

**TIFA**

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## 1 TIFA

### 1.1 About the TIFA library

**TIFA** is an acronym standing for "Tools for Integer FActorisation". As its (utterly unoriginal) name implies **TIFA** is a open source library for composite integer factorization. Its goal is to provide portable and reasonably fast implementations for several algorithms, with a particular emphasis on the factorization of small to medium-sized composites, say from 40 bits to about 200 bits.

Although it obviously won't break any record by itself, **TIFA** may be a good companion to more ambitious factorization attempts such as a distributed implementation of the Number Field Sieve, where it could be used to factor the numerous smaller-sized by-products.

### 1.2 License

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### 1.3 Content of the TIFA package

Actually, **TIFA** is a little bit more than a library *per se*. The **TIFA** package supplies:

- a **C99** library providing implementations for the following factorization algorithms:
  - CFRAC (Continued FRAction factorization)
  - ECM (Elliptic Curve Method)
  - Fermat (McKee's "fast" variant of Fermat's algorithm)

- SIQS (Self-Initializing Quadratic Sieve)
  - SQUFOF (SQUare FOrm Factorization)
- a set of stand-alone factorization programs for each algorithm implemented:
  - `cfrac_program`
  - `ecm_program`
  - `fermat_program`
  - `siqs_program`
  - `squfof_program`
- a set of **Perl 5** scripts wrappers and launchers;
- a basic benchmarking framework written in **Perl 5** used to assess the performance of **TIFA**'s implementations.

## 1.4 Documentation

A complete user's guide is in preparation.

In the interim, the best source of documentation (apart from this Doxygen documentation generated during the build process) is the included (infamous) `readme.txt` file in the `readme` directory.

Also worth a look is the (unfortunately not empty) `issues.txt` file.

## 2 Data Structure Index

### 2.1 Data Structures

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## 3 File Index

### 3.1 File List

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## 4 Data Structure Documentation

### 4.1 struct\_approximer\_t Struct Reference

Structure used to find number approximation.

```
#include <lib/utils/include/approx.h>
```

#### Data Fields

- [mpz\\_t target](#)
- [float targetlog](#)
- [float dlog\\_tolerance](#)
- [uint32\\_array\\_t \\* facpool](#)
- [uint32\\_t nfactores](#)
- [int32\\_t imin](#)
- [int32\\_t imax](#)
- [uint32\\_t keven](#)
- [uint32\\_t neven](#)
- [uint32\\_t kodd](#)
- [uint32\\_t nodd](#)
- [uint32\\_t nsubsets\\_odd](#)
- [uint32\\_t \\* subset\\_odd](#)
- [uint32\\_t rank](#)
- [uint32\\_tuple\\_t \\* tuples](#)
- [uint32\\_t ntuples](#)

#### 4.1.1 Detailed Description

Structure used to find number approximation.

The structure `approximer_t` (and its associated functions) is used to approximate a target value by multiplying a given number of factors from a given base. Each factor is allowed to appear only once in the decomposition of the approximation on the given base.

Definition at line 116 of file `approx.h`.

## 4.1.2 Field Documentation

### 4.1.2.1 `mpz_t struct_approximer_t::target`

The target number to approximate.

Definition at line 120 of file `approx.h`.

### 4.1.2.2 `float struct_approximer_t::targetlog`

Logarithm in base 10 of the target number.

Definition at line 124 of file `approx.h`.

### 4.1.2.3 `float struct_approximer_t::dlog_tolerance`

The logarithm in base 10 of the approximation should be within `dlog_tolerance` of `targetlog`.

Definition at line 129 of file `approx.h`.

### 4.1.2.4 `uint32_array_t* struct_approximer_t::facpool`

Pool of potential factors.

Definition at line 133 of file `approx.h`.

### 4.1.2.5 `uint32_t struct_approximer_t::nfactors`

Numbers of factors from `facpool` in the approximation.

Definition at line 137 of file `approx.h`.

### 4.1.2.6 `int32_t struct_approximer_t::imin`

`facpool[imin]` is the smallest factor allowed.

Definition at line 141 of file `approx.h`.

### 4.1.2.7 `int32_t struct_approximer_t::imax`

`facpool[imax]` is the largest factor allowed.

Definition at line 145 of file `approx.h`.

### 4.1.2.8 `uint32_t struct_approximer_t::keven`

Number of factors to choose with even indexes.

Definition at line 149 of file `approx.h`.

### 4.1.2.9 `uint32_t struct_approximer_t::neven`

Number of available factors with even indexes.

Definition at line 153 of file `approx.h`.

**4.1.2.10 uint32\_t struct\_approximer\_t::kodd**

Number of factors to choose with odd indexes.

Definition at line 157 of file approx.h.

**4.1.2.11 uint32\_t struct\_approximer\_t::nodd**

Number of available factors with odd indexes.

Definition at line 161 of file approx.h.

**4.1.2.12 uint32\_t struct\_approximer\_t::nsubsets\_odd**

Number of distinct combination of `kodd` factors from the pool of odd indexed factors (in other words  $C(nodd, kodd)$ ).

Definition at line 167 of file approx.h.

**4.1.2.13 uint32\_t\* struct\_approximer\_t::subset\_odd**

A subset of `kodd` odd-indexes.

Definition at line 171 of file approx.h.

**4.1.2.14 uint32\_t struct\_approximer\_t::rank**

The rank of the subset of `kodd` odd-indexes in lexicographic order.

Definition at line 176 of file approx.h.

**4.1.2.15 uint32\_tuple\_t\* struct\_approximer\_t::tuples**

List of tuples obtained by precomputing all combinations of `keven` factors.

Definition at line 181 of file approx.h.

**4.1.2.16 uint32\_t struct\_approximer\_t::ntuples**

Number of all possible combinations of `keven` factors.

Definition at line 185 of file approx.h.

The documentation for this struct was generated from the following file:

- [approx.h](#)

**4.2 struct\_binary\_array\_t Struct Reference**

Defines an array of bits.

```
#include <lib/utills/include/array.h>
```

**Data Fields**

- [uint32\\_t allocated](#)



- [uint32\\_t length](#)
- TIFA\_BITSTRING\_T \* [data](#)

#### 4.2.1 Detailed Description

Defines an array of bits.

This structure defines an array of bits which knows its current length and its allocated memory space.

##### Note:

Internally, bits are packed in a TIFA\_BITSTRING\_T array.

Definition at line 1127 of file array.h.

#### 4.2.2 Field Documentation

##### 4.2.2.1 uint32\_t struct\_binary\_array\_t::allocated

Memory space allocated for this array's data field, given as a multiple of `sizeof(TIFA_BITSTRING_T)`. This is the maximum number of TIFA\_BITSTRING\_T that the array can accommodate. The number of bits that the array can hold is hence `CHAR_BIT * sizeof(TIFA_BITSTRING_T)` times this value (`CHAR_BIT` being the number of bits used to represent a `char`, usually 8 on most current architectures).

Definition at line 1137 of file array.h.

##### 4.2.2.2 uint32\_t struct\_binary\_array\_t::length

Current number of bits hold in the array pointed by the structure's `data` field.

Definition at line 1142 of file array.h.

##### 4.2.2.3 TIFA\_BITSTRING\_T\* struct\_binary\_array\_t::data

Array of TIFA\_BITSTRING\_T whose size is given by the `allocated` field.

Definition at line 1147 of file array.h.

Referenced by `flip_array_bit()`, `get_array_bit()`, `set_array_bit_to_one()`, and `set_array_bit_to_zero()`.

The documentation for this struct was generated from the following file:

- [array.h](#)

### 4.3 struct\_binary\_matrix\_t Struct Reference

Defines a matrix of bits.

```
#include <lib/utils/include/matrix.h>
```

#### Data Fields

- [uint32\\_t nrows\\_allocated](#)
- [uint32\\_t ncols\\_allocated](#)

- uint32\_t nrows
- uint32\_t ncols
- TIFA\_BITSTRING\_T \*\* data

### 4.3.1 Detailed Description

Defines a matrix of bits.

This structure defines a matrix of bits which knows its current dimensions and its allocated memory space.

#### Note:

Internally, a matrix of bits is represented as a matrix of TIFA\_BITSTRING\_T elements.

Definition at line 71 of file matrix.h.

### 4.3.2 Field Documentation

#### 4.3.2.1 uint32\_t struct\_binary\_matrix\_t::nrows\_allocated

Maximum number of rows of the matrix.

Definition at line 75 of file matrix.h.

#### 4.3.2.2 uint32\_t struct\_binary\_matrix\_t::ncols\_allocated

Maximum number of columns of the matrix. Since bits are packed in TIFA\_BITSTRING\_T elements, the maximum number of bits per column is  $8 * \text{sizeof}(TIFA\_BITSTRING\_T) * \text{nrows\_allocated}$ .

Hence the total allocated memory for the data field is  $\text{nrows\_allocated} * \text{ncols\_allocated} * \text{sizeof}(TIFA\_BITSTRING\_T)$  bytes.

Definition at line 86 of file matrix.h.

#### 4.3.2.3 uint32\_t struct\_binary\_matrix\_t::nrows

Current number of rows of the matrix.

Definition at line 90 of file matrix.h.

Referenced by first\_row\_with\_one\_on\_col().

#### 4.3.2.4 uint32\_t struct\_binary\_matrix\_t::ncols

Current number of columns of the matrix.

Definition at line 94 of file matrix.h.

#### 4.3.2.5 TIFA\_BITSTRING\_T\*\* struct\_binary\_matrix\_t::data

2D array of TIFA\_BITSTRING\_T elements whose dimensions are given by the nrows\_allocated and ncols\_allocated fields.

Definition at line 99 of file matrix.h.

Referenced by first\_row\_with\_one\_on\_col(), flip\_matrix\_bit(), get\_matrix\_bit(), set\_matrix\_bit\_to\_one(), and set\_matrix\_bit\_to\_zero().

The documentation for this struct was generated from the following file:

- [matrix.h](#)

## 4.4 `struct_byte_array_t` Struct Reference

Defines an array of bytes.

```
#include <lib/utils/include/array.h>
```

### Data Fields

- `uint32_t` [allocated](#)
- `uint32_t` [length](#)
- `unsigned char *` [data](#)

### 4.4.1 Detailed Description

Defines an array of bytes.

This structure defines a special kind of byte array (actually `unsigned char` array) which knows its current length and its allocated memory space.

Definition at line 100 of file `array.h`.

### 4.4.2 Field Documentation

#### 4.4.2.1 `uint32_t struct_byte_array_t::allocated`

Memory space allocated for this array's `data` field, given as a multiple of `sizeof(unsigned char)`. This is the maximum number of bytes that the array can accommodate.

Definition at line 106 of file `array.h`.

#### 4.4.2.2 `uint32_t struct_byte_array_t::length`

Current number of bytes hold in the array pointed by the structure's `data` field.

Definition at line 111 of file `array.h`.

Referenced by `is_in_sorted_byte_array()`.

#### 4.4.2.3 `unsigned char* struct_byte_array_t::data`

Array of `unsigned char` whose size is given by the `allocated` field.

Definition at line 116 of file `array.h`.

The documentation for this struct was generated from the following file:

- [array.h](#)

## 4.5 struct\_byte\_matrix\_t Struct Reference

Defines a matrix of bytes.

```
#include <lib/utls/include/matrix.h>
```

### Data Fields

- [uint32\\_t nrows\\_allocated](#)
- [uint32\\_t ncols\\_allocated](#)
- [uint32\\_t nrows](#)
- [uint32\\_t ncols](#)
- [unsigned char \\*\\* data](#)

### 4.5.1 Detailed Description

Defines a matrix of bytes.

This structure defines a matrix of bytes which knows its current dimensions and its allocated memory space.

#### Note:

Internally, a matrix of bytes is represented as a matrix of `unsigned char` elements.

Definition at line 351 of file `matrix.h`.

### 4.5.2 Field Documentation

#### 4.5.2.1 `uint32_t struct_byte_matrix_t::nrows_allocated`

Maximum number of rows of the matrix.

Definition at line 355 of file `matrix.h`.

#### 4.5.2.2 `uint32_t struct_byte_matrix_t::ncols_allocated`

Maximum number of columns of the matrix.

Definition at line 359 of file `matrix.h`.

#### 4.5.2.3 `uint32_t struct_byte_matrix_t::nrows`

Current number of rows of the matrix.

Definition at line 363 of file `matrix.h`.

#### 4.5.2.4 `uint32_t struct_byte_matrix_t::ncols`

Current number of columns of the matrix.

Definition at line 367 of file `matrix.h`.

#### 4.5.2.5 unsigned char\*\* struct\_byte\_matrix\_t::data

2D array of unsigned char elements whose dimensions are given by the `nrows_allocated` and `ncols_allocated` fields.

Definition at line 372 of file `matrix.h`.

The documentation for this struct was generated from the following file:

- [matrix.h](#)

## 4.6 struct\_cfrac\_params\_t Struct Reference

Defines the variable parameters used in the CFRAC algorithm.

```
#include <lib/algo/include/cfrac.h>
```

### Data Fields

- [uint32\\_t nprimes\\_in\\_base](#)
- [uint32\\_t nprimes\\_tdiv](#)
- [uint32\\_t nrelations](#)
- [linalg\\_method\\_t linalg\\_method](#)
- [bool use\\_large\\_primes](#)
- [smooth\\_filter\\_method\\_t filter\\_method](#)
- [unsigned short int nsteps\\_early\\_abort](#)

### 4.6.1 Detailed Description

Defines the variable parameters used in the CFRAC algorithm.

This structure defines the set of the variable parameters used in the CFRAC algorithm.

Definition at line 93 of file `cfrac.h`.

### 4.6.2 Field Documentation

#### 4.6.2.1 uint32\_t struct\_cfrac\_params\_t::nprimes\_in\_base

Number of prime numbers composing the factor base on which to factor the residues.

Definition at line 98 of file `cfrac.h`.

#### 4.6.2.2 uint32\_t struct\_cfrac\_params\_t::nprimes\_tdiv

Number of the first primes to use in the trial division of the residues known to be smooth.

#### Warning:

`nprimes_tdiv` should be greater than or equal to 1.

Definition at line 105 of file `cfrac.h`.

#### 4.6.2.3 `uint32_t struct_cfrac_params_t::nrelations`

Number of linear dependences to find.

Definition at line 109 of file `cfrac.h`.

#### 4.6.2.4 `linalg_method_t struct_cfrac_params_t::linalg_method`

Linear system resolution method to use.

Definition at line 113 of file `cfrac.h`.

#### 4.6.2.5 `bool struct_cfrac_params_t::use_large_primes`

True if we use the single large prime variation. False otherwise.

Definition at line 118 of file `cfrac.h`.

#### 4.6.2.6 `smooth_filter_method_t struct_cfrac_params_t::filter_method`

Method to use to detect smooth residues and relations.

Definition at line 122 of file `cfrac.h`.

#### 4.6.2.7 `unsigned short int struct_cfrac_params_t::nsteps_early_abort`

Number of steps in the early abort strategy. If zero, no early abort is performed. Only used is `linalg_method` is set to `TDIV` or `TDIV_EARLY_ABORT`.

#### Note:

`nsteps` should be less than or equal to `MAX_NSTEPS`, as defined in [smooth\\_filter.h](#).

Definition at line 131 of file `cfrac.h`.

The documentation for this struct was generated from the following file:

- [cfrac.h](#)

## 4.7 `struct_cont_frac_state_t` Struct Reference

An ad-hoc structure for the computation of the continued fraction of a square root.

```
#include <sqrt_cont_frac.h>
```

#### Data Fields

- `mpz_t a`
- `mpz_t p`
- `mpz_t q`
- `mpz_t t`
- `mpz_t sqrtn`
- `mpz_t n`
- `uint32_t nsteps_performed`

### 4.7.1 Detailed Description

An ad-hoc structure for the computation of the continued fraction of a square root.

[lib/utls/include/sqrt\\_cont\\_frac.h](#) This ad-hoc structure defines the variables needed for the computation of the expansion of the continued fraction of the square root of a non perfect square.

#### Note:

Since the denominators of the fraction are not needed in the CFRAC algorithm, they are not computed in this particular implementation.

Definition at line 69 of file `sqrt_cont_frac.h`.

### 4.7.2 Field Documentation

#### 4.7.2.1 `mpz_t struct_cont_frac_state_t::a`

Current numerator of the continued fraction approximating `sqrt(n)`, given modulo `n`.

Definition at line 78 of file `sqrt_cont_frac.h`.

#### 4.7.2.2 `mpz_t struct_cont_frac_state_t::p`

(Used in the computation of `a`).

Definition at line 87 of file `sqrt_cont_frac.h`.

#### 4.7.2.3 `mpz_t struct_cont_frac_state_t::q`

One has:  $(-1)^{(\text{nsteps\_performed})} q = a*a - b*b*n$

Definition at line 91 of file `sqrt_cont_frac.h`.

