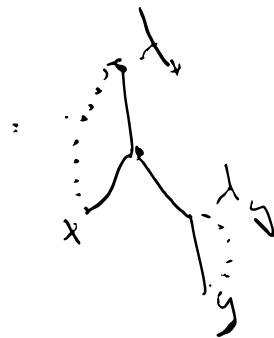


$$L = aL \mid bL \mid \epsilon \Leftrightarrow L = (a+b)L + \epsilon$$

$$B = \square + \begin{array}{c} \circ \\ \swarrow \searrow \\ B \quad B \end{array} \Leftrightarrow \text{binary tree}$$

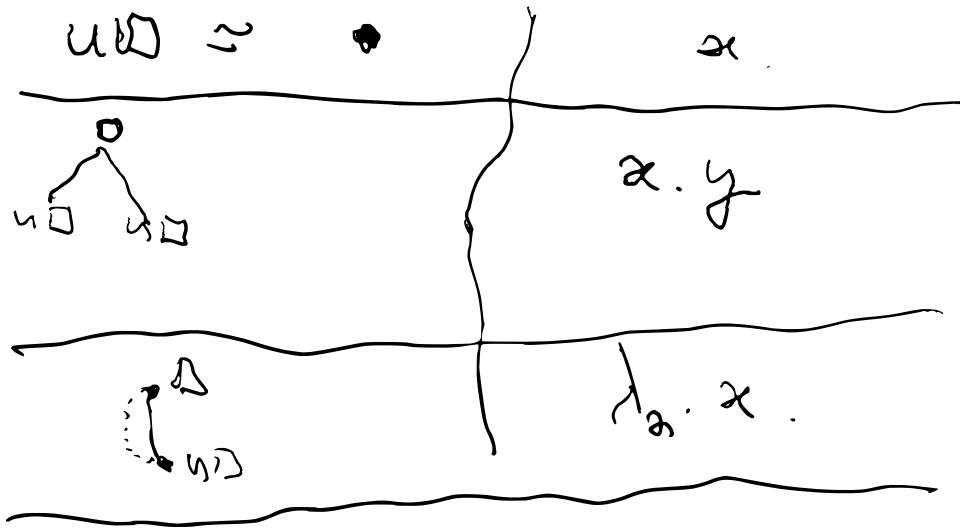
linear lambda terms:

$$L = \begin{array}{c} \text{free} \\ \downarrow \\ \text{graph} \end{array} + \begin{array}{c} \circ \\ \swarrow \searrow \\ \text{graph} \end{array}$$



$$\Leftrightarrow \lambda x. (y y)$$

linear term L



$$\{ = uB + oL^2 + \Delta \partial_u L \Leftrightarrow \text{describes linear lambda terms}$$

$$\partial_u \left(\begin{array}{c} \diagup \\ \square \\ \diagdown \end{array} \right) = \left\{ \begin{array}{c} \diagup \\ \square \otimes \\ \diagdown \end{array} \right\} \cup \left\{ \begin{array}{c} \diagup \\ \square \\ \diagdown \otimes \end{array} \right\}$$

$$\left\{ \begin{array}{l} \omega = 0 \\ L(z, u) = uz + z \cdot L_n^z(z, u) + z \partial_u L_n(z, u) \end{array} \right.$$

$$L(z, u) = \sum a_{n,k} \cdot u^k \cdot z^n$$

↖ # linear lambda terms of size n
 a = 0 with k free leaves.

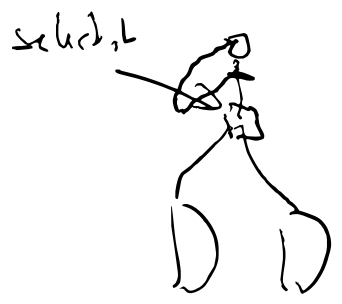
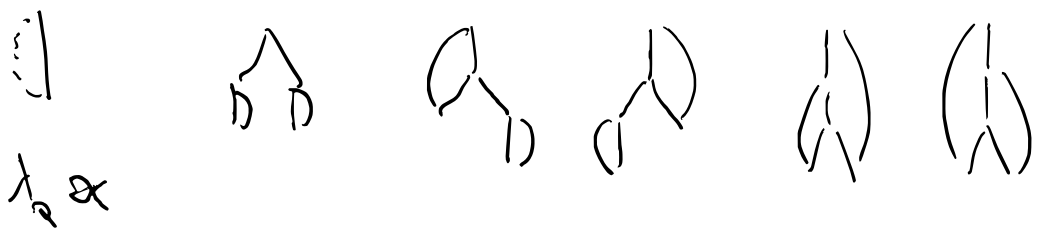
$$L(z, u) = \underset{\substack{\uparrow \\ z}}{uz} + \overset{\substack{\uparrow \\ z}}{\cancel{z^2}} + \dots$$

↘ ↗
 $\left(\begin{array}{c} \uparrow \\ z \\ \downarrow \\ \infty \end{array} \right)$

$L(z, 0)$ = generating function for closed linear lambda terms.

$L(z, 0)$ follows also an algebraically differential equation.

$$L(3,0) = z^2 + \cancel{z^3} + 60 z^4 + \dots$$



$$L(3,0) = z^2 + zL^2 + 2z \cdot z^2.$$



$$L = z^2 + zL^2 + 2z^3 L$$

$$L_3 = \mathbb{Z}^2 + \mathbb{Z} L_2 + 2\mathbb{Z}^4 \partial_3 L_3$$



??
!

