)	-	-	●	●	●
euler_step	Assertion	Typed (Ref) (Real)	-	-	●	●	●
euler_step	Assertion	Typed (Ref) (Real)	-	-	●	●	●
euler_step	Assertion	Typed (Ref) (Real)	-	-	●	●	●
euler_step	Assertion	Typed (Ref) (Real)	-	-	●	●	●
euler_step	Assertion	Typed (Ref) (Real)	-	-	●	●	●
euler_step	Assigns ... (exit)	Typed (Ref) (Real)	●	-			

# CONTRACT TRANSLATION

---

## PRINCIPLES

### High-level specification

- contracts expressed at dataflow level
- verified by model checking techniques (eg. Kind2)



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### Logical meaning

- synchronous observers
- $\Box (\mathcal{H} (Pre(S, x)) \wedge tr(S, x, y, S') \rightarrow Post(S, x, y, S'))$

## PRINCIPLES

### High-level specification

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- verified by model checking techniques (eg. Kind2)

### Logical meaning

- synchronous observers
- $\square (\mathcal{H} (Pre(S, x)) \wedge tr(S, x, y, S') \rightarrow Post(S, x, y, S'))$

### Code-level specification

- encoding as specific transition predicates and contracts in ACSL
- **focus:** k-induction

## EXAMPLE

```
node greycounter (x:bool) returns (out:bool);
var a,b:bool;
let
  a = false -> not pre(b);
  b = false -> pre(a);
  out = a and b;
tel

node intloopcounter (x:bool) returns (out:bool);
var time: int;
let
  time = 0 -> if pre(time) = 3 then 0
              else pre time + 1;
  out = (time = 2);
tel

node top (x:bool) returns (OK:bool);
--@ guarantee OK;
var b,d:bool;
let
  b = greycounter(x);
  d = intloopcounter(x);
  OK = b = d;
--%PROPERTY OK;
tel
```

<i>a</i>	<i>F</i>	<i>T</i>	<i>T</i>	<i>F</i>	<i>F</i>	...
<i>b</i>	<i>F</i>	<i>F</i>	<i>T</i>	<i>T</i>	<i>F</i>	...
<i>out</i>	<i>F</i>	<i>F</i>	<i>T</i>	<i>F</i>	<i>F</i>	...
<hr/>						
<i>time</i>	0	1	2	3	0	...
<i>out</i>	<i>F</i>	<i>F</i>	<i>T</i>	<i>F</i>	<i>F</i>	...
<hr/>						
<i>OK</i>	<i>T</i>	<i>T</i>	<i>T</i>	<i>T</i>	<i>T</i>	...

## EXAMPLE: MODEL-CHECKING

```
node greycounter (x:bool) returns (out:bool);
var a,b:bool;
let
  a = false -> not pre(b);
  b = false -> pre(a);
  out = a and b;
tel

node intloopcounter (x:bool) returns (out:bool);
var time: int;
let
  time = 0 -> if pre(time) = 3 then 0
              else pre time + 1;
  out = (time = 2);
tel

node top (x:bool) returns (OK:bool);
--@ guarantee OK;
var b,d:bool;
let
  b = greycounter(x);
  d = intloopcounter(x);
  OK = b = d;
--%PROPERTY OK;
tel
```

```
> kind2 --enable BMC --enable IND two_counters.lus
kind2 v1.5.0

=====
Analyzing top
  with First top: 'top'
      subsystems
        | concrete: intloopcounter, greycounter

<Success> Property OK is valid by inductive step after 0.062s.

-----
Summary of properties:
-----
OK: valid (at 5)
=====
```

## EXAMPLE: K-INDUCTION ANNOTATION

```
node top (x:bool) returns (OK:bool);  
--@ guarantee OK by 5-induction;  
var b,d:bool;  
let  
  b = greycounter(x);  
  d = intloopcounter(x);  
  OK = b = d;  
tel
```