#### 4.7.2.4 `mpz_t struct_cont_frac_state_t::t`

The current term of the expansion of the continued fraction.

Definition at line 95 of file `sqrt_cont_frac.h`.

#### 4.7.2.5 `mpz_t struct_cont_frac_state_t::sqrtn`

The (truncated) square root of which to compute the continued fraction.

Definition at line 100 of file `sqrt_cont_frac.h`.

#### 4.7.2.6 `mpz_t struct_cont_frac_state_t::n`

The non perfect square integer whose square root will be approximated by the computation of a continued fraction.

Definition at line 105 of file `sqrt_cont_frac.h`.

#### 4.7.2.7 `uint32_t struct_cont_frac_state_t::nsteps_performed`

The number of non trivial terms of the continued fraction already computed.

Definition at line 110 of file `sqrt_cont_frac.h`.

The documentation for this struct was generated from the following file:

- [sqrt\\_cont\\_frac.h](#)

## 4.8 `struct_ecm_params_t` Struct Reference

Defines the variable parameters used in ECM.

```
#include <lib/algo/include/ecm.h>
```

### Data Fields

- `uint32_t b1`
- `uint32_t b2`
- `uint32_t ncurves`

### 4.8.1 Detailed Description

Defines the variable parameters used in ECM.

This structure defines the set of the variable parameters used in the elliptic curve method (ECM).

Definition at line 67 of file `ecm.h`.

### 4.8.2 Field Documentation

#### 4.8.2.1 `uint32_t struct_ecm_params_t::b1`

Bound used in the first phase of ECM.

Definition at line 71 of file `ecm.h`.

#### 4.8.2.2 `uint32_t struct_ecm_params_t::b2`

Bound used in the second phase of ECM. If set to 0, no second phase is performed.

#### Warning:

Due to a current limitation in the code, it is required than `b2 == 0` (no second phase) or `b2 > 105`. Failure to assess such a condition will lead to unpredictable behaviour.

Definition at line 80 of file `ecm.h`.

#### 4.8.2.3 `uint32_t struct_ecm_params_t::ncurves`

Number of curves to try before giving up the factorization when using the `SINGLE_RUN` factoring mode.

Definition at line 85 of file `ecm.h`.

The documentation for this struct was generated from the following file:

- [ecm.h](#)



## 4.9 struct\_factoring\_machine Struct Reference

Defines a structure to represent the logic behind all factorization algorithms.

```
#include <factoring_machine.h>
```

### Data Fields

- `mpz_t n`
- `factoring_mode_t mode`
- `void * context`
- `void * params`
- `ecode_t(* init_context_func)(struct struct_factoring_machine *const)`
- `ecode_t(* perform_algo_func)(struct struct_factoring_machine *const)`
- `ecode_t(* update_context_func)(struct struct_factoring_machine *const)`
- `ecode_t(* clear_context_func)(struct struct_factoring_machine *const)`
- `ecode_t(* recurse_func)(mpz_array_t *const, uint32_array_t *const, const mpz_t, factoring_mode_t)`
- `mpz_array_t * factors`
- `uint32_array_t * multis`
- `bool success`

### 4.9.1 Detailed Description

Defines a structure to represent the logic behind all factorization algorithms.

tools/include/factoring\_machine.h

This structure defines a set of data and functions to represent the logic behind all factorization algorithms. The idea is to be able to write down the factoring process' boilerplate once and for all so that actual factorization algorithm can use such a structure by merely "filling-in" the gaps.

Definition at line 118 of file factoring\_machine.h.

### 4.9.2 Field Documentation

#### 4.9.2.1 `mpz_t struct_factoring_machine::n`

The integer to factor.

Definition at line 122 of file factoring\_machine.h.

#### 4.9.2.2 `factoring_mode_t struct_factoring_machine::mode`

The factoring mode to use.

Definition at line 126 of file factoring\_machine.h.

#### 4.9.2.3 `void* struct_factoring_machine::context`

The context of the factorization algorithm. This is a pointer to an algorithm implementation dependant structure holding all variables, data, and functions needed by the implementation.

Definition at line 132 of file factoring\_machine.h.

#### 4.9.2.4 void\* struct\_factoring\_machine::params

The parameters used by the factorization algorithm. This is a pointer to an algorithm implementation dependant structure holding the algorithm parameters needed by the implementation.

Definition at line 138 of file factoring\_machine.h.

#### 4.9.2.5 ecode\_t(\* struct\_factoring\_machine::init\_context\_func)(struct struct\_factoring\_machine \*const)

A pointer to a function initializing the algorithm context.

##### Parameters:

(*unnamed*) A pointer to the `factoring_machine_t` used by the actual algorithm implementation.

#### 4.9.2.6 ecode\_t(\* struct\_factoring\_machine::perform\_algo\_func)(struct struct\_factoring\_machine \*const)

A pointer to a function performing the actual factorization stage of the factorization algorithm (by opposition to the initialization stage for example).

##### Parameters:

(*unnamed*) A pointer to the `factoring_machine_t` used by the actual algorithm implementation.

#### 4.9.2.7 ecode\_t(\* struct\_factoring\_machine::update\_context\_func)(struct struct\_factoring\_machine \*const)

A pointer to a function updating the context of the factorization algorithm. This function is responsible of the definition of the factorization strategy should something bad happens (e.g. what to do if no factors are found after the first run?).

##### Parameters:

(*unnamed*) A pointer to the `factoring_machine_t` used by the actual algorithm implementation.

#### 4.9.2.8 ecode\_t(\* struct\_factoring\_machine::clear\_context\_func)(struct struct\_factoring\_machine \*const)

A pointer to a function clearing all memory space used by the context.

##### Parameters:

(*unnamed*) A pointer to the `factoring_machine_t` used by the actual algorithm implementation.

#### 4.9.2.9 `ecode_t(* struct factoring_machine::recurse_func)(mpz_array_t *const, uint32_array_t *const, const mpz_t, factoring_mode_t)`

A pointer to the function to use to perform recursive factorization (i.e. factorization of the non-prime factors found).

##### Parameters:

- (unnamed)* A pointer to an `mpz_array_t` to hold the found factors.
- (unnamed)* A pointer to an `uint32_array_t` to hold the multiplicities.
- (unnamed)* The non-prime factor to factorize.
- (unnamed)* The `factoring_mode_t` to use.

#### 4.9.2.10 `mpz_array_t* struct factoring_machine::factors`

A pointer to a `mpz_array_t` to hold the found factors.

Definition at line 191 of file `factoring_machine.h`.

#### 4.9.2.11 `uint32_array_t* struct factoring_machine::multis`

A pointer to a `uint32_array_t` to hold the multiplicities of the found factors.

Definition at line 196 of file `factoring_machine.h`.

#### 4.9.2.12 `bool struct factoring_machine::success`

true if the algorithm succeeds. false otherwise.

##### Note:

The notion of success is given by the `factoring_mode_t` mode used and not on whether or not some factors are found.

Definition at line 204 of file `factoring_machine.h`.

The documentation for this struct was generated from the following file:

- [factoring\\_machine.h](#)

## 4.10 struct factoring\_program Struct Reference

Defines a structure to represent the logic behind all factorization programs.

```
#include <factoring_program.h>
```

##### Data Fields

- `int argc`
- `char ** argv`
- `mpz_t n`
- `factoring_mode_t mode`
- `int verbose`

- int [timing](#)
- uint32\_t [nprimes\\_tdiv](#)
- uint32\_t [nfactors](#)
- char \* [algo\\_name](#)
- void \* [params](#)
- void(\* [print\\_usage\\_func](#) )(struct [struct\\_factoring\\_program](#) \*const)
- void(\* [print\\_params\\_func](#) )(struct [struct\\_factoring\\_program](#) \*const)
- void(\* [process\\_args\\_func](#) )(struct [struct\\_factoring\\_program](#) \*const)
- [ecode\\_t](#)(\* [factoring\\_algo\\_func](#) )(mpz\_array\_t \*const factors, [uint32\\_array\\_t](#) \*const multis, const mpz\_t n, const void \*const params, [factoring\\_mode\\_t](#) mode)
- void(\* [set\\_params\\_to\\_default\\_func](#) )(struct [struct\\_factoring\\_program](#) \*const)

### 4.10.1 Detailed Description

Defines a structure to represent the logic behind all factorization programs.

[tools/include/factoring\\_program.h](#)

This structure defines a set of data and functions to represent the logic behind all factorization programs. The idea is to be able to write down the actual factoring process once and for all so that actual factorization program can use such a structure by merely "filling-in" the gaps.

Definition at line 58 of file [factoring\\_program.h](#).

### 4.10.2 Field Documentation

#### 4.10.2.1 int struct\_factoring\_program::argc

Argument count as given by the "main" function.

Definition at line 62 of file [factoring\\_program.h](#).

#### 4.10.2.2 char\*\* struct\_factoring\_program::argv

Argument values as given by the "main" function.

Definition at line 66 of file [factoring\\_program.h](#).

#### 4.10.2.3 mpz\_t struct\_factoring\_program::n

Integer to factor.

Definition at line 70 of file [factoring\\_program.h](#).

#### 4.10.2.4 factoring\_mode\_t struct\_factoring\_program::mode

Factoring mode to use.

Definition at line 74 of file [factoring\\_program.h](#).

#### 4.10.2.5 int struct\_factoring\_program::verbose

Verbosity option. Should be either 1 (be verbose) or 0 (stay laconic).

Definition at line 78 of file [factoring\\_program.h](#).

**4.10.2.6 `int struct factoring_program::timing`**

Timing option. Should be either 1 (proceed with timings) or 0 (do not perform timings).

Definition at line 83 of file `factoring_program.h`.

**4.10.2.7 `uint32_t struct factoring_program::nprimes_tdiv`**

Number of primes used in the trial division of the number to factor.

Definition at line 87 of file `factoring_program.h`.

**4.10.2.8 `uint32_t struct factoring_program::nfactors`**

The maximum number of factors to collect (excluding the factors found in the trial division stage).

Definition at line 92 of file `factoring_program.h`.

**4.10.2.9 `char* struct factoring_program::algo_name`**

Name of the factoring algorithm to use (preferably a short acronym).

Definition at line 96 of file `factoring_program.h`.

**4.10.2.10 `void* struct factoring_program::params`**

A pointer to the parameters of the factoring algorithm to use.

Definition at line 100 of file `factoring_program.h`.

**4.10.2.11 `void(* struct factoring_program::print_usage_func)(struct struct factoring_program *const)`**

A pointer to a function printing the usage of the factoring program.

**Parameters:**

A pointer to the `factoring_program_t` used by the actual factoring program.

**4.10.2.12 `void(* struct factoring_program::print_params_func)(struct struct factoring_program *const)`**

A pointer to a function printing the values of the parameters used by the actual factoring program.

**Parameters:**

A pointer to the `factoring_program_t` used by the actual factoring program.

**4.10.2.13 `void(* struct factoring_program::process_args_func)(struct struct factoring_program *const)`**

A pointer to a function reading arguments on the command line and setting the parameters of the actual factoring program.

**Parameters:**

A pointer to the `factoring_program_t` used by the actual factoring program.

#### 4.10.2.14 `ecode_t(* struct_factoring_program::factoring_algo_func)(mpz_array_t *const factors, uint32_array_t *const multis, const mpz_t n, const void *const params, factoring_mode_t mode)`

A pointer to a function implementing the factorization algorithm to use.

##### Parameters:

*factors* An `mpz_array_t` to hold the found factors.

*factors* A `uint32_array_t` to hold the found multiplicities.

*n* The integer to factor.

*params* A pointer to the parameters to be used in the factorization algorithm.

*mode* The factorization mode to use.

#### 4.10.2.15 `void(* struct_factoring_program::set_params_to_default_func)(struct_factoring_program *const)`

A pointer to a function setting the algorithm's parameters to some default values.

##### Parameters:

A pointer to the `factoring_program_t` used by the actual factoring program.

The documentation for this struct was generated from the following file:

- [factoring\\_program.h](#)

## 4.11 struct\_fermat\_params\_t Struct Reference

Defines the variable parameters used in Fermat's algorithm (dummy structure).

```
#include <lib/alg/include/fermat.h>
```

### Data Fields

- unsigned int `_dummy_variable_`

#### 4.11.1 Detailed Description

Defines the variable parameters used in Fermat's algorithm (dummy structure).

This structure is intended to define the set of the variable parameters used in Fermat's algorithm.

##### Warning:

For the time being, this is a completely unused dummy structure which is kept only as a placeholder should the need for user parameters arise in future code revisions.

Definition at line 69 of file `fermat.h`.

### 4.11.2 Field Documentation

#### 4.11.2.1 unsigned int struct\_fermap\_params\_t::\_dummy\_variable\_

Unused dummy variable.

Definition at line 73 of file fermap.h.

The documentation for this struct was generated from the following file:

- [fermap.h](#)

## 4.12 struct\_hashtable\_entry\_t Struct Reference

The structure of a hashtable's entry.

```
#include <lib/utills/include/hashtable.h>
```

### Data Fields

- void \* [key](#)
- void \* [data](#)

### 4.12.1 Detailed Description

The structure of a hashtable's entry.

This structure defines a hashtable entry, i.e. some data and its associated key.

Definition at line 110 of file hashtable.h.

### 4.12.2 Field Documentation

#### 4.12.2.1 void\* struct\_hashtable\_entry\_t::key

Key associated to this entry, as a pointer to void.

Definition at line 114 of file hashtable.h.

#### 4.12.2.2 void\* struct\_hashtable\_entry\_t::data

Data associated to this entry, as a pointer to void.

Definition at line 118 of file hashtable.h.

The documentation for this struct was generated from the following file:

- [hashtable.h](#)

## 4.13 struct\_hashtable\_t Struct Reference

A basic implementation of a hashtable.

```
#include <lib/utills/include/hashtable.h>
```

## Data Fields

- `uint32_t allocated`
- `uint32_t nentries`
- `linked_list_t * buckets`
- `int(* cmp_func)(const void *const key_a, const void *const key_b)`
- `uint32_t(* hash_func)(const void *const key)`

### 4.13.1 Detailed Description

A basic implementation of a hashtable.

This structure defines a simple generic hashtable. It can store any type of elements, provided that suitable comparison and hash functions exist for the type of the keys used.

This hashtable implementation uses a simple sequential search in a linked list to solve the collisions.

#### Warning:

Due to limitations in the current implementation, it is strongly advised to use *only* pointers to integers or strings as keys.

Definition at line 59 of file `hashtable.h`.

### 4.13.2 Field Documentation

#### 4.13.2.1 `uint32_t struct_hashtable_t::allocated`

Number of allocated buckets (always a power of two).

Definition at line 63 of file `hashtable.h`.

#### 4.13.2.2 `uint32_t struct_hashtable_t::nentries`

Current number of entries in the hashtable.

Definition at line 67 of file `hashtable.h`.

#### 4.13.2.3 `linked_list_t* struct_hashtable_t::buckets`

Array of `linked_list_t` of size `allocated` used to store the hashtable's entries.

Definition at line 72 of file `hashtable.h`.

#### 4.13.2.4 `int(* struct_hashtable_t::cmp_func)(const void *const key_a, const void *const key_b)`

Pointer to a comparison function for the keys stored in the hashtable. The function's signature should be: `int cmp_func(const void* const, const void* const)`. The function should take two keys of *identical* type passed as pointers to `void`.

For now, the only requirement is that the pointed function should return 0 if two identical keys are compared.



#### 4.13.2.5 uint32\_t(\* struct\_hashtable\_t::hash\_func)(const void \*const key)

Pointer to the hash function used by the hashtable. The hash function's signature should be: `uint32_t hash_func(const void* const)`. The function should take a key passed as a pointer to `void`.

Needless to say, the real type of the key handled by this function should be the same as the one handled by the comparison function pointed by `cmp_int`.

The documentation for this struct was generated from the following file:

- [hashtable.h](#)

## 4.14 struct\_int32\_array\_t Struct Reference

Defines an array of `int32`.

```
#include <lib/utils/include/array.h>
```

### Data Fields

- [uint32\\_t allocated](#)
- [uint32\\_t length](#)
- [int32\\_t\\* data](#)

#### 4.14.1 Detailed Description

Defines an array of `int32`.

This structure defines a special kind of `int32` array which knows its current length and its allocated memory space.

Definition at line 621 of file `array.h`.

#### 4.14.2 Field Documentation

##### 4.14.2.1 uint32\_t struct\_int32\_array\_t::allocated

Memory space allocated for this array's `data` field, given as a multiple of `sizeof(int32_t)`. This is the maximum number of `int32_t` that the array can accommodate.

Definition at line 627 of file `array.h`.

##### 4.14.2.2 uint32\_t struct\_int32\_array\_t::length

Current number of `int32_t` hold in the array pointed by the structure's `data` field.

Definition at line 632 of file `array.h`.

Referenced by `is_in_sorted_int32_array()`.

##### 4.14.2.3 int32\_t\* struct\_int32\_array\_t::data

Array of `int32_t` whose size is given by the `allocated` field.