## EXAMPLE: ACSL GENERATION

### Contract node compiled as a transition predicate

```
/*@ predicate top_contract_tr0(_Bool x, _Bool OK) =  
    \true;  
*/  
/*@ predicate top_contract_tr1(_Bool x, _Bool OK, _Bool spec36) =  
    top_contract_tr0(x, OK)  
    && spec36 == OK;  
*/  
/*@ predicate top_contract_tr(_Bool x, _Bool OK, _Bool spec36) =  
    top_contract_tr1(x, OK, spec36);  
*/
```

## EXAMPLE: ACSL GENERATION

### Requirements as contracts

```
//@ ghost _Bool spec36;
/*@ ...
    requires top_pack(*mem, self);
    ensures top_pack(*mem, self);
    ensures top_tr(\old(*mem), x, *OK, *mem);
    ensures top_contract_tr(x, *OK, spec36) ==>
        spec36;
    ...
*/
void top_step(_Bool x, _Bool *OK, struct top_mem *self)
/*@ ghost (struct top_mem_ghost \ghost *mem) */ {
```

## EXAMPLE: ACSL GENERATION

### k-induction base cases predicates

```
predicate top_full_init(struct top_mem_ghost mem) =  
    top_init(mem) && mem._reset;
```

```
predicate top_base_1(struct top_mem_ghost mem_0,  
                    _Bool x_1, _Bool OK_1,  
                    struct top_mem_ghost mem_1) =  
\forall _Bool spec36_1;  
    top_full_init(mem_0)  
    && top_tr(mem_0, x_1, OK_1, mem_1)  
    && top_contract_tr(x_1, OK_1, spec36_1) ==>  
    spec36_1;
```



## EXAMPLE: ACSL GENERATION

### k-induction base cases predicates

```
predicate top_base_2(struct top_mem_ghost mem_1,
                    _Bool x_2, _Bool OK_2,
                    struct top_mem_ghost mem_2) =
\forall _Bool spec36_2;
  \forall struct top_mem_ghost mem_0, _Bool x_1, _Bool OK_1;
    top_full_init(mem_0)
    && top_tr(mem_0, x_1, OK_1, mem_1)
    && top_contract_tr(x_1, OK_1, (_Bool) 1)
    && top_tr(mem_1, x_2, OK_2, mem_2)
    && top_contract_tr(x_2, OK_2, spec36_2) ==>
    spec36_2;
```

## EXAMPLE: ACSL GENERATION

### k-induction base cases predicates

```
predicate top_base_3(struct top_mem_ghost mem_2,
                    _Bool x_3, _Bool OK_3,
                    struct top_mem_ghost mem_3) =
\forall _Bool spec36_3;
  \forall struct top_mem_ghost mem_0, mem_1,
    _Bool x_1, _Bool OK_1, _Bool x_2, _Bool OK_2;
    top_full_init(mem_0)
    && top_tr(mem_0, x_1, OK_1, mem_1)
    && top_contract_tr(x_1, OK_1, (_Bool) 1)
    && top_tr(mem_1, x_2, OK_2, mem_2)
    && top_contract_tr(x_2, OK_2, (_Bool) 1)
    && top_tr(mem_2, x_3, OK_3, mem_3)
    && top_contract_tr(x_3, OK_3, spec36_3) ==>
    spec36_3;
```

## EXAMPLE: ACSL GENERATION

### k-induction base cases predicates

```
predicate top_base_4(struct top_mem_ghost mem_3,
                    _Bool x_4, _Bool OK_4,
                    struct top_mem_ghost mem_4) =
\forall _Bool spec36_4;
  \forall struct top_mem_ghost mem_0, mem_1, mem_2,
    _Bool x_1, _Bool OK_1, _Bool x_2, _Bool OK_2, _Bool x_3,
    _Bool OK_3;
    top_full_init(mem_0)
    && top_tr(mem_0, x_1, OK_1, mem_1)
    && top_contract_tr(x_1, OK_1, (_Bool) 1)
    && top_tr(mem_1, x_2, OK_2, mem_2)
    && top_contract_tr(x_2, OK_2, (_Bool) 1)
    && top_tr(mem_2, x_3, OK_3, mem_3)
    && top_contract_tr(x_3, OK_3, (_Bool) 1)
    && top_tr(mem_3, x_4, OK_4, mem_4)
    && top_contract_tr(x_4, OK_4, spec36_4) ==>
    spec36_4;
```