Definition at line 636 of file `array.h`.

The documentation for this struct was generated from the following file:

- [array.h](#)

## 4.15 `struct_linked_list_node_t` Struct Reference

A basic implementation of a linked list node.

```
#include <linked_list.h>
```

### Data Fields

- struct [struct\\_linked\\_list\\_node\\_t](#) \* `next`
- void \* `data`

#### 4.15.1 Detailed Description

A basic implementation of a linked list node.

[lib/utls/include/linked\\_list.h](#) This structure defines a simple linked list node, i.e. some data together with a pointer to the next node.

Definition at line 51 of file `linked_list.h`.

#### 4.15.2 Field Documentation

##### 4.15.2.1 `struct struct_linked_list_node_t* struct_linked_list_node_t::next` [read]

Pointer to the next node of the linked list.

Definition at line 55 of file `linked_list.h`.

##### 4.15.2.2 `void* struct_linked_list_node_t::data`

Pointer to the node data.

Definition at line 59 of file `linked_list.h`.

The documentation for this struct was generated from the following file:

- [linked\\_list.h](#)

## 4.16 `struct_linked_list_t` Struct Reference

A basic implementation of a linked list.

```
#include <lib/utls/include/linked_list.h>
```

### Data Fields

- struct [struct\\_linked\\_list\\_node\\_t](#) \* `head`
- struct [struct\\_linked\\_list\\_node\\_t](#) \* `tail`
- int(\* [cmp\\_func](#))(const void \*const data\_a, const void \*const data\_b)
- uint32\_t `length`

### 4.16.1 Detailed Description

A basic implementation of a linked list.

This structure defines a simple linked list. It can store any type of elements, provided that there is a suitable comparison function for the type of the data used.

Definition at line 70 of file `linked_list.h`.

### 4.16.2 Field Documentation

#### 4.16.2.1 `struct struct_linked_list_node_t* struct_linked_list_t::head` [read]

Pointer to the head of the linked list.

Definition at line 74 of file `linked_list.h`.

#### 4.16.2.2 `struct struct_linked_list_node_t* struct_linked_list_t::tail` [read]

Pointer to the tail of the linked list.

Definition at line 78 of file `linked_list.h`.

#### 4.16.2.3 `int(* struct_linked_list_t::cmp_func)(const void *const data_a, const void *const data_b)`

Pointer to the comparison function used to compare the node data. This function, which take two pointers to the data to compare, should return:

- 0 if the datas pointed by `data_a` and `data_b` are the same.
- A positive number if the data pointed by `data_a` is greater than the data pointed by `data_b`.
- A negative number if the data pointed by `data_a` is less than the data pointed by `data_b`.

#### 4.16.2.4 `uint32_t struct_linked_list_t::length`

Number of nodes composing the linked list.

Definition at line 93 of file `linked_list.h`.

The documentation for this struct was generated from the following file:

- [linked\\_list.h](#)

## 4.17 `struct_mpz_array_list_t` Struct Reference

Defines a list of `mpz_array_t`.

```
#include <x_array_list.h>
```

### Data Fields

- `uint32_t allocated`
- `uint32_t length`
- `mpz_array_t ** data`

### 4.17.1 Detailed Description

Defines a list of `mpz_array_t`.

`lib/utils/include/x_array.h`

This structure defines an array of pointers to `mpz_array_t` elements. Its name is a bit confusing since it is actually more of an array than a list strictly speaking.

Definition at line 170 of file `x_array_list.h`.

### 4.17.2 Field Documentation

#### 4.17.2.1 uint32\_t struct\_mpz\_array\_list\_t::allocated

This is the maximum number of `mpz_array_t` pointers that the array can accommodate.

Definition at line 175 of file `x_array_list.h`.

#### 4.17.2.2 uint32\_t struct\_mpz\_array\_list\_t::length

Current number of `mpz_array_t` pointers hold in the array pointed by the structure's `data` field.

Definition at line 180 of file `x_array_list.h`.

Referenced by `add_entry_in_mpz_array_list()`.

#### 4.17.2.3 mpz\_array\_t\*\* struct\_mpz\_array\_list\_t::data

Array of pointers to `mpz_array_t` whose size is given by the `allocated` field.

Definition at line 185 of file `x_array_list.h`.

Referenced by `add_entry_in_mpz_array_list()`.

The documentation for this struct was generated from the following file:

- [x\\_array\\_list.h](#)

## 4.18 struct\_mpz\_array\_t Struct Reference

Defines an array of `mpz_t` elements from the GMP library.

```
#include <lib/utils/include/array.h>
```

### Data Fields

- [uint32\\_t allocated](#)
- [uint32\\_t length](#)
- [mpz\\_t \\* data](#)

### 4.18.1 Detailed Description

Defines an array of `mpz_t` elements from the GMP library.

This structure defines a special kind of `mpz` array which knows its current length and its allocated memory space.

Definition at line 857 of file array.h.

## 4.18.2 Field Documentation

### 4.18.2.1 uint32\_t struct\_mpz\_array\_t::allocated

Memory space allocated for this array's data field, given as a multiple of `sizeof(mpz_t)`. This is the maximum number of `mpz_t` elements that the array can accommodate.

Definition at line 863 of file array.h.

### 4.18.2.2 uint32\_t struct\_mpz\_array\_t::length

Current number of "useful" `mpz_t` elements hold in the array pointed by the structure's data field.

#### Warning:

Prior to version 1.2, the `length` field also indicated which positions had been `mpz_init'`ed in the data field. Since version 1.2 this is no longer true. Now all positions in the data array are `mpz_init'`ed and `length` only gives which part of the array is useful from the client standpoint.

Definition at line 874 of file array.h.

Referenced by `is_in_sorted_mpz_array()`.

### 4.18.2.3 mpz\_t\* struct\_mpz\_array\_t::data

Array of `mpz_t` elements whose size is given by the `allocated` field.

Definition at line 879 of file array.h.

The documentation for this struct was generated from the following file:

- [array.h](#)

## 4.19 struct\_mpz\_pair\_t Struct Reference

A pair of `mpz_t` integers.

```
#include <lib/utils/include/gmp_utils.h>
```

### Data Fields

- [mpz\\_t x](#)
- [mpz\\_t y](#)

### 4.19.1 Detailed Description

A pair of `mpz_t` integers.

This very simple structure defines a pair of `mpz_t` integers.

Definition at line 50 of file `gmp_utils.h`.

### 4.19.2 Field Documentation

#### 4.19.2.1 `mpz_t struct_mpz_pair_t::x`

The first `mpz_t` integer of the pair.

Definition at line 54 of file `gmp_utils.h`.

Referenced by `clear_mpz_pair()`, and `init_mpz_pair()`.

#### 4.19.2.2 `mpz_t struct_mpz_pair_t::y`

The second `mpz_t` integer of the pair.

Definition at line 58 of file `gmp_utils.h`.

Referenced by `clear_mpz_pair()`, and `init_mpz_pair()`.

The documentation for this struct was generated from the following file:

- [gmp\\_utils.h](#)

## 4.20 `struct_mult_data_t` Struct Reference

Ad hoc structure used in the computation of the multiplier to use.

```
#include <lib/utils/include/funcs.h>
```

### Data Fields

- `uint32_t multiplier`
- `uint32_t count`
- `double sum_inv_pi`

### 4.20.1 Detailed Description

Ad hoc structure used in the computation of the multiplier to use.

This ad-hoc structure defines several variables needed in the determination of the best multiplier, as described by M. A. Morrison and J. Brillhart in the remark 5.3 of the paper "A Method of Factoring and the Factorization of  $F_7$ " (Mathematics of Computation, vol 29, #129, Jan 1975, pages 183-205).

Definition at line 87 of file `funcs.h`.

### 4.20.2 Field Documentation

#### 4.20.2.1 `uint32_t struct_mult_data_t::multiplier`

The multiplier to use in the factoring algorithms.

Definition at line 91 of file `funcs.h`.

#### 4.20.2.2 `uint32_t struct_mult_data_t::count`

The number of primes  $p_i$  less than or equal to the `MAX_IPRIME_IN_MULT_CALC`-th prime for which the legendre symbol  $(k*N/p_i)$  is 0 or 1 *and* for which either  $(k*N/3)$  or  $(k*N/5)$  (or both) is 0 or 1.

Definition at line 99 of file `funcs.h`.

#### 4.20.2.3 `double struct_mult_data_t::sum_inv_pi`

The sum of  $1/p_i$  where  $\{p_i\}$  is the set of primes previously described.

Definition at line 104 of file `funcs.h`.

The documentation for this struct was generated from the following file:

- [funcs.h](#)

## 4.21 `struct_siqs_params_t` Struct Reference

Defines the variable parameters used in the SIQS algorithm.

```
#include <lib/algo/include/siqs.h>
```

### Data Fields

- `uint32_t sieve_half_width`
- `uint32_t nprimes_in_base`
- `uint32_t threshold`
- `uint32_t nprimes_tdiv`
- `uint32_t nrelations`
- `linalg_method_t linalg_method`
- `bool use_large_primes`

### 4.21.1 Detailed Description

Defines the variable parameters used in the SIQS algorithm.

This structure defines the set of the variable parameters used in the SIQS algorithm.

Definition at line 89 of file `siqs.h`.

### 4.21.2 Field Documentation

#### 4.21.2.1 `uint32_t struct_siqs_params_t::sieve_half_width`

Sieve's half-width, i.e. the SIQS will sieve in the interval  $[-sieve\_half\_width, sieve\_half\_width]$ .

Definition at line 94 of file `siqs.h`.

#### 4.21.2.2 `uint32_t struct_siqs_params_t::nprimes_in_base`

Number of prime numbers composing the factor base on which to factor the residues.

Definition at line 99 of file `siqs.h`.

#### 4.21.2.3 `uint32_t struct_siqs_params_t::threshold`

Sieve threshold.

Definition at line 103 of file `siqs.h`.

#### 4.21.2.4 `uint32_t struct_siqs_params_t::nprimes_tdiv`

Number of the first primes to use in the trial division of the residues.

##### Warning:

`nprimes_tdiv` should be greater than or equal to 1.

Definition at line 111 of file `siqs.h`.

#### 4.21.2.5 `uint32_t struct_siqs_params_t::nrelations`

Number of congruence relations to find before attempting the factorization of the large integer.

Definition at line 116 of file `siqs.h`.

#### 4.21.2.6 `linalg_method_t struct_siqs_params_t::linalg_method`

Linear system resolution method to use.

Definition at line 120 of file `siqs.h`.

#### 4.21.2.7 `bool struct_siqs_params_t::use_large_primes`

True if we use the large prime variation. False otherwise.

Definition at line 125 of file `siqs.h`.

The documentation for this struct was generated from the following file:

- [siqs.h](#)

## 4.22 `struct_siqs_poly_t` Struct Reference

Defines polynomials used by SIQS.

```
#include <lib/utils/include/siqs_poly.h>
```

### Data Fields

- `mpz_t a`
- `mpz_t b`
- `mpz_t c`
- `mpz_t n`
- `uint32_t loga`
- `uint32_t logb`
- `uint32_t logc`
- `approximer_t * approximer`
- `uint32_array_t * factor_base`
- `uint32_array_t * sqrtm_pi`
- `int32_array_t * sol1`
- `int32_array_t * sol2`
- `mpz_array_t * B1`
- `uint32_t ** Bainv2`



- [uint32\\_t npolys](#)
- [uint32\\_t polyno](#)
- [uint32\\_t nprimes\\_in\\_a](#)
- [uint32\\_t \\* idx\\_of\\_a](#)
- [uint32\\_t nfullpolyinit](#)

#### 4.22.1 Detailed Description

Defines polynomials used by SIQS.

This structure defines the polynomials used by SIQS together with all its associated data.

A polynomial  $\mathbf{P}$  is given by  $\mathbf{aX}^2 + \mathbf{bX} + \mathbf{c}$ .

Definition at line 53 of file siqs\_poly.h.

#### 4.22.2 Field Documentation

##### 4.22.2.1 mpz\_t struct\_siqs\_poly\_t::a

The  $\mathbf{a}$  coefficient

Definition at line 57 of file siqs\_poly.h.

##### 4.22.2.2 mpz\_t struct\_siqs\_poly\_t::b

The  $\mathbf{b}$  coefficient

Definition at line 61 of file siqs\_poly.h.

##### 4.22.2.3 mpz\_t struct\_siqs\_poly\_t::c

The  $\mathbf{c}$  coefficient

Definition at line 65 of file siqs\_poly.h.

##### 4.22.2.4 mpz\_t struct\_siqs\_poly\_t::n

The number to factor (or a small multiple if a multiplier is used)

Definition at line 69 of file siqs\_poly.h.

##### 4.22.2.5 uint32\_t struct\_siqs\_poly\_t::loga

Logarithm of  $\mathbf{a}$  in base 2

Definition at line 73 of file siqs\_poly.h.

##### 4.22.2.6 uint32\_t struct\_siqs\_poly\_t::logb

Logarithm of  $\mathbf{b}$  in base 2

Definition at line 77 of file siqs\_poly.h.

**4.22.2.7 uint32\_t struct\_siqs\_poly\_t::logc**

Logarithm of **c** in base 2

Definition at line 81 of file siqs\_poly.h.

**4.22.2.8 approximer\_t\* struct\_siqs\_poly\_t::approximer**

An **approximer\_t** used to determine suitable values of the **a** coefficient

Definition at line 86 of file siqs\_poly.h.

**4.22.2.9 uint32\_array\_t\* struct\_siqs\_poly\_t::factor\_base**

The factor base

Definition at line 90 of file siqs\_poly.h.

**4.22.2.10 uint32\_array\_t\* struct\_siqs\_poly\_t::sqrtm\_pi**

The modular square roots of **n** modulo each primes in the factor base

Definition at line 94 of file siqs\_poly.h.

**4.22.2.11 int32\_array\_t\* struct\_siqs\_poly\_t::sol1**

The first solution to the equation  $P(x) = 0 \pmod{\mathbf{p}_i}$  for each prime **pi** in the factor base

Definition at line 99 of file siqs\_poly.h.

**4.22.2.12 int32\_array\_t\* struct\_siqs\_poly\_t::sol2**

The second solution to the equation  $P(x) = 0 \pmod{\mathbf{p}_i}$  for each prime **pi** in the factor base

Definition at line 104 of file siqs\_poly.h.

**4.22.2.13 mpz\_array\_t\* struct\_siqs\_poly\_t::B1**

For all **l** in  $[0, \text{npolys}-1]$  solutions to

- $B_l^2 = n \pmod{q_l}$
- $B_l = 0 \pmod{q_j}$  for all  $j \neq l$

where **q<sub>i</sub>** are the primes from the factor base such that  $\mathbf{a} = \mathbf{q}_0 \times \mathbf{q}_1 \times \dots \times \mathbf{q}_{\text{npolys}}$

Definition at line 114 of file siqs\_poly.h.

**4.22.2.14 uint32\_t\*\* struct\_siqs\_poly\_t::Bainv2**

$B_{\text{ainv2}}[i][j] = 2 \times B_l[i] \times \text{inv}(\mathbf{a}) \pmod{\mathbf{p}_j}$  for **i** in  $[0, \text{npolys}-1]$  and **pj** in the factor base

Definition at line 119 of file siqs\_poly.h.

**4.22.2.15 uint32\_t struct\_siqs\_poly\_t::npolys**

Number of different polynomials having the same **a** coefficient

Definition at line 123 of file siqs\_poly.h.

**4.22.2.16** `uint32_t struct_siqs_poly_t::polyno`

Current polynomial number (from 1 to `npolys`)

Definition at line 127 of file `siqs_poly.h`.

**4.22.2.17** `uint32_t struct_siqs_poly_t::nprimes_in_a`

Number of primes in the prime decomposition of `a`

Definition at line 131 of file `siqs_poly.h`.

**4.22.2.18** `uint32_t* struct_siqs_poly_t::idx_of_a`

Indexes (in the factor base) of the (prime) factors of `a`

Definition at line 135 of file `siqs_poly.h`.

**4.22.2.19** `uint32_t struct_siqs_poly_t::nfullpolyinit`

Number of "full" polynomial initializations performed

Definition at line 139 of file `siqs_poly.h`.

The documentation for this struct was generated from the following file:

- [siqs\\_poly.h](#)

**4.23** `struct_siqs_sieve_t` Struct Reference

Defines the sieve used by SIQS.

```
#include <lib/utils/include/siqs_sieve.h>
```

**Data Fields**

- `uint32_t nchunks`
- `uint32_t chunk_size`
- `int32_t next_chunkno_to_fill`
- `uint32_t scan_begin`
- `uint32_t threshold`
- `byte_array_t * log_primes`
- `byte_array_t * sieve`
- `siqs_poly_t * poly`
- `int32_array_t * sol1`
- `int32_array_t * sol2`
- `uint32_t endlast`
- `bool use_buckets`
- `uint32_t nprimes_no_buckets`
- `uint32_t buckets_first_prime`
- `buckets_t * buckets_positive`
- `buckets_t * buckets_negative`
- `stopwatch_t init_poly_timer`
- `stopwatch_t fill_timer`
- `stopwatch_t scan_timer`

### 4.23.1 Detailed Description

Defines the sieve used by SIQS.

This structure defines the sieve used by SIQS together with all its associated data.

Definition at line 122 of file `siqs_sieve.h`.

### 4.23.2 Field Documentation

#### 4.23.2.1 `uint32_t struct_siqs_sieve_t::nchunks`

Number of blocks to sieve on each side of zero (`nchunks` for positive `x` and `nchunks` for negative `x`)

Definition at line 127 of file `siqs_sieve.h`.

#### 4.23.2.2 `uint32_t struct_siqs_sieve_t::chunk_size`

Size of a sieve chunk. The total sieving interval is thus given by  $2 * \text{chunk\_size} * \text{nchunks}$

Definition at line 132 of file `siqs_sieve.h`.

#### 4.23.2.3 `int32_t struct_siqs_sieve_t::next_chunkno_to_fill`

The number of the next sieve chunk to fill (in  $[\text{nchunks}, 0[ \cup ]0, \text{nchunks}]$ )

Definition at line 137 of file `siqs_sieve.h`.

#### 4.23.2.4 `uint32_t struct_siqs_sieve_t::scan_begin`

The position to start scanning in the next sieve chunk to scan

Definition at line 141 of file `siqs_sieve.h`.

#### 4.23.2.5 `uint32_t struct_siqs_sieve_t::threshold`

The sieve threshold. An `xi` will be tested for smoothness if `sieve[xi] < threshold`

Definition at line 146 of file `siqs_sieve.h`.

#### 4.23.2.6 `byte_array_t* struct_siqs_sieve_t::log_primes`

Approximated logarithm (in base 2) of the primes in the factor base

Definition at line 150 of file `siqs_sieve.h`.

#### 4.23.2.7 `byte_array_t* struct_siqs_sieve_t::sieve`

The actual sieve array, of size `chunk_size`

Definition at line 154 of file `siqs_sieve.h`.

#### 4.23.2.8 `siqs_poly_t* struct_siqs_sieve_t::poly`

The SIQS polynomial

Definition at line 158 of file `siqs_sieve.h`.

**4.23.2.9 `int32_array_t* struct_siqs_sieve_t::sol1`**

The first solution to the equation  $P(x) = 0 \pmod{p_i}$  for each prime  $p_i$  in the factor base

Definition at line 163 of file `siqs_sieve.h`.

**4.23.2.10 `int32_array_t* struct_siqs_sieve_t::sol2`**

The first solution to the equation  $P(x) = 0 \pmod{p_i}$  for each prime  $p_i$  in the factor base

Definition at line 168 of file `siqs_sieve.h`.

**4.23.2.11 `uint32_t struct_siqs_sieve_t::endlast`**

The index of the last position to sieve in the last sieve chunk (on either side)

Definition at line 174 of file `siqs_sieve.h`.

**4.23.2.12 `bool struct_siqs_sieve_t::use_buckets`**

Should we use a bucket sieving for the largest primes in the base?

Definition at line 180 of file `siqs_sieve.h`.

**4.23.2.13 `uint32_t struct_siqs_sieve_t::nprimes_no_buckets`**

Index (in the factor base) of the largest prime for which a standard sieving procedure is use

Definition at line 185 of file `siqs_sieve.h`.

**4.23.2.14 `uint32_t struct_siqs_sieve_t::buckets_first_prime`**

Index (in the factor base) of the smallest prime for which the bucket sieving procedure is use

Definition at line 190 of file `siqs_sieve.h`.

**4.23.2.15 `buckets_t* struct_siqs_sieve_t::buckets_positive`**

Buckets for the positive  $x$ 's

Definition at line 194 of file `siqs_sieve.h`.

**4.23.2.16 `buckets_t* struct_siqs_sieve_t::buckets_negative`**

Buckets for the negative  $x$ 's

Definition at line 198 of file `siqs_sieve.h`.

**4.23.2.17 `stopwatch_t struct_siqs_sieve_t::init_poly_timer`**

Additional stopwatch (to get timing for the polynomial initializations)

Definition at line 202 of file `siqs_sieve.h`.

**4.23.2.18 `stopwatch_t struct_siqs_sieve_t::fill_timer`**

Additional stopwatch (to get timing for the sieve filling)

Definition at line 206 of file `siqs_sieve.h`.

#### 4.23.2.19 `stopwatch_t struct_siqs_sieve_t::scan_timer`

Additional stopwatch (to get timing for the sieve scanning)

Definition at line 210 of file `siqs_sieve.h`.

The documentation for this struct was generated from the following file:

- [siqs\\_sieve.h](#)

## 4.24 `struct_smooth_filter_t` Struct Reference

Structure grouping variables needed for multi-step early abort strategy.

```
#include <smooth_filter.h>
```

### Data Fields

- `mpz_ptr n`
- `mpz_ptr kn`
- `smooth_filter_method_t method`
- unsigned short int `nsteps`
- unsigned long int `batch_size`
- unsigned long int `base_size`
- `uint32_array_t * complete_base`
- `uint32_array_t * factor_base [MAX_NSTEPS]`
- `mpz_array_t * candidate_xi`
- `mpz_array_t * candidate_yi`
- `mpz_array_t * candidate_ai`
- `mpz_array_t * accepted_xi`
- `mpz_array_t * accepted_yi`
- `mpz_array_t * accepted_ai`
- `mpz_array_t * filtered_xi [MAX_NSTEPS]`
- `mpz_array_t * filtered_yi [MAX_NSTEPS]`
- `mpz_array_t * filtered_ai [MAX_NSTEPS]`
- `mpz_array_t * cofactors [MAX_NSTEPS]`
- `mpz_t bounds [MAX_NSTEPS]`
- `mpz_t prod_pj [MAX_NSTEPS+1]`
- `hashtable_t * htable`
- bool `use_large_primes`
- bool `use_siqs_variant`

### 4.24.1 Detailed Description

Structure grouping variables needed for multi-step early abort strategy.

[lib/utls/include/smooth\\_filter.h](#)

This structure and its associated functions implement the multi-step early abort strategy in a way reminiscent of Pomerance's suggestion in "Analysis and Comparison of Some Integer Factoring Algorithm" with the exception that the smoothness tests are performed by batch instead of trial division.

C. Pomerance, *Analysis and Comparison of Some Integer Factoring Algorithm*, in Mathematical Centre Tracts 154.

Definition at line 171 of file `smooth_filter.h`.

#### 4.24.2 Field Documentation

##### 4.24.2.1 `mpz_ptr struct_smooth_filter_t::n`

The number to factor.

Definition at line 175 of file `smooth_filter.h`.

##### 4.24.2.2 `mpz_ptr struct_smooth_filter_t::kn`

The number to factor multiplied by a multiplier.

Definition at line 179 of file `smooth_filter.h`.

##### 4.24.2.3 `smooth_filter_method_t struct_smooth_filter_t::method`

The method to use for smooth residue detection.

Definition at line 183 of file `smooth_filter.h`.

##### 4.24.2.4 `unsigned short int struct_smooth_filter_t::nsteps`

The number of steps in the early abort strategy. If `nsteps == 0` no early abort is performed.

#### Note:

`nsteps` should be less than or equal to `MAX_NSTEPS`.

Definition at line 190 of file `smooth_filter.h`.

##### 4.24.2.5 `unsigned long int struct_smooth_filter_t::batch_size`

Number of relations to accumulate before testing for smoothness.

Definition at line 194 of file `smooth_filter.h`.

##### 4.24.2.6 `unsigned long int struct_smooth_filter_t::base_size`

Size of the complete factor base.

Definition at line 198 of file `smooth_filter.h`.

##### 4.24.2.7 `uint32_array_t* struct_smooth_filter_t::complete_base`

Pointer to the complete factor base.

Definition at line 202 of file `smooth_filter.h`.

##### 4.24.2.8 `uint32_array_t* struct_smooth_filter_t::factor_base[MAX_NSTEPS]`

Array giving the factor base to use at each step if we use the early-abort strategy.

Definition at line 207 of file `smooth_filter.h`.

#### 4.24.2.9 mpz\_array\_t\* struct\_smooth\_filter\_t::candidate\_xi

The candidate  $x$ 's. Together with `candidate_yi`, stores candidate relations verifying  $x^2 \pmod{kn} == y \pmod{kn}$

**Note:**

See `candidate_ai` if `use_siqs_batch_variant` is true. In that case the relations become  $x^2 \pmod{kn} == y * a \pmod{kn}$ .

Definition at line 216 of file `smooth_filter.h`.

#### 4.24.2.10 mpz\_array\_t\* struct\_smooth\_filter\_t::candidate\_yi

The candidate  $y$ 's. Together with `candidate_xi`, stores candidate relations verifying  $x^2 \pmod{kn} == y \pmod{kn}$

**Note:**

See `candidate_ai` if `use_siqs_batch_variant` is true. In that case the relations become  $x^2 \pmod{kn} == y * a \pmod{kn}$ .

Definition at line 225 of file `smooth_filter.h`.

#### 4.24.2.11 mpz\_array\_t\* struct\_smooth\_filter\_t::candidate\_ai

Used only if `use_siqs_batch_variant` is true.

`candidate_ai` stores the  $a$ 's (i.e. the value of the first parameter of the SIQS polynomial used). Together with `candidate_xi` and `candidate_yi`, stores candidate relations verifying  $x^2 \pmod{kn} == y * a \pmod{kn}$ .

Definition at line 234 of file `smooth_filter.h`.

#### 4.24.2.12 mpz\_array\_t\* struct\_smooth\_filter\_t::accepted\_xi

The accepted  $x$ 's. Together with `accepted_yi`, stores 'good' relations verifying  $x^2 \pmod{kn} == y \pmod{kn}$  with  $y$  smooth over the factor base.

**Note:**

See `accepted_ai` if `use_siqs_batch_variant` is true. In that case the relations become  $x^2 \pmod{kn} == y * a \pmod{kn}$ .

Definition at line 244 of file `smooth_filter.h`.

#### 4.24.2.13 mpz\_array\_t\* struct\_smooth\_filter\_t::accepted\_yi

The accepted  $y$ 's. Together with `accepted_xi`, stores 'good' relations verifying  $x^2 \pmod{kn} == y \pmod{kn}$  with  $y$  smooth over the factor base.

**Note:**

See `accepted_ai` if `use_siqs_batch_variant` is true. In that case the relations become  $x^2 \pmod{kn} == y * a \pmod{kn}$ .

Definition at line 254 of file `smooth_filter.h`.



**4.24.2.14 `mpz_array_t* struct_smooth_filter_t::accepted_ai`**

Used only if `use_siqs_batch_variant` is true.

The `accepted_a`'s (i.e. the value of the first parameter of the SIQS polynomial used). Together with `accepted_xi`, and `accepted_yi`, stores candidate relations verifying  $x^2 \pmod{kn} == y * a \pmod{kn}$  with `y` smooth over the factor base.

Definition at line 264 of file `smooth_filter.h`.

**4.24.2.15 `mpz_array_t* struct_smooth_filter_t::filtered_xi[MAX_NSTEPS]`**

The `filtered_xi[s]` array gives the filtered `x`'s after `s` early abort steps. Together with `filtered_yi[s]` and `cofactors[s]`, stores relations verifying  $x^2 \pmod{kn} == y * cofactor \pmod{kn}$  with `cofactor` smooth over the base composed by the `partial_factor` bases used in the early abort steps up to (and including) the `s`-th one, and with `y` less than `bounds[s]`.

**Note:**

See `filtered_ai` if `use_siqs_batch_variant` is true. In that case the relations become  $x^2 \pmod{kn} == y * a * cofactor \pmod{kn}$ .

Definition at line 278 of file `smooth_filter.h`.

**4.24.2.16 `mpz_array_t* struct_smooth_filter_t::filtered_yi[MAX_NSTEPS]`**

The `filtered_yi[s]` array gives the filtered `x`'s after `s` early abort steps. See `filtered_xi`.

Definition at line 283 of file `smooth_filter.h`.

**4.24.2.17 `mpz_array_t* struct_smooth_filter_t::filtered_ai[MAX_NSTEPS]`**

The `filtered_ai[s]` array gives the filtered `a`'s after `s` early abort steps. See `filtered_xi`.

Definition at line 288 of file `smooth_filter.h`.

**4.24.2.18 `mpz_array_t* struct_smooth_filter_t::cofactors[MAX_NSTEPS]`**

The `cofactor[s]` array gives the cofactors of the `y`'s in `filtered_yi[s]` after `s` early abort steps. See `filtered_xi`.

Definition at line 293 of file `smooth_filter.h`.

**4.24.2.19 `mpz_t struct_smooth_filter_t::bounds[MAX_NSTEPS]`**

`bounds[s]` is the upper bound of the `s`-th early abort step. A relation will not pass this step if it has a `y` greater than this bound.

Definition at line 299 of file `smooth_filter.h`.

**4.24.2.20 `mpz_t struct_smooth_filter_t::prod_pj[MAX_NSTEPS+1]`**

`prod_pj[s]` is the product of all the elements in the partial factor base at the `s`-th early abort step.

Definition at line 304 of file `smooth_filter.h`.

#### 4.24.2.21 `hashtable_t*` `struct_smooth_filter_t::htable`

Hashtable used if the large prime variation is used. Can be `NULL` if the variation is not used.

Definition at line 309 of file `smooth_filter.h`.

#### 4.24.2.22 `bool` `struct_smooth_filter_t::use_large_primes`

true if and only if we are using the large prime variation.

Definition at line 313 of file `smooth_filter.h`.

#### 4.24.2.23 `bool` `struct_smooth_filter_t::use_siqs_variant`

true if and only if we are using this `smooth_filter_t` with SIQS.

Definition at line 318 of file `smooth_filter.h`.

The documentation for this struct was generated from the following file:

- [smooth\\_filter.h](#)

## 4.25 `struct_squfof_params_t` Struct Reference

Defines the variable parameters used in the SQUFOF algorithm (dummy structure).

```
#include <lib/algo/include/squfof.h>
```

### Data Fields

- unsigned int `_dummy_variable_`

### 4.25.1 Detailed Description

Defines the variable parameters used in the SQUFOF algorithm (dummy structure).

This structure is intended to define the set of the variable parameters used in the SQUFOF algorithm.

#### Warning:

For the time being, this is a completely unused dummy structure which is kept only as a placeholder should the need for user parameters arise in future code revisions.

Definition at line 79 of file `squfof.h`.

### 4.25.2 Field Documentation

#### 4.25.2.1 `unsigned int` `struct_squfof_params_t::_dummy_variable_`

Unused dummy variable.

Definition at line 83 of file `squfof.h`.

The documentation for this struct was generated from the following file:

- [squfof.h](#)

## 4.26 struct\_stopwatch\_t Struct Reference

Defines a very basic stopwatch-like timer.

```
#include <lib/utils/include/stopwatch.h>
```

### Data Fields

- struct rusage [rsg](#) [1]
- uint64\_t [started\\_usec](#)
- uint64\_t [elapsed\\_usec](#)
- bool [is\\_running](#)

### 4.26.1 Detailed Description

Defines a very basic stopwatch-like timer.

This structure defines very basic stopwatch-like timer based on the `rusage` structure.

Definition at line 55 of file `stopwatch.h`.

### 4.26.2 Field Documentation

#### 4.26.2.1 struct rusage struct\_stopwatch\_t::rsg[1] [read]

An `rusage` structure.

Definition at line 59 of file `stopwatch.h`.

#### 4.26.2.2 uint64\_t struct\_stopwatch\_t::started\_usec

The time (in microseconds) when the stopwatch started.

Definition at line 63 of file `stopwatch.h`.

#### 4.26.2.3 uint64\_t struct\_stopwatch\_t::elapsed\_usec

The elapsed time accumulated (in microseconds).

Definition at line 67 of file `stopwatch.h`.

#### 4.26.2.4 bool struct\_stopwatch\_t::is\_running

`true` iif the stopwatch is currently running.

Definition at line 71 of file `stopwatch.h`.

The documentation for this struct was generated from the following file:

- [stopwatch.h](#)

## 4.27 struct\_uint32\_array\_list\_t Struct Reference

Defines a list of `uint32_array_t`.

```
#include <x_array_list.h>
```

## Data Fields

- [uint32\\_t allocated](#)
- [uint32\\_t length](#)
- [uint32\\_array\\_t \\*\\* data](#)

### 4.27.1 Detailed Description

Defines a list of `uint32_array_t`.

`lib/utils/include/x_array.h`

This structure defines an array of pointers to `uint32_array_t` elements. Its name is a bit confusing since it is actually more of an array than a list strictly speaking.

Definition at line 62 of file `x_array_list.h`.