## EXAMPLE: ACSL GENERATION

### k-induction inductive case predicate

```
predicate top_inductive_5(struct top_mem_ghost mem_4,  
                          _Bool x_5, _Bool OK_5,  
                          struct top_mem_ghost mem_5) =  
\forall _Bool spec36_5;  
  \forall struct top_mem_ghost mem_0, mem_1, mem_2, mem_3,  
    _Bool x_1, _Bool OK_1, _Bool x_2, _Bool OK_2, _Bool x_3,  
    _Bool OK_3, _Bool x_4, _Bool OK_4;  
    top_tr(mem_0, x_1, OK_1, mem_1)  
    && top_contract_tr(x_1, OK_1, (_Bool) 1)  
    && top_tr(mem_1, x_2, OK_2, mem_2)  
    && top_contract_tr(x_2, OK_2, (_Bool) 1)  
    && top_tr(mem_2, x_3, OK_3, mem_3)  
    && top_contract_tr(x_3, OK_3, (_Bool) 1)  
    && top_tr(mem_3, x_4, OK_4, mem_4)  
    && top_contract_tr(x_4, OK_4, (_Bool) 1)  
    && top_tr(mem_4, x_5, OK_5, mem_5)  
    && top_contract_tr(x_5, OK_5, spec36_5) ==>  
    spec36_5;
```

## EXAMPLE: ACSL GENERATION

### k-induction corresponding lemmas

```
lemma top_k_induction_1:
  \forall struct top_mem_ghost mem_in, mem_out, _Bool x, _Bool OK;
  top_base_1(mem_in, x, OK, mem_out);

lemma top_k_induction_2:
  \forall struct top_mem_ghost mem_in, mem_out, _Bool x, _Bool OK;
  top_base_2(mem_in, x, OK, mem_out);

lemma top_k_induction_3:
  \forall struct top_mem_ghost mem_in, mem_out, _Bool x, _Bool OK;
  top_base_3(mem_in, x, OK, mem_out);

lemma top_k_induction_4:
  \forall struct top_mem_ghost mem_in, mem_out, _Bool x, _Bool OK;
  top_base_4(mem_in, x, OK, mem_out);

lemma top_k_induction_5:
  \forall struct top_mem_ghost mem_in, mem_out, _Bool x, _Bool OK;
  top_inductive_5(mem_in, x, OK, mem_out);
```

## EXAMPLE: ACSL GENERATION

### k-induction principle as an axiom

```
axiomatic top_k_Induction {
  axiom top_k_induction:
    \forall struct top_mem_ghost mem_in, mem_out, _Bool x, _Bool OK;
      top_base_1(mem_in, x, OK, mem_out)
      && top_base_2(mem_in, x, OK, mem_out)
      && top_base_3(mem_in, x, OK, mem_out)
      && top_base_4(mem_in, x, OK, mem_out)
      && top_inductive_5(mem_in, x, OK, mem_out) ==>
    \forall _Bool spec36;
      top_tr(mem_in, x, OK, mem_out)
      && top_contract_tr(x, OK, spec36) ==>
      spec36;
}
```

## STATEFUL CONTRACT EXAMPLE

```
node fibo(x: bool) returns(a: int);
--@ guarantee a = (0 -> pre a) + (0 -> pre (1 -> pre a));
var b: int;
let
  a = 0 -> pre b;
  b = 1 -> pre (a + b);
  --%PROPERTY a = (0 -> pre a) + (0 -> pre (1 -> pre a));
tel
```