### 4.27.2 Field Documentation

#### 4.27.2.1 uint32\_t struct\_uint32\_array\_list\_t::allocated

This is the maximum number of `uint32_array_t` pointers that the array can accommodate.

Definition at line 67 of file `x_array_list.h`.

Referenced by `add_entry_in_uint32_array_list()`.

#### 4.27.2.2 uint32\_t struct\_uint32\_array\_list\_t::length

Current number of `uint32_array_t` pointers hold in the array pointed by the structure's `data` field.

Definition at line 72 of file `x_array_list.h`.

Referenced by `add_entry_in_uint32_array_list()`.

#### 4.27.2.3 uint32\_array\_t\*\* struct\_uint32\_array\_list\_t::data

Array of pointers to `uint32_array_t` whose size is given by the `allocated` field.

Definition at line 77 of file `x_array_list.h`.

Referenced by `add_entry_in_uint32_array_list()`.

The documentation for this struct was generated from the following file:

- [x\\_array\\_list.h](#)

## 4.28 struct\_uint32\_array\_t Struct Reference

Defines an array of `uint32`.

```
#include <lib/utils/include/array.h>
```

## Data Fields

- [uint32\\_t allocated](#)
- [uint32\\_t length](#)

- `uint32_t * data`

#### 4.28.1 Detailed Description

Defines an array of `uint32`.

This structure defines a special kind of `uint32` array which knows its current length and its allocated memory space.

Definition at line 361 of file `array.h`.

#### 4.28.2 Field Documentation

##### 4.28.2.1 `uint32_t struct_uint32_array_t::allocated`

Memory space allocated for this array's `data` field, given as a multiple of `sizeof(uint32_t)`. This is the maximum number of `uint32_t` that the array can accommodate.

Definition at line 367 of file `array.h`.

##### 4.28.2.2 `uint32_t struct_uint32_array_t::length`

Current number of `uint32_t` hold in the array pointed by the structure's `data` field.

Definition at line 372 of file `array.h`.

Referenced by `is_in_sorted_uint32_array()`.

##### 4.28.2.3 `uint32_t* struct_uint32_array_t::data`

Array of `uint32_t` whose size is given by the `allocated` field.

Definition at line 376 of file `array.h`.

The documentation for this struct was generated from the following file:

- [array.h](#)

## 4.29 struct\_uint32\_tuple\_t Struct Reference

Defines a tuple of integers together with a sorting key.

```
#include <lib/utills/include/approx.h>
```

#### Data Fields

- `uint32_t tuple` [MAX\_NPRIMES\_IN\_TUPLE]
- `float tlog`

#### 4.29.1 Detailed Description

Defines a tuple of integers together with a sorting key.

This structure defines a tuple of up to `MAX_NPRIMES_IN_TUPLE` integers together with a sorting key given as a float.

Definition at line 90 of file approx.h.

#### 4.29.2 Field Documentation

##### 4.29.2.1 `uint32_t struct_uint32_tuple_t::tuple[MAX_NPRIMES_IN_TUPLE]`

The value of the tuple.

Definition at line 94 of file approx.h.

##### 4.29.2.2 `float struct_uint32_tuple_t::tlog`

Used as a key to sort tuples.

Definition at line 98 of file approx.h.

The documentation for this struct was generated from the following file:

- [approx.h](#)

## 5 File Documentation

### 5.1 approx.h File Reference

Approximate a value by multiplying some numbers from a pool.

```
#include <stdint.h>
#include <stdbool.h>
#include "exit_codes.h"
#include "array.h"
```

#### Data Structures

- struct [struct\\_uint32\\_tuple\\_t](#)  
*Defines a tuple of integers together with a sorting key.*
- struct [struct\\_approximer\\_t](#)  
*Structure used to find number approximation.*

#### Defines

- #define [\\_TIFA\\_APPROX\\_H\\_](#)
- #define [MAX\\_NPRIMES\\_IN\\_TUPLE](#) 3

#### Typedefs

- typedef struct [struct\\_uint32\\_tuple\\_t](#) [uint32\\_tuple\\_t](#)  
*Equivalent to [struct\\_uint32\\_tuple\\_t](#).*

**Functions**

- `approximer_t * alloc_approximer (mpz_t target, uint32_array_t *const facpool, uint32_t nfactores)`  
*Allocates and returns a new approximer\_t.*
- `void free_approximer (approximer_t *aximer)`  
*Frees a previously allocated approximer\_t.*
- `void random_approximation (approximer_t *const aximer, mpz_t approxed, uint32_t *indexes)`  
*Generates a "random" approximation.*

**5.1.1 Detailed Description**

Approximate a value by multiplying some numbers from a pool.

**Author:**

Jerome Milan

**Date:**

Fri Jun 10 2011

**Version:**

2011-06-10

This provides a structure `approximer_t` and associated functions that can be used to approximate a target value by multiplying a given number of factors from a given base. Each factor is allowed to appear only once in the decomposition of the approximation on the given base.

This is used in TIFA's SIQS implementation where we need to find a polynomial coefficient of a given order from the product of some prime numbers.

The strategy used to reach a good approximation is adapted from the Carrier-Wagstaff method.

- Let  $t$  be the target number to be obtained by multiplying  $n$  distinct numbers from a given base  $\mathbf{B}=[p_{-1}, p_{-2}, p_{-3}, \dots]$  (with  $p_i < p_{i+1}$ ).
- Set  $m$  so that  $\mathbf{B}[m]$  is roughly equal to the  $n^{\text{th}}$ -root of  $t$ . Factors will be chosen from the set  $\mathbf{B}[m-d], \dots, \mathbf{B}[m+d]$  with  $d$  suitably chosen.
- The approximation  $a$  of the target  $t$  is obtained by choosing a random combination of  $(n-i)$  factors completed by  $i$  other factors so as to obtain the best approximation as possible.
- Since all numbers must be distinct the  $(n-i)$  randomly chosen factors are picked from the set of  $\mathbf{B}[j]$  with  $j$  odd and the remaining  $i$  factors from the set of  $\mathbf{B}[k]$  with  $k$  even.
- The best remaining  $i$  factors are obtained by precomputing and sorting all combinations of  $i$  factors, then picking the most suitable one.

Definition in file [approx.h](#).

## 5.1.2 Define Documentation

### 5.1.2.1 #define \_TIFA\_APPROX\_H\_

Standard include guard.

Definition at line 65 of file approx.h.

### 5.1.2.2 #define MAX\_NPRIMES\_IN\_TUPLE 3

Maximum number of factors in the sorted factor combinations.

Definition at line 81 of file approx.h.

## 5.1.3 Function Documentation

### 5.1.3.1 approximer\_t\* alloc\_approximer (mpz\_t target, uint32\_array\_t \*const facpool, uint32\_t nfactores)

Allocates and returns a new `approximer_t`.

#### Parameters:

- target* the target number to approximate.
- facpool* the pool of available factors.
- nfactors* the number of factors from `facpool` to use.

#### Returns:

A pointer to the newly allocated `approximer_t`.

### 5.1.3.2 void free\_approximer (approximer\_t \* aximer)

Frees a previously allocated `approximer_t`.

Frees all memory used by the pointed `approximer_t` and then frees the `aximer` pointer.

#### Warning:

Do not call `free(aximer)` in client code after a call to `free_approximer(aximer)`: it would result in an error.

#### Parameters:

*aximer* the `approximer_t` to free.

### 5.1.3.3 void random\_approximation (approximer\_t \*const aximer, mpz\_t approxed, uint32\_t \* indexes)

Generates a "random" approximation.

#### Parameters:

- ← *aximer* the `approximer_t` to use.
- *approxed* the approximation obtained.
- *indexes* the (sorted) indexes of the factors making up the approximation.



## 5.2 array.h File Reference

Higher level arrays and associated functions.

```
#include "tifa_config.h"
#include <inttypes.h>
#include <stdbool.h>
#include <gmp.h>
#include "bitstring_t.h"
```

### Data Structures

- struct [struct\\_byte\\_array\\_t](#)  
*Defines an array of bytes.*
- struct [struct\\_uint32\\_array\\_t](#)  
*Defines an array of uint32.*
- struct [struct\\_int32\\_array\\_t](#)  
*Defines an array of int32.*
- struct [struct\\_mpz\\_array\\_t](#)  
*Defines an array of mpz\_t elements from the GMP library.*
- struct [struct\\_binary\\_array\\_t](#)  
*Defines an array of bits.*

### Defines

- #define [\\_TIFA\\_ARRAY\\_H\\_](#)
- #define [ELONGATION](#) 16
- #define [NOT\\_IN\\_ARRAY](#) UINT32\_MAX
- #define [ARRAY\\_IS\\_FULL](#)(ARRAY\_PTR) ((ARRAY\_PTR) → length == (ARRAY\_PTR) → allocated)
- #define [reset\\_byte\\_array](#)(ARRAY) do {(ARRAY) → length = 0;} while (0)  
*Resets a byte\_array\_t.*
- #define [reset\\_uint32\\_array](#)(ARRAY) do {(ARRAY) → length = 0;} while (0)  
*Resets a uint32\_array\_t.*
- #define [reset\\_int32\\_array](#)(ARRAY) do {(ARRAY) → length = 0;} while (0)  
*Resets an int32\_array\_t.*
- #define [reset\\_mpz\\_array](#)(ARRAY) do {(ARRAY) → length = 0;} while (0)  
*Resets an mpz\_array\_t.*
- #define [reset\\_binary\\_array](#)(ARRAY) do {(ARRAY) → length = 0;} while (0)  
*Resets a binary\_array\_t.*

## Typedefs

- typedef struct [struct\\_byte\\_array\\_t](#) [byte\\_array\\_t](#)  
*Equivalent to struct [struct\\_byte\\_array\\_t](#).*
- typedef struct [struct\\_uint32\\_array\\_t](#) [uint32\\_array\\_t](#)  
*Equivalent to struct [struct\\_uint32\\_array\\_t](#).*
- typedef struct [struct\\_int32\\_array\\_t](#) [int32\\_array\\_t](#)  
*Equivalent to struct [struct\\_int32\\_array\\_t](#).*
- typedef struct [struct\\_mpz\\_array\\_t](#) [mpz\\_array\\_t](#)  
*Equivalent to struct [struct\\_mpz\\_array\\_t](#).*
- typedef struct [struct\\_binary\\_array\\_t](#) [binary\\_array\\_t](#)  
*Equivalent to struct [struct\\_binary\\_array\\_t](#).*

## Functions

- [byte\\_array\\_t \\* alloc\\_byte\\_array](#) ([uint32\\_t](#) length)  
*Allocates and returns a new [byte\\_array\\_t](#).*
- void [free\\_byte\\_array](#) ([byte\\_array\\_t](#) \*array)  
*Frees a [byte\\_array\\_t](#).*
- void [resize\\_byte\\_array](#) ([byte\\_array\\_t](#) \*const array, [uint32\\_t](#) allocated)  
*Resizes the allocated memory of a [byte\\_array\\_t](#).*
- void [append\\_byte\\_to\\_array](#) ([byte\\_array\\_t](#) \*array, const unsigned char to\_append)  
*Appends a [uint32\\_t](#) to an [byte\\_array\\_t](#).*
- void [append\\_byte\\_array](#) ([byte\\_array\\_t](#) \*const array, const [byte\\_array\\_t](#) \*const to\_append)  
*Appends the content of a [byte\\_array\\_t](#) to another one.*
- void [swap\\_byte\\_array](#) ([byte\\_array\\_t](#) \*const a, [byte\\_array\\_t](#) \*const b)  
*Swaps two [byte\\_array\\_t](#)'s contents.*
- void [print\\_byte\\_array](#) (const [byte\\_array\\_t](#) \*const array)  
*Prints a [byte\\_array\\_t](#).*
- void [ins\\_sort\\_byte\\_array](#) ([byte\\_array\\_t](#) \*const array)  
*Sorts the elements of a [byte\\_array\\_t](#).*
- void [qsort\\_byte\\_array](#) ([byte\\_array\\_t](#) \*const array)  
*Sorts the elements of a [byte\\_array\\_t](#) with a quick sort.*
- [uint32\\_t index\\_in\\_byte\\_array](#) (unsigned char to\_find, const [byte\\_array\\_t](#) \*const array)  
*Returns the position of a byte in a [byte\\_array\\_t](#).*

- static bool `is_in_byte_array` (unsigned char to\_find, const `byte_array_t` \*const array)  
*Returns true if a given byte is in a given array.*
- `uint32_t index_in_sorted_byte_array` (unsigned char to\_find, const `byte_array_t` \*const sorted\_array, `uint32_t` min\_index, `uint32_t` max\_index)  
*Returns the position of an integer in a sorted portion of a `byte_array_t`.*
- static bool `is_in_sorted_byte_array` (unsigned char to\_find, const `byte_array_t` \*const array)  
*Returns true if a given byte is in a sorted `byte_array_t`.*
- `uint32_array_t * alloc_uint32_array` (`uint32_t` length)  
*Allocates and returns a new `uint32_array_t`.*
- void `free_uint32_array` (`uint32_array_t` \*array)  
*Frees a `uint32_array_t`.*
- void `resize_uint32_array` (`uint32_array_t` \*const array, `uint32_t` allocated)  
*Resizes the allocated memory of an `uint32_array_t`.*
- void `append_uint32_to_array` (`uint32_array_t` \*array, const `uint32_t` to\_append)  
*Appends a `uint32_t` to an `uint32_array_t`.*
- void `append_uint32_array` (`uint32_array_t` \*const array, const `uint32_array_t` \*const to\_append)  
*Appends the content of a `uint32_array_t` to another one.*
- void `swap_uint32_array` (`uint32_array_t` \*const a, `uint32_array_t` \*const b)  
*Swaps two `uint32_array_t`'s contents.*
- void `print_uint32_array` (const `uint32_array_t` \*const array)  
*Prints a `uint32_array_t`.*
- void `ins_sort_uint32_array` (`uint32_array_t` \*const array)  
*Sorts the `uint32_t` elements of a `uint32_array_t`.*
- void `qsort_uint32_array` (`uint32_array_t` \*const array)  
*Sorts the `uint32_t` elements of a `uint32_array_t` with a quick sort.*
- `uint32_t index_in_uint32_array` (`uint32_t` to\_find, const `uint32_array_t` \*const array)  
*Returns the position of an integer in a `uint32_array_t`.*
- static bool `is_in_uint32_array` (`uint32_t` to\_find, const `uint32_array_t` \*const array)  
*Returns true if a given integer is in a given array.*
- `uint32_t index_in_sorted_uint32_array` (`uint32_t` to\_find, const `uint32_array_t` \*const sorted\_array, `uint32_t` min\_index, `uint32_t` max\_index)  
*Returns the position of an integer in a sorted portion of a `uint32_array_t`.*
- static bool `is_in_sorted_uint32_array` (`uint32_t` to\_find, const `uint32_array_t` \*const array)  
*Returns true if a given integer is in a given array.*

- `int32_array_t * alloc_int32_array (uint32_t length)`  
*Allocates and returns a new int32\_array\_t.*
- `void free_int32_array (int32_array_t *array)`  
*Frees a int32\_array\_t.*
- `void resize_int32_array (int32_array_t *const array, uint32_t allocated)`  
*Resizes the allocated memory of an int32\_array\_t.*
- `void append_int32_to_array (int32_array_t *array, const int32_t to_append)`  
*Appends a int32\_t to an int32\_array\_t.*
- `void append_int32_array (int32_array_t *const array, const int32_array_t *const to_append)`  
*Appends the content of an int32\_array\_t to another one.*
- `void swap_int32_array (int32_array_t *const a, int32_array_t *const b)`  
*Swaps two int32\_array\_t's contents.*
- `void print_int32_array (const int32_array_t *const array)`  
*Prints a int32\_array\_t.*
- `uint32_t index_in_int32_array (int32_t to_find, const int32_array_t *const array)`  
*Returns the position of an integer in a int32\_array\_t.*
- `static bool is_in_int32_array (int32_t to_find, const int32_array_t *const array)`  
*Returns true if a given integer is in a given array.*
- `uint32_t index_in_sorted_int32_array (int32_t to_find, const int32_array_t *const sorted_array, uint32_t min_index, uint32_t max_index)`  
*Returns the position of an integer in a sorted portion of a int32\_array\_t.*
- `static bool is_in_sorted_int32_array (int32_t to_find, const int32_array_t *const array)`  
*Returns true if a given integer is in a given array.*
- `mpz_array_t * alloc_mpz_array (uint32_t length)`  
*Allocates and returns a new mpz\_array\_t.*
- `void free_mpz_array (mpz_array_t *array)`  
*Frees a mpz\_array\_t.*
- `void resize_mpz_array (mpz_array_t *const array, uint32_t allocated)`  
*Resizes the allocated memory of an mpz\_array\_t.*
- `void swap_mpz_array (mpz_array_t *const a, mpz_array_t *const b)`  
*Swaps two mpz\_array\_t's contents.*
- `void append_mpz_to_array (mpz_array_t *array, const mpz_t to_append)`  
*Appends an mpz\_t to an mpz\_array\_t.*
- `void append_mpz_array (mpz_array_t *const array, const mpz_array_t *const to_append)`

*Appends the content of an mpz\_array\_t to another one.*

- void [print\\_mpz\\_array](#) (const [mpz\\_array\\_t](#) \*const array)  
*Prints a mpz\_array\_t.*
- [uint32\\_t](#) [index\\_in\\_mpz\\_array](#) (const [mpz\\_t](#) to\_find, const [mpz\\_array\\_t](#) \*const array)  
*Returns the position of a mpz\_t in a mpz\_array\_t.*
- [uint32\\_t](#) [index\\_in\\_sorted\\_mpz\\_array](#) (const [mpz\\_t](#) to\_find, const [mpz\\_array\\_t](#) \*const sorted\_array, [uint32\\_t](#) min\_index, [uint32\\_t](#) max\_index)  
*Returns the position of an mpz\_t in a sorted portion of an mpz\_array\_t.*
- static bool [is\\_in\\_mpz\\_array](#) (const [mpz\\_t](#) to\_find, const [mpz\\_array\\_t](#) \*const array)  
*Returns true if a given integer is in a given array.*
- void [ins\\_sort\\_mpz\\_array](#) ([mpz\\_array\\_t](#) \*const array)  
*Sorts the mpz\_t elements of a mpz\_array\_t.*
- void [qsort\\_mpz\\_array](#) ([mpz\\_array\\_t](#) \*const array)  
*Sorts the mpz\_t elements of a mpz\_array\_t with a quick sort.*
- static bool [is\\_in\\_sorted\\_mpz\\_array](#) (const [mpz\\_t](#) to\_find, const [mpz\\_array\\_t](#) \*const array)  
*Returns true if a given integer is in a given array.*
- [binary\\_array\\_t](#) \* [alloc\\_binary\\_array](#) ([uint32\\_t](#) length)  
*Allocates and returns a new binary\_array\_t.*
- void [free\\_binary\\_array](#) ([binary\\_array\\_t](#) \*array)  
*Frees a binary\_array\_t.*
- void [resize\\_binary\\_array](#) ([binary\\_array\\_t](#) \*const array, [uint32\\_t](#) allocated)  
*Resizes the allocated memory of a binary\_array\_t.*
- void [append\\_bit\\_to\\_array](#) ([binary\\_array\\_t](#) \*array, const unsigned int to\_append)  
*Appends a bit to a binary\_array\_t.*
- void [print\\_binary\\_array](#) (const [binary\\_array\\_t](#) \*const array)  
*Prints a binary\_array\_t.*
- static [uint8\\_t](#) [get\\_array\\_bit](#) ([uint32\\_t](#) index, const [binary\\_array\\_t](#) \*const array)  
*Returns the value of a given bit in a binary\_array\_t.*
- static void [set\\_array\\_bit\\_to\\_one](#) ([uint32\\_t](#) index, [binary\\_array\\_t](#) \*const array)  
*Sets a given bit to one in a binary\_array\_t.*
- static void [set\\_array\\_bit\\_to\\_zero](#) ([uint32\\_t](#) index, [binary\\_array\\_t](#) \*const array)  
*Sets a given bit to zero in a binary\_array\_t.*
- static void [flip\\_array\\_bit](#) ([uint32\\_t](#) index, [binary\\_array\\_t](#) \*const array)  
*Flips a given bit to zero in a binary\_array\_t.*

### 5.2.1 Detailed Description

Higher level arrays and associated functions.

**Author:**

Jerome Milan

**Date:**

Fri Jun 10 2011

**Version:**

2011-06-10

This file defines higher level arrays together with some associated functions.

The `*_array_t` types and their associated functions are quite similar, the only differences being the type of the elements these arrays hold. Each `*_array_t` type is a structure composed of three fields:

- `allocated` - The maximum number of element the array can accomodate
- `length` - The current number of element in the array
- `data` - A pointer to the allocated memory space of `allocated` elements

**Warning:**

Since version 1.2.1 memory management changed. See the `alloc*_array` and `clear*_array` functions for more information.

Definition in file [array.h](#).

### 5.2.2 Define Documentation

#### 5.2.2.1 `#define _TIFA_ARRAY_H_`

Standard include guard.

Definition at line 47 of file `array.h`.

#### 5.2.2.2 `#define ARRAY_IS_FULL(ARRAY_PTR) ((ARRAY_PTR) → length == (ARRAY_PTR) → allocated)`

Returns true if the `*_array_t` pointed by `ARRAY_PTR` is full (i.e. no more element can be added to the array without resizing it).

Returns false otherwise.

Definition at line 84 of file `array.h`.

#### 5.2.2.3 `#define ELONGATION 16`

Incremental size used when automatically expanding the capacity of a `*_array_t`.

**Note:**

This is, of course, an hint to GMP's limbs and nails :-)

Definition at line 68 of file `array.h`.

#### 5.2.2.4 #define NOT\_IN\_ARRAY UINT32\_MAX

Value returned by the `index_in*_array(x, array, ...)` functions if the element `x` is not in the array `array`.

Definition at line 75 of file `array.h`.

Referenced by `is_in_byte_array()`, `is_in_int32_array()`, `is_in_mpz_array()`, `is_in_sorted_byte_array()`, `is_in_sorted_int32_array()`, `is_in_sorted_mpz_array()`, `is_in_sorted_uint32_array()`, and `is_in_uint32_array()`.

#### 5.2.2.5 #define reset\_binary\_array(ARRAY) do {(ARRAY) → length = 0;} while (0)

Resets a `binary_array_t`.

Resets the `length` field of `array` to zero.

Note that its `allocated` field is left unchanged and that memory for `allocated * CHAR_BIT * sizeof(TIFA_BITSTRING_T)` bits is still allocated.

##### Parameters:

← `array` A pointer to the `binary_array_t` to reset.

Definition at line 1197 of file `array.h`.

#### 5.2.2.6 #define reset\_byte\_array(ARRAY) do {(ARRAY) → length = 0;} while (0)

Resets a `byte_array_t`.

Resets the `length` field of `array` to zero.

Note that its `allocated` field is left unchanged and that memory for `allocated byte_t` elements is still allocated.

##### Parameters:

← `array` A pointer to the `byte_array_t` to reset.

Definition at line 163 of file `array.h`.

#### 5.2.2.7 #define reset\_int32\_array(ARRAY) do {(ARRAY) → length = 0;} while (0)

Resets an `int32_array_t`.

Resets the `length` field of `array` to zero.

Note that its `allocated` field is left unchanged and that memory for `allocated int32_t` elements is still allocated.

##### Parameters:

← `array` A pointer to the `int32_array_t` to reset.

Definition at line 683 of file `array.h`.

### 5.2.2.8 #define reset\_mpz\_array(ARRAY) do {(ARRAY) → length = 0;} while (0)

Resets an `mpz_array_t`.

Resets the `length` field of `array` to zero.

Note that its `allocated` field is left unchanged and that memory for allocated `mpz_t` elements is still allocated (all the elements remaining fully `mpz_init'`ed).

#### Warning:

Prior to 1.2 when the semantic was different, this function used to `mpz_clear` all positions in `array->data`. This is no longer true.

#### Parameters:

← *array* A pointer to the `mpz_array_t` to clear.

Definition at line 934 of file `array.h`.

### 5.2.2.9 #define reset\_uint32\_array(ARRAY) do {(ARRAY) → length = 0;} while (0)

Resets a `uint32_array_t`.

Resets the `length` field of `array` to zero.

Note that its `allocated` field is left unchanged and that memory for allocated `uint32_t` elements is still allocated.

#### Parameters:

← *array* A pointer to the `uint32_array_t` to reset.

Definition at line 423 of file `array.h`.

## 5.2.3 Function Documentation

### 5.2.3.1 binary\_array\_t\* alloc\_binary\_array (uint32\_t length)

Allocates and returns a new `binary_array_t`.

Allocates and returns a new `binary_array_t` such that:

- its `allocated` field is set to the minimum number of `TIFA_BITSTRING_T` variables needed to store `length` bits.
- its `length` field is set to zero.
- its `data` array is completely filled with zeroes.

#### Parameters:

← *length* The maximum bitlength of the `uint32_array_t` to allocate.

#### Returns:

A pointer to the newly allocated `uint32_array_t` structure. Note that this array may hold more than `length` bits if `length` is not a multiple of `8 * sizeof(TIFA_BITSTRING_T)`.



### 5.2.3.2 `byte_array_t*` `alloc_byte_array (uint32_t length)`

Allocates and returns a new `byte_array_t`.

Allocates and returns a new `byte_array_t` such that:

- its `allocated` field is set to the parameter length.
- its `length` field is set to zero.
- its `data` array is completely filled with zeroes.

#### Parameters:

← *length* The maximum length of the `byte_array_t` to allocate.

#### Returns:

A pointer to the newly allocated `byte_array_t` structure.

### 5.2.3.3 `int32_array_t*` `alloc_int32_array (uint32_t length)`

Allocates and returns a new `int32_array_t`.

Allocates and returns a new `int32_array_t` such that:

- its `allocated` field is set to the parameter length.
- its `length` field is set to zero.
- its `data` array is completely filled with zeroes.

#### Parameters:

← *length* The maximum length of the `int32_array_t` to allocate.

#### Returns:

A pointer to the newly allocated `int32_array_t` structure.

### 5.2.3.4 `mpz_array_t*` `alloc_mpz_array (uint32_t length)`

Allocates and returns a new `mpz_array_t`.

Allocates and returns a new `mpz_array_t` such that:

- its `allocated` field is set to the parameter length.
- its `length` field is set to zero.
- its `data` array is fully `mpz_init'`ed.

#### Parameters:

← *length* The maximum length of the `mpz_array_t` to allocate.

#### Returns:

A pointer to the newly allocated `mpz_array_t` structure.

**Warning:**

Since version 1.2, the `data` field is completely `mpz_init`'ed (from `data[0]` to `data[allocated - 1]`) whereas older versions did not `mpz_init` anything. This change in behaviour was prompted by the need to avoid multiple memory deallocations and reallocations when using the same `mpz_array_t` repeatedly.

**5.2.3.5 uint32\_array\_t\* alloc\_uint32\_array (uint32\_t length)**

Allocates and returns a new `uint32_array_t`.

Allocates and returns a new `uint32_array_t` such that:

- its `allocated` field is set to the parameter `length`.
- its `length` field is set to zero.
- its `data` array is completely filled with zeroes.

**Parameters:**

← *length* The maximum length of the `uint32_array_t` to allocate.

**Returns:**

A pointer to the newly allocated `uint32_array_t` structure.

**5.2.3.6 void append\_bit\_to\_array (binary\_array\_t \* array, const unsigned int to\_append)**

Appends a bit to a `binary_array_t`.

Appends a bit (set to one if `to_append != 0`, set to zero otherwise) to `array`. If `array` has not enough capacity to accommodate this extra element it will be resized via a call to `resize_binary_array` adding `ELONGATION * BITSTRING_T_BITSIZE` bit slots to avoid too frequent resizes.

**Parameters:**

- ← *array* A pointer to the recipient `binary_array_t`.
- ← *to\_append* The bit to append (1 if `to_append != 0`, 0 otherwise).

**5.2.3.7 void append\_byte\_array (byte\_array\_t \*const array, const byte\_array\_t \*const to\_append)**

Appends the content of a `byte_array_t` to another one.

Appends the content of the `to_append` array to the `byte_array_t` named `array`. If `array` has not enough capacity to accommodate all elements from `to_append`, it will be resized via a call to `resize_byte_array` with extra room for `ELONGATION` unused slots to avoid too frequent resizes.

**Parameters:**

- ← *array* A pointer to the recipient `byte_array_t`.
- ← *to\_append* A pointer to the `byte_array_t` to append.

**5.2.3.8 void append\_byte\_to\_array (byte\_array\_t \*array, const unsigned char to\_append)**

Appends a uint32\_t to an byte\_array\_t.

Appends the byte to\_append to array. If array has not enough capacity to accommodate this extra element it will be resized via a call to resize\_byte\_array adding ELONGATION byte slots to avoid too frequent resizes.

**Parameters:**

- ← *array* A pointer to the recipient byte\_array\_t.
- ← *to\_append* The byte to append.

**5.2.3.9 void append\_int32\_array (int32\_array\_t \*const array, const int32\_array\_t \*const to\_append)**

Appends the content of an int32\_array\_t to another one.

Appends the content of the to\_append array to the int32\_array\_t named array. If array has not enough capacity to accommodate all elements from to\_append, it will be resized via a call to resize\_int32\_array with extra room for ELONGATION unused int32\_t slots to avoid too frequent resizes.

**Parameters:**

- ← *array* A pointer to the recipient int32\_array\_t.
- ← *to\_append* A pointer to the int32\_array\_t to append.

**5.2.3.10 void append\_int32\_to\_array (int32\_array\_t \*array, const int32\_t to\_append)**

Appends a int32\_t to an int32\_array\_t.

Appends the int32\_t integer to\_append to array. If array has not enough capacity to accommodate this extra element it will be resized via a call to resize\_int32\_array adding ELONGATION int32\_t slots to avoid too frequent resizes.

**Parameters:**

- ← *array* A pointer to the recipient int32\_array\_t.
- ← *to\_append* The integer to append.

**5.2.3.11 void append\_mpz\_array (mpz\_array\_t \*const array, const mpz\_array\_t \*const to\_append)**

Appends the content of an mpz\_array\_t to another one.

Appends the content of the to\_append array to the mpz\_array\_t named array. If array has not enough capacity to accommodate all elements from to\_append, it will be resized via a call to resize\_mpz\_array with extra room for ELONGATION unused mpz\_t slots to avoid too frequent resizes.

**Parameters:**

- ← *array* A pointer to the recipient mpz\_array\_t.
- ← *to\_append* A pointer to the mpz\_array\_t to append.

**5.2.3.12 void append\_mpz\_to\_array (mpz\_array\_t \*array, const mpz\_t to\_append)**

Appends an `mpz_t` to an `mpz_array_t`.

Appends the `mpz_t` integer `to_append` to `array`. If `array` has not enough capacity to accommodate this extra element it will be resized via a call to `resize_mpz_array` adding `ELONGATION` `mpz_t` slots to avoid too frequent resizes.

**Parameters:**

- ← *array* A pointer to the recipient `mpz_array_t`.
- ← *to\_append* The `mpz_t` to append.

**5.2.3.13 void append\_uint32\_array (uint32\_array\_t \*const array, const uint32\_array\_t \*const to\_append)**

Appends the content of a `uint32_array_t` to another one.

Appends the content of the `to_append` array to the `uint32_array_t` named `array`. If `array` has not enough capacity to accommodate all elements from `to_append`, it will be resized via a call to `resize_uint32_array` with extra room for `ELONGATION` unused `uint32_t` slots to avoid too frequent resizes.

**Parameters:**

- ← *array* A pointer to the recipient `uint32_array_t`.
- ← *to\_append* A pointer to the `uint32_array_t` to append.

**5.2.3.14 void append\_uint32\_to\_array (uint32\_array\_t \*array, const uint32\_t to\_append)**

Appends a `uint32_t` to an `uint32_array_t`.

Appends the `uint32_t` integer `to_append` to `array`. If `array` has not enough capacity to accommodate this extra element it will be resized via a call to `resize_uint32_array` adding `ELONGATION` `uint32_t` slots to avoid too frequent resizes.

**Parameters:**

- ← *array* A pointer to the recipient `uint32_array_t`.
- ← *to\_append* The integer to append.

**5.2.3.15 static void flip\_array\_bit (uint32\_t index, binary\_array\_t \*const array) [inline, static]**

Flips a given bit to zero in a `binary_array_t`.

Flips the `index`-th bit of the `binary_array_t` pointed to by `array`.

**Parameters:**

- ← *index* The position of the bit to flip.
- ← *array* A pointer to the `binary_array_t`.

Definition at line 1318 of file `array.h`.

References `struct_binary_array_t::data`.

**5.2.3.16 void free\_binary\_array (binary\_array\_t \* array)**

Frees a `binary_array_t`.

Frees the `binary_array_t` pointed to by `array`, *i.e.* frees the memory space used by the C-style array pointed by `array->data` and frees the `array` pointer.

**Warning:**

Before version 1.2.1, the `array` pointer was not freed which required explicit calls to `free(...)` in client code.

**Parameters:**

← `array` A pointer to the `binary_array_t` to clear.

**5.2.3.17 void free\_byte\_array (byte\_array\_t \* array)**

Frees a `byte_array_t`.

Frees the `byte_array_t` pointed to by `array`, *i.e.* frees the memory space used by the C-style array pointed by `array->data` and frees the `array` pointer.

**Warning:**

Before version 1.2.1, the `array` pointer was not freed which required explicit calls to `free(...)` in client code.

**Parameters:**

← `array` A pointer to the `byte_array_t` to clear.