## STATEFUL CONTRACT EXAMPLE

```
node fibo(x: bool) returns(a: int);
--@ guarantee a = (0 -> pre a) + (0 -> pre (1 -> pre a));
var b: int;
let
  a = 0 -> pre b;
  b = 1 -> pre (a + b);
  --%PROPERTY a = (0 -> pre a) + (0 -> pre (1 -> pre a));
tel
```

```
> kind2 --enable BMC --enable IND fibo.lus
kind2 v1.5.0

=====
Analyzing fibo
  with First top: 'fibo' (no subsystems)

<Success> Property (a = ((0 -> (pre a)) + (0 -> (pre (1 -> (pre a)))))) is valid by inductive step after 0.05

-----
Summary of properties:
-----
(a = ((0 -> (pre a)) + (0 -> (pre (1 -> (pre a)))))): valid (at 3)
=====
```



## STATEFUL CONTRACT EXAMPLE

```
node fibo(x: bool) returns(a: int);  
--@ guarantee a = (0 -> pre a) + (0 -> pre (1 -> pre a)) by 3-induction;  
var b: int;  
let  
  a = 0 -> pre b;  
  b = 1 -> pre (a + b);  
tel
```

## STATEFUL CONTRACT EXAMPLE

### Much more complex contract transition predicate

```
/*@ predicate fibo_contract_tr0(struct fibo_contract_mem_ghost mem_in,
                               _Bool x, integer a,
                               struct fibo_contract_mem_ghost mem_out) =
    mem_out._reset == mem_in._reset;
*/
/*@ predicate fibo_contract_tr1(struct fibo_contract_mem_ghost mem_in,
                               _Bool x, integer a,
                               _Bool __fibo_contract_7,
                               struct fibo_contract_mem_ghost mem_out) =
    fibo_contract_tr0(mem_in, x, a, mem_out)
    && _arrow_transition(mem_in.ni_4, __fibo_contract_7, mem_out.ni_4);
*/
/*@ predicate fibo_contract_tr2(struct fibo_contract_mem_ghost mem_in,
                               _Bool x, integer a,
                               integer __fibo_contract_9,
                               struct fibo_contract_mem_ghost mem_out) =
    \exists _Bool __fibo_contract_7;
    fibo_contract_tr1(mem_in, x, a, __fibo_contract_7, mem_out)
    && (__fibo_contract_7 ? __fibo_contract_9 == 0
        : (!_arrow_initialization(mem_in.ni_4) ==>
           __fibo_contract_9 == mem_in.reg.__fibo_contract_8
        ));
*/
```

## STATEFUL CONTRACT EXAMPLE

### Much more complex contract transition predicate

```
/*@ predicate fibo_contract_tr3(struct fibo_contract_mem_ghost mem_in,
    _Bool x, integer a,
    integer __fibo_contract_9,
    _Bool __fibo_contract_1,
    struct fibo_contract_mem_ghost mem_out) =
    fibo_contract_tr2(mem_in, x, a, __fibo_contract_9, mem_out)
    && _arrow_transition(mem_in.ni_5, __fibo_contract_1, mem_out.ni_5);
*/
/*@ predicate fibo_contract_tr4(struct fibo_contract_mem_ghost mem_in,
    _Bool x, integer a,
    integer __fibo_contract_9,
    integer __fibo_contract_6,
    struct fibo_contract_mem_ghost mem_out) =
    \exists _Bool __fibo_contract_1;
    fibo_contract_tr3(mem_in,
        x, a, __fibo_contract_9, __fibo_contract_1,
        mem_out)
    && (__fibo_contract_1 ? __fibo_contract_6 == 0
        : (!_arrow_initialization(mem_in.ni_4) ==>
            __fibo_contract_6 == mem_in.reg.__fibo_contract_5
        ));
*/
```