**5.2.3.18 void free\_int32\_array (int32\_array\_t \* array)**

Frees a `int32_array_t`.

Frees the `int32_array_t` pointed to by `array`, *i.e.* frees the memory space used by the C-style array pointed by `array->data` and frees the `array` pointer.

**Warning:**

Before version 1.2.1, the `array` pointer was not freed which required explicit calls to `free(...)` in client code.

**Parameters:**

← `array` A pointer to the `int32_array_t` to clear.

**5.2.3.19 void free\_mpz\_array (mpz\_array\_t \* array)**

Frees a `mpz_array_t`.

Frees the `mpz_array_t` pointed to by `array`, *i.e.* frees the memory space used by the C-style array pointed by `array->data` and frees the `array` pointer.

**Warning:**

Before version 1.2.1, the `array` pointer was not freed which required explicit calls to `free(...)` in client code.

**Parameters:**

← *array* A pointer to the `mpz_array_t` to clear.

**5.2.3.20 void free\_uint32\_array (uint32\_array\_t \* array)**

Frees a `uint32_array_t`.

Frees the `uint32_array_t` pointed to by `array`, *i.e.* frees the memory space used by the C-style array pointed by `array->data` and frees the `array` pointer.

**Warning:**

Before version 1.2.1, the `array` pointer was not freed which required explicit calls to `free(...)` in client code.

**Parameters:**

← *array* A pointer to the `uint32_array_t` to clear.

**5.2.3.21 static uint8\_t get\_array\_bit (uint32\_t index, const binary\_array\_t \*const array)**  
[inline, static]

Returns the value of a given bit in a `binary_array_t`.

Returns the value of the `index`-th bit of the `binary_array_t` pointed to by `array`, as either 0 or 1.

**Parameters:**

← *index* The position of the bit to read.

← *array* A pointer to the `binary_array_t`.

**Returns:**

The value of the `index`-th bit: either 0 or 1.

Definition at line 1248 of file `array.h`.

References `struct_binary_array_t::data`.

**5.2.3.22 uint32\_t index\_in\_byte\_array (unsigned char to\_find, const byte\_array\_t \*const array)**

Returns the position of a byte in a `byte_array_t`.

Returns the position of the byte `to_find` in the `byte_array_t` pointed to by `array`. If the byte `to_find` is not found in the `byte_array_t`, returns `NOT_IN_ARRAY`.

**Note:**

The `NOT_IN_ARRAY` value is actually -1 if interpreted as a signed `int32_t`.

If the array is already sorted, the more efficient function `index_in_sorted_byte_array` can be used as it uses a basic binary search instead of a complete scanning of the array.

**Parameters:**

- ← *to\_find* The byte to find in the `byte_array_t`.
- ← *array* A pointer to the `byte_array_t`.

**Returns:**

The index of `to_find` in the array if `to_find` is found.  
`NOT_IN_ARRAY` otherwise.

Referenced by `is_in_byte_array()`.

**5.2.3.23 uint32\_t index\_in\_int32\_array (int32\_t to\_find, const int32\_array\_t \*const array)**

Returns the position of an integer in a `int32_array_t`.

Returns the position of the integer `to_find` in the `int32_array_t` pointed to by `array`. If the integer `to_find` is not found in the `int32_array_t`, returns `NOT_IN_ARRAY`.

**Note:**

The `NOT_IN_ARRAY` value is actually -1 if interpreted as a signed `int32_t`.  
If the array is already sorted, the more efficient function `index_in_sorted_int32_array` can be used as it uses a basic binary search instead of a complete scanning of the array.

**Parameters:**

- ← *to\_find* The integer to find in the `int32_array_t`.
- ← *array* A pointer to the `int32_array_t`.

**Returns:**

The index of `to_find` in the array if `to_find` is found.  
`NOT_IN_ARRAY` otherwise.

Referenced by `is_in_int32_array()`.

**5.2.3.24 uint32\_t index\_in\_mpz\_array (const mpz\_t to\_find, const mpz\_array\_t \*const array)**

Returns the position of a `mpz_t` in a `mpz_array_t`.

Returns the position of the `mpz_t` `to_find` in the `mpz_array_t` pointed to by `array`. If the integer `to_find` is not found in the `mpz_array_t`, returns `NOT_IN_ARRAY`.

**Note:**

The `NOT_IN_ARRAY` value is actually -1 if interpreted as a signed `int32_t`.

**Parameters:**

- ← *to\_find* The `mpz_t` integer to find in the `mpz_array_t`.
- ← *array* A pointer to the `mpz_array_t`.

**Returns:**

The index of `to_find` in the array if `to_find` is found.  
`NOT_IN_ARRAY` otherwise.

Referenced by `is_in_mpz_array()`.

### 5.2.3.25 `uint32_t index_in_sorted_byte_array (unsigned char to_find, const byte_array_t *const sorted_array, uint32_t min_index, uint32_t max_index)`

Returns the position of an integer in a sorted portion of a `byte_array_t`.

Returns the position of the byte `to_find` in a *sorted* portion of the `byte_array_t` pointed to by `array`. If the byte `to_find` is not found in the portion delimited by `min_index` and `max_index`, returns `NOT_IN_ARRAY`.

#### Note:

The `NOT_IN_ARRAY` value is actually -1 if interpreted as a signed `int32_t`.

#### Parameters:

- ← *to\_find* The byte to find in the `byte_array_t`.
- ← *sorted\_array* A pointer to the `byte_array_t`.
- ← *min\_index* The beginning of the sorted array portion to search in.
- ← *max\_index* The end of the sorted array portion to search in.

#### Returns:

The index of `to_find` in the array if `to_find` is found in the sorted array portion.  
`NOT_IN_ARRAY` otherwise.

Referenced by `is_in_sorted_byte_array()`.

### 5.2.3.26 `uint32_t index_in_sorted_int32_array (int32_t to_find, const int32_array_t *const sorted_array, uint32_t min_index, uint32_t max_index)`

Returns the position of an integer in a sorted portion of a `int32_array_t`.

Returns the position of the integer `to_find` in a *sorted* portion of the `int32_array_t` pointed to by `array`. If the integer `to_find` is not found in the portion delimited by `min_index` and `max_index`, returns `NOT_IN_ARRAY`.

#### Note:

The `NOT_IN_ARRAY` value is actually -1 if interpreted as a signed `int32_t`.

#### Parameters:

- ← *to\_find* The integer to find in the `int32_array_t`.
- ← *sorted\_array* A pointer to the `int32_array_t`.
- ← *min\_index* The beginning of the sorted array portion to search in.
- ← *max\_index* The end of the sorted array portion to search in.

#### Returns:

The index of `to_find` in the array if `to_find` is found in the sorted array portion.  
`NOT_IN_ARRAY` otherwise.

Referenced by `is_in_sorted_int32_array()`.



**5.2.3.27 uint32\_t index\_in\_sorted\_mpz\_array (const mpz\_t to\_find, const mpz\_array\_t \*const sorted\_array, uint32\_t min\_index, uint32\_t max\_index)**

Returns the position of an mpz\_t in a *sorted* portion of an mpz\_array\_t.

Returns the position of the mpz\_t to\_find in the *sorted* portion of the mpz\_array\_t pointed to by array. If the integer to\_find is not found in this portion, returns NOT\_IN\_ARRAY.

**Note:**

The NOT\_IN\_ARRAY value is actually -1 if interpreted as a signed int32\_t.

**Parameters:**

- ← *to\_find* The mpz\_t integer to find in the mpz\_array\_t.
- ← *sorted\_array* A pointer to the *sorted* mpz\_array\_t.
- ← *min\_index* The beginning of the sorted array portion to search in.
- ← *max\_index* The end of the sorted array portion to search in.

**Returns:**

The index of to\_find in the array if to\_find is found.  
NOT\_IN\_ARRAY otherwise.

Referenced by is\_in\_sorted\_mpz\_array().

**5.2.3.28 uint32\_t index\_in\_sorted\_uint32\_array (uint32\_t to\_find, const uint32\_array\_t \*const sorted\_array, uint32\_t min\_index, uint32\_t max\_index)**

Returns the position of an integer in a sorted portion of a uint32\_array\_t.

Returns the position of the integer to\_find in a *sorted* portion of the uint32\_array\_t pointed to by array. If the integer to\_find is not found in the portion delimited by min\_index and max\_index, returns NOT\_IN\_ARRAY.

**Note:**

The NOT\_IN\_ARRAY value is actually -1 if interpreted as a signed int32\_t.

**Parameters:**

- ← *to\_find* The integer to find in the uint32\_array\_t.
- ← *sorted\_array* A pointer to the uint32\_array\_t.
- ← *min\_index* The beginning of the sorted array portion to search in.
- ← *max\_index* The end of the sorted array portion to search in.

**Returns:**

The index of to\_find in the array if to\_find is found in the sorted array portion.  
NOT\_IN\_ARRAY otherwise.

Referenced by is\_in\_sorted\_uint32\_array().

**5.2.3.29 uint32\_t index\_in\_uint32\_array (uint32\_t to\_find, const uint32\_array\_t \*const array)**

Returns the position of an integer in a `uint32_array_t`.

Returns the position of the integer `to_find` in the `uint32_array_t` pointed to by `array`. If the integer `to_find` is not found in the `uint32_array_t`, returns `NOT_IN_ARRAY`.

**Note:**

The `NOT_IN_ARRAY` value is actually -1 if interpreted as a signed `int32_t`.  
If the array is already sorted, the more efficient function `index_in_sorted_uint32_array` can be used as it uses a basic binary search instead of a complete scanning of the array.

**Parameters:**

- ← *to\_find* The integer to find in the `uint32_array_t`.
- ← *array* A pointer to the `uint32_array_t`.

**Returns:**

The index of `to_find` in the array if `to_find` is found.  
`NOT_IN_ARRAY` otherwise.

Referenced by `is_in_uint32_array()`.

**5.2.3.30 void ins\_sort\_byte\_array (byte\_array\_t \*const array)**

Sorts the elements of a `byte_array_t`.

Sorts the elements of a `byte_array_t` in natural order using a basic insertion sort.

**Parameters:**

- ← *array* A pointer to the `byte_array_t` to sort.

**5.2.3.31 void ins\_sort\_mpz\_array (mpz\_array\_t \*const array)**

Sorts the `mpz_t` elements of a `mpz_array_t`.

Sorts the `mpz_t` elements of a `mpz_array_t` in natural order using a basic insertion sort.

**Parameters:**

- ← *array* A pointer to the `mpz_array_t` to sort.

**5.2.3.32 void ins\_sort\_uint32\_array (uint32\_array\_t \*const array)**

Sorts the `uint32_t` elements of a `uint32_array_t`.

Sorts the `uint32_t` elements of a `uint32_array_t` in natural order using a basic insertion sort.

**Parameters:**

- ← *array* A pointer to the `uint32_array_t` to sort.

**5.2.3.33** `static bool is_in_byte_array (unsigned char to_find, const byte_array_t *const array)`  
[inline, static]

Returns true if a given byte is in a given array.

Returns true if the byte `to_find` is in the `byte_array_t` pointed to by `array`. Returns false otherwise.

**Note:**

If the array is already sorted, the more efficient function `is_in_sorted_byte_array` can be used as it uses a basic binary search instead of a complete scanning of the array.

**Parameters:**

- ← *to\_find* The integer to find in the `byte_array_t`.
- ← *array* A pointer to the `byte_array_t`.

**Returns:**

- true if `to_find` is in the array `array`.
- false otherwise.

Definition at line 296 of file `array.h`.

References `index_in_byte_array()`, and `NOT_IN_ARRAY`.

**5.2.3.34** `static bool is_in_int32_array (int32_t to_find, const int32_array_t *const array)`  
[inline, static]

Returns true if a given integer is in a given array.

Returns true if the integer `to_find` is in the `int32_array_t` pointed to by `array`. Returns false otherwise.

**Note:**

If the array is already sorted, the more efficient function `is_in_sorted_int32_array` can be used as it uses a basic binary search instead of a complete scanning of the array.

**Parameters:**

- ← *to\_find* The integer to find in the `int32_array_t`.
- ← *array* A pointer to the `int32_array_t`.

**Returns:**

- true if `to_find` is in the array `array`.
- false otherwise.

Definition at line 792 of file `array.h`.

References `index_in_int32_array()`, and `NOT_IN_ARRAY`.

**5.2.3.35** `static bool is_in_mpz_array (const mpz_t to_find, const mpz_array_t *const array)`  
[inline, static]

Returns true if a given integer is in a given array.

Returns true if the `mpz_t` integer `to_find` is in the `mpz_array_t` pointed to by `array`. Returns false otherwise.

**Note:**

If the array is already sorted, the more efficient function `is_in_sorted_mpz_array` can be used as it uses a basic binary search instead of a complete scanning of the array.

**Parameters:**

- ← *to\_find* The integer to find in the `mpz_array_t`.
- ← *array* A pointer to the `mpz_array_t`.

**Returns:**

true if `to_find` is in the array `array`.  
false otherwise.

Definition at line 1062 of file `array.h`.

References `index_in_mpz_array()`, and `NOT_IN_ARRAY`.

**5.2.3.36 static bool is\_in\_sorted\_byte\_array (unsigned char to\_find, const byte\_array\_t \*const array) [inline, static]**

Returns true if a given byte is in a sorted `byte_array_t`.

Returns true if the byte `to_find` is in the (*already sorted*) `byte_array_t` pointed to by `array`.  
Returns false otherwise.

**Parameters:**

- ← *to\_find* The byte to find in the `byte_array_t`.
- ← *array* A pointer to the *sorted* `byte_array_t`.

**Returns:**

true if `to_find` is in the array `array`.  
false otherwise.

Definition at line 337 of file `array.h`.

References `index_in_sorted_byte_array()`, `struct_byte_array_t::length`, and `NOT_IN_ARRAY`.

**5.2.3.37 static bool is\_in\_sorted\_int32\_array (int32\_t to\_find, const int32\_array\_t \*const array) [inline, static]**

Returns true if a given integer is in a given array.

Returns true if the integer `to_find` is in the (*already sorted*) `int32_array_t` pointed to by `array`.  
Returns false otherwise.

**Parameters:**

- ← *to\_find* The integer to find in the `int32_array_t`.
- ← *array* A pointer to the *sorted* `int32_array_t`.

**Returns:**

true if `to_find` is in the array `array`.  
false otherwise.

Definition at line 833 of file array.h.

References `index_in_sorted_int32_array()`, `struct_int32_array_t::length`, and `NOT_IN_ARRAY`.

**5.2.3.38** `static bool is_in_sorted_mpz_array (const mpz_t to_find, const mpz_array_t *const array)`  
[inline, static]

Returns true if a given integer is in a given array.

Returns true if the `mpz_t` integer `to_find` is in the `mpz_array_t` pointed to by `array`. Returns false otherwise.

**Parameters:**

- ← *to\_find* The integer to find in the `mpz_array_t`.
- ← *array* A pointer to the *sorted* `mpz_array_t`.

**Returns:**

- true if `to_find` is in the array `array`.
- false otherwise.

Definition at line 1102 of file array.h.

References `index_in_sorted_mpz_array()`, `struct_mpz_array_t::length`, and `NOT_IN_ARRAY`.

**5.2.3.39** `static bool is_in_sorted_uint32_array (uint32_t to_find, const uint32_array_t *const array)`  
[inline, static]

Returns true if a given integer is in a given array.

Returns true if the integer `to_find` is in the (*already sorted*) `uint32_array_t` pointed to by `array`. Returns false otherwise.

**Parameters:**

- ← *to\_find* The integer to find in the `uint32_array_t`.
- ← *array* A pointer to the *sorted* `uint32_array_t`.

**Returns:**

- true if `to_find` is in the array `array`.
- false otherwise.

Definition at line 598 of file array.h.

References `index_in_sorted_uint32_array()`, `struct_uint32_array_t::length`, and `NOT_IN_ARRAY`.

**5.2.3.40** `static bool is_in_uint32_array (uint32_t to_find, const uint32_array_t *const array)`  
[inline, static]

Returns true if a given integer is in a given array.

Returns true if the integer `to_find` is in the `uint32_array_t` pointed to by `array`. Returns false otherwise.

**Note:**

If the array is already sorted, the more efficient function `is_in_sorted_uint32_array` can be used as it uses a basic binary search instead of a complete scanning of the array.

**Parameters:**

- ← *to\_find* The integer to find in the `uint32_array_t`.
- ← *array* A pointer to the `uint32_array_t`.

**Returns:**

- true if `to_find` is in the array `array`.
- false otherwise.

Definition at line 557 of file `array.h`.

References `index_in_uint32_array()`, and `NOT_IN_ARRAY`.

**5.2.3.41 void print\_binary\_array (const binary\_array\_t \*const array)**

Prints a `binary_array_t`.

Prints a `binary_array_t`'s on the standard output.

**Parameters:**

- ← *array* A pointer to the `binary_array_t` to print.