## STATEFUL CONTRACT EXAMPLE

### Much more complex contract transition predicate

```
/*@ predicate fibo_contract_tr5(struct fibo_contract_mem_ghost mem_in,
                               _Bool x, integer a, _Bool spec19,
                               struct fibo_contract_mem_ghost mem_out) =
  \exists integer __fibo_contract_9, integer __fibo_contract_6;
  fibo_contract_tr4(mem_in,
                   x, a, __fibo_contract_9, __fibo_contract_6,
                   mem_out)
  && spec19 == (a == (__fibo_contract_9 + __fibo_contract_6));
*/
/*@ predicate fibo_contract_tr6(struct fibo_contract_mem_ghost mem_in,
                               _Bool x, integer a, _Bool spec19,
                               struct fibo_contract_mem_ghost mem_out) =
  fibo_contract_tr5(mem_in, x, a, spec19, mem_out)
  && mem_out._reg.__fibo_contract_8 == a;
*/
/*@ predicate fibo_contract_tr7(struct fibo_contract_mem_ghost mem_in,
                               _Bool x, integer a,
                               _Bool __fibo_contract_2, _Bool spec19,
                               struct fibo_contract_mem_ghost mem_out) =
  fibo_contract_tr6(mem_in, x, a, spec19, mem_out)
  && _arrow_transition(mem_in.ni_6, __fibo_contract_2, mem_out.ni_6);
*/
```

## STATEFUL CONTRACT EXAMPLE

### Much more complex contract transition predicate

```
/*@ predicate fibo_contract_tr8(struct fibo_contract_mem_ghost mem_in,
    _Bool x, integer a,
    integer __fibo_contract_4,
    _Bool spec19,
    struct fibo_contract_mem_ghost mem_out) =
  \exists _Bool __fibo_contract_2;
  fibo_contract_tr7(mem_in, x, a, __fibo_contract_2, spec19,
    mem_out)
  && (__fibo_contract_2 ? __fibo_contract_4 == 1
    : (!_arrow_initialization(mem_in.ni_4) ==>
      __fibo_contract_4 == mem_in._reg.__fibo_contract_3
    ));
*/
/*@ predicate fibo_contract_tr9(struct fibo_contract_mem_ghost mem_in,
    _Bool x, integer a, _Bool spec19,
    struct fibo_contract_mem_ghost mem_out) =
  \exists integer __fibo_contract_4;
  fibo_contract_tr8(mem_in, x, a, __fibo_contract_4, spec19,
    mem_out)
  && mem_out._reg.__fibo_contract_5 == __fibo_contract_4;
*/
```

## STATEFUL CONTRACT EXAMPLE

### Much more complex contract transition predicate

```
/*@ predicate fibo_contract_tr10(struct fibo_contract_mem_ghost mem_in,
                                _Bool x, integer a, _Bool spec19,
                                struct fibo_contract_mem_ghost mem_out) =
    fibo_contract_tr9(mem_in, x, a, spec19, mem_out)
    && mem_out._reg.__fibo_contract_3 == a;
*/
/*@ predicate fibo_contract_tr(struct fibo_contract_mem_ghost mem_in,
                                _Bool x, integer a, _Bool spec19,
                                struct fibo_contract_mem_ghost mem_out) =
    \exists struct fibo_contract_mem_ghost mem_reset;
    fibo_contract_reset_cleared(mem_in, mem_reset)
    && fibo_contract_tr10(mem_reset, x, a, spec19, mem_out);
*/
```

## STATEFUL CONTRACT EXAMPLE

### Same k-induction principles, with state

```
/*@ ghost
    _Bool spec19;
    struct fibo_contract_mem_ghost mem_in_c, mem_out_c;
*/
/*@ ...
    requires fibo_pack(*mem, self);
    ensures fibo_pack(*mem, self);
    ensures fibo_transition(\old(*mem), x, *a, *mem);
    ensures fibo_contract_tr(mem_in_c, x, *a, spec19, mem_out_c) ==>
        spec19;
    ...
*/
void fibo_step(_Bool x, int *a, struct fibo_mem *self)
/*@ ghost (struct fibo_mem_ghost \ghost *mem) */ {
```

## CONCLUSION

### Summary

- A certifying compiler from Lustre to C / ACSL
- Certificate of correctness wrt a state / transition semantics
- Automatic translation of high-level contracts

### Future

- Prototype
- Other alternative for compiling the *reset*
- Optimizations
- Invariant generation
- Encoding a synchronous dataflow semantics?
- SPARK / Ada



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