**5.2.3.42 void print\_byte\_array (const byte\_array\_t \*const array)**

Prints a `byte_array_t`.

Prints a `byte_array_t`'s data elements on the standard output.

**Note:**

This function is mostly intended for debugging purposes as the output is not particularly well structured.

**Parameters:**

- ← *array* A pointer to the `byte_array_t` to print.

**5.2.3.43 void print\_int32\_array (const int32\_array\_t \*const array)**

Prints a `int32_array_t`.

Prints a `int32_array_t`'s data elements on the standard output.

**Note:**

This function is mostly intended for debugging purposes as the output is not particularly well structured.

**Parameters:**

- ← *array* A pointer to the `int32_array_t` to print.

**5.2.3.44 void print\_mpz\_array (const mpz\_array\_t \*const array)**

Prints a `mpz_array_t`.

Prints a `mpz_array_t`'s data elements on the standard output.

**Note:**

This function is mostly intended for debugging purposes as the output is not particularly well structured.

**Parameters:**

← *array* A pointer to the `mpz_array_t` to print.

**5.2.3.45 void print\_uint32\_array (const uint32\_array\_t \*const array)**

Prints a `uint32_array_t`.

Prints a `uint32_array_t`'s data elements on the standard output.

**Note:**

This function is mostly intended for debugging purposes as the output is not particularly well structured.

**Parameters:**

← *array* A pointer to the `uint32_array_t` to print.

**5.2.3.46 void qsort\_byte\_array (byte\_array\_t \*const array)**

Sorts the elements of a `byte_array_t` with a quick sort.

Sorts the elements of a `byte_array_t` in natural order using the quick sort algorithm.

**Note:**

This function relies on the C library implementation of the quick sort provided by the function `qsort`.

**Parameters:**

← *array* A pointer to the `byte_array_t` to sort.

**5.2.3.47 void qsort\_mpz\_array (mpz\_array\_t \*const array)**

Sorts the `mpz_t` elements of a `mpz_array_t` with a quick sort.

Sorts the `mpz_t` elements of a `mpz_array_t` in natural order using the quick sort algorithm.

**Note:**

This function relies on the C library implementation of the quick sort provided by the function `qsort`.

**Parameters:**

← *array* A pointer to the `mpz_array_t` to sort.

**5.2.3.48 void qsort\_uint32\_array (uint32\_array\_t \*const array)**

Sorts the uint32\_t elements of a uint32\_array\_t with a quick sort.

Sorts the uint32\_t elements of a uint32\_array\_t in natural order using the quick sort algorithm.

**Note:**

This function relies on the C library implementation of the quick sort provided by the function `qsort`.

**Parameters:**

← *array* A pointer to the uint32\_array\_t to sort.

**5.2.3.49 void resize\_binary\_array (binary\_array\_t \*const array, uint32\_t allocated)**

Resizes the allocated memory of a binary\_array\_t.

Resizes the storage available to an binary\_array\_t to make room for `allocated` integers, while preserving its content. If `allocated` is less than the length of the array, then obviously some of its content will be lost.

**Parameters:**

← *allocated* The new maximum length of the binary\_array\_t to resize.

← *array* A pointer to the binary\_array\_t to resize.

**5.2.3.50 void resize\_byte\_array (byte\_array\_t \*const array, uint32\_t allocated)**

Resizes the allocated memory of a byte\_array\_t.

Resizes the storage available to an byte\_array\_t to make room for `allocated` integers, while preserving its content. If `allocated` is less than the length of the array, then obviously some of its content will be lost.

**Parameters:**

← *allocated* The new maximum length of the byte\_array\_t to resize.

← *array* A pointer to the byte\_array\_t to resize.

**5.2.3.51 void resize\_int32\_array (int32\_array\_t \*const array, uint32\_t allocated)**

Resizes the allocated memory of an int32\_array\_t.

Resizes the storage available to an int32\_array\_t to make room for `allocated` integers, while preserving its content. If `allocated` is less than the length of the array, then obviously some of its content will be lost.

**Parameters:**

← *allocated* The new maximum length of the int32\_array\_t to resize.

← *array* A pointer to the int32\_array\_t to resize.



**5.2.3.52 void `resize_mpz_array` (`mpz_array_t` \*const `array`, `uint32_t` `allocated`)**

Resizes the allocated memory of an `mpz_array_t`.

Resizes the storage available to an `mpz_array_t` to make room for `allocated` integers, while preserving its content. If `allocated` is less than the length of the array, then obviously some of its content will be freed and lost.

**Parameters:**

- ← *allocated* The new maximum length of the `mpz_array_t` to resize.
- ← *array* A pointer to the `mpz_array_t` to resize.

**5.2.3.53 void `resize_uint32_array` (`uint32_array_t` \*const `array`, `uint32_t` `allocated`)**

Resizes the allocated memory of an `uint32_array_t`.

Resizes the storage available to an `uint32_array_t` to make room for `allocated` integers, while preserving its content. If `allocated` is less than the length of the array, then obviously some of its content will be lost.

**Parameters:**

- ← *allocated* The new maximum length of the `uint32_array_t` to resize.
- ← *array* A pointer to the `uint32_array_t` to resize.

**5.2.3.54 static void `set_array_bit_to_one` (`uint32_t` `index`, `binary_array_t` \*const `array`)**  
[inline, static]

Sets a given bit to one in a `binary_array_t`.

Sets the `index`-th bit of the `binary_array_t` pointed to by `array` to 1.

**Parameters:**

- ← *index* The position of the bit to set.
- ← *array* A pointer to the `binary_array_t`.

Definition at line 1274 of file `array.h`.

References `struct_binary_array_t::data`.

**5.2.3.55 static void `set_array_bit_to_zero` (`uint32_t` `index`, `binary_array_t` \*const `array`)**  
[inline, static]

Sets a given bit to zero in a `binary_array_t`.

Sets the `index`-th bit of the `binary_array_t` pointed to by `array` to 0.

**Parameters:**

- ← *index* The position of the bit to set.
- ← *array* A pointer to the `binary_array_t`.

Definition at line 1296 of file `array.h`.

References `struct_binary_array_t::data`.

**5.2.3.56 void swap\_byte\_array (byte\_array\_t \*const a, byte\_array\_t \*const b)**

Swaps two `byte_array_t`'s contents.

Swaps the contents of `a` and `b`, two `byte_array_t`'s.

**Note:**

In some case, pointer swapping is inappropriate (for example, if the pointers are passed as function arguments!), hence the need for such a swapping function.

**Parameters:**

← *a* A pointer to the first `byte_array_t` to swap.

← *b* A pointer to the second `byte_array_t` to swap.

**5.2.3.57 void swap\_int32\_array (int32\_array\_t \*const a, int32\_array\_t \*const b)**

Swaps two `int32_array_t`'s contents.

Swaps the contents of `a` and `b`, two `int32_array_t`'s.

**Note:**

In some case, pointer swapping is inappropriate (for example, if the pointers are passed as function arguments!), hence the need for such a swapping function.

**Parameters:**

← *a* A pointer to the first `int32_array_t` to swap.

← *b* A pointer to the second `int32_array_t` to swap.

**5.2.3.58 void swap\_mpz\_array (mpz\_array\_t \*const a, mpz\_array\_t \*const b)**

Swaps two `mpz_array_t`'s contents.

Swaps the contents of `a` and `b`, two `mpz_array_t`'s.

**Note:**

In some case, pointer swapping is inappropriate (for example, if the pointers are passed as function arguments!), hence the need for such a swapping function.

**Parameters:**

← *a* A pointer to the first `mpz_array_t` to swap.

← *b* A pointer to the second `mpz_array_t` to swap.

**5.2.3.59 void swap\_uint32\_array (uint32\_array\_t \*const a, uint32\_array\_t \*const b)**

Swaps two `uint32_array_t`'s contents.

Swaps the contents of `a` and `b`, two `uint32_array_t`'s.

**Note:**

In some case, pointer swapping is inappropriate (for example, if the pointers are passed as function arguments!), hence the need for such a swapping function.

**Parameters:**

- ← *a* A pointer to the first `uint32_array_t` to swap.
- ← *b* A pointer to the second `uint32_array_t` to swap.

**5.3 bernsteinisms.h File Reference**

Algorithms from two D. J. Bernstein's papers on the factorization of small integers.

```
#include <inttypes.h>
#include "array.h"
#include "x_array_list.h"
#include "hashtable.h"
#include "smooth_filter.h"
```

**Defines**

- `#define TIFA_BERNSTEINISMS_H`

**Functions**

- `mpz_t * bern_51 (uint32_t b, const mpz_t u)`  
*Daniel J. Bernstein's algorithm 5.1.*
- `mpz_t * bern_53 (uint32_t b, const mpz_t u, const mpz_t x)`  
*Daniel J. Bernstein's algorithm 5.3.*
- `uint32_array_t * bern_63 (const mpz_t x, const mpz_array_t *const tree)`  
*Daniel J. Bernstein's algorithm 6.3.*
- `void bern_71 (uint32_array_list_t *const decomp_list, const mpz_array_t *const to_be_factored, const uint32_array_t *const odd_primes)`  
*Daniel J. Bernstein's algorithm 7.1.*
- `uint32_t bern_21_rt (mpz_array_t *const smooth, const mpz_array_t *const xi, const mpz_t z)`  
*Daniel J. Bernstein's algorithm 2.1 (with computation of a remainder tree).*
- `uint32_t bern_21 (mpz_array_t *const smooth, const mpz_array_t *const xi, const mpz_t z)`  
*Daniel J. Bernstein's algorithm 2.1 (without computation of a remainder tree).*
- `uint32_t bern_21_rt_pairs (mpz_array_t *const xi, mpz_array_t *const smooth_yi, const mpz_array_t *const cand_xi, const mpz_array_t *const cand_yi, const mpz_t z)`  
*Daniel J. Bernstein's algorithm 2.1 modified.*

- `uint32_t bern_21_pairs` (`mpz_array_t *const xi`, `mpz_array_t *const smooth_yi`, `const mpz_array_t *const cand_xi`, `const mpz_array_t *const cand_yi`, `const mpz_t z`)  
*Daniel J. Bernstein's algorithm 2.1 modified (without computation of a remainder tree).*
- `uint32_t bern_21_rt_pairs_lp` (`const mpz_t n`, `hashtable_t *const htable`, `mpz_array_t *const xi`, `mpz_array_t *const smooth_yi`, `const mpz_array_t *const cand_xi`, `const mpz_array_t *const cand_yi`, `const mpz_t z`)  
*Daniel J. Bernstein's algorithm 2.1 modified, with large primes variation.*
- `uint32_t bern_21_pairs_lp` (`const mpz_t n`, `hashtable_t *const htable`, `mpz_array_t *const xi`, `mpz_array_t *const smooth_yi`, `const mpz_array_t *const cand_xi`, `const mpz_array_t *const cand_yi`, `const mpz_t z`)  
*Daniel J. Bernstein's algorithm 2.1 modified, with large primes variation (without computation of a remainder tree).*
- `uint32_t bern_21_rt_pairs_siqs` (`mpz_array_t *const xi`, `mpz_array_t *const smooth_yi`, `mpz_array_t *const a_for_smooth_gx`, `const mpz_array_t *const cand_xi`, `const mpz_array_t *const cand_yi`, `const mpz_array_t *const cand_a`, `const mpz_t z`)  
*Daniel J. Bernstein's algorithm 2.1 modified for SIQS (with computation of a remainder tree).*
- `uint32_t bern_21_rt_pairs_lp_siqs` (`const mpz_t n`, `hashtable_t *const htable`, `mpz_array_t *const xi`, `mpz_array_t *const smooth_yi`, `mpz_array_t *const a_for_smooth_yi`, `const mpz_array_t *const cand_xi`, `const mpz_array_t *const cand_yi`, `const mpz_array_t *const cand_a`, `const mpz_t z`)  
*Daniel J. Bernstein's algorithm 2.1 modified for SIQS, with large primes variation (with computation of a remainder tree).*
- `uint32_t djb_batch_rt` (`smooth_filter_t *const filter`, `unsigned long int step`)  
*Daniel J. Bernstein's algorithm 2.1 adapted to be used with a smooth\_filter\_t.*

### 5.3.1 Detailed Description

Algorithms from two D. J. Bernstein's papers on the factorization of small integers.

**Author:**

Jerome Milan

**Date:**

Fri Jun 10 2011

**Version:**

2011-06-10

Algorithms from two D. J. Bernstein's papers on the factorization of small integers:

- "How to find small factors of integers", <http://cr.yp.to/papers/sf.pdf>
- "How to find smooth parts of integers", <http://cr.yp.to/factorization/smoothparts-20040510.pdf>

Definition in file [bernsteinisms.h](#).

### 5.3.2 Define Documentation

#### 5.3.2.1 #define \_TIFA\_BERNSTEINISMS\_H\_

Standard include guard.

Definition at line 40 of file bernsteinisms.h.

### 5.3.3 Function Documentation

#### 5.3.3.1 uint32\_t bern\_21 (mpz\_array\_t \*const smooth, const mpz\_array\_t \*const xi, const mpz\_t z)

Daniel J. Bernstein's algorithm 2.1 (without computation of a remainder tree).

Given the prime numbers  $p_j$  listed by  $p_j$  and the positive integers  $x_i$  listed by  $x_i$ , determines the  $\{p_j\}$ -smooth part of each  $x_i$  and stores them in *smooth*, so that *smooth*->data[i] is the  $\{p_j\}$ -smooth part of *xi*->data[i].

The function stops when each integer from *xi* has been checked for smoothness or when the *smooth* array is completely filled. It then returns the index of the last integer in *xi* that has been checked for smoothness.

This is the algorithm 2.1 described in Daniel J. Bernstein's paper: "How to find smooth parts of integers".

#### Note:

This function differs from *bern\_21\_rt* only because no remainder tree is computed. This can sometimes be faster than the full fledged version.

#### See also:

Daniel J. Bernstein's paper: "How to find smooth parts of integers", <http://cr.yep.to/factorization/smoothparts-20040510.pdf>

#### Parameters:

- *smooth* A pointer to the  $\{p_j\}$ -smooth parts of each  $x_i$  integer.
- ← *xi* A pointer to the list of the  $x_i$  integers.
- ← *z* The product of the the  $p_j$  prime numbers in the facotr base.

#### Returns:

The index of the last integer in *xi* that has been checked for smoothness.

#### 5.3.3.2 uint32\_t bern\_21\_pairs (mpz\_array\_t \*const xi, mpz\_array\_t \*const smooth\_yi, const mpz\_array\_t \*const cand\_xi, const mpz\_array\_t \*const cand\_yi, const mpz\_t z)

Daniel J. Bernstein's algorithm 2.1 modified (without computation of a remainder tree).

Given the prime numbers  $p_j$  listed by  $p_j$  and the positive integers  $y_i$  listed by *cand\_yi*, determines the  $y_i$  that are  $\{p_j\}$ -smooth and stores them in *smooth\_yi*, so that *smooth\_yi*->data[i] is indeed  $\{p_j\}$ -smooth.

In a typical factorization problem, we other found ourselves in situations where each  $y_i$  is associated to another integer  $x_i$ . The  $x_i$  associated to the  $\{p_j\}$ -smooth  $y_i$  are hence stored in *xi*.

The function stops when each integer from `cand_yi` has been checked for smoothness or when the `smooth_yi` array is completely filled. It then returns the index of the last integer in `cand_yi` that has been checked for smoothness.

This function uses the algorithm 2.1 described in Daniel J. Bernstein's paper: "How to find smooth parts of integers" except that this function has been tailored to better suit the factorization problem.

**Note:**

This function is very similar to `bern_21_rt_pairs`. The only difference is that in `bern_21_pairs` no remainder tree is computed. This can sometimes be faster than the full fledged version.

**See also:**

Daniel J. Bernstein's paper: "How to find smooth parts of integers", <http://cr.yz.to/factorization/smoothparts-20040510.pdf>

**Parameters:**

- *xi* A pointer to the  $\{x_i\}$  associated to the  $\{p_j\}$ -smooth  $y_i$  integer.
- *smooth\_yi* A pointer to the  $\{p_j\}$ -smooth  $y_i$  integer.
- ← *cand\_xi* A pointer to the list of the  $x_i$  integers.
- ← *cand\_yi* A pointer to the list of the  $y_i$  integers.
- ← *z* The product of the the  $p_j$  prime numbers in the facotr base.

**Returns:**

The index of the last integer in `cand_yi` that has been checked for smoothness.

**5.3.3.3 uint32\_t bern\_21\_pairs\_lp (const mpz\_t n, hashtable\_t \*const htable, mpz\_array\_t \*const xi, mpz\_array\_t \*const smooth\_yi, const mpz\_array\_t \*const cand\_xi, const mpz\_array\_t \*const cand\_yi, const mpz\_t z)**

Daniel J. Bernstein's algorithm 2.1 modified, with large primes variation (without computation of a remainder tree).

Given  $z$ , the product of prime numbers  $p_j$  and the positive integers  $y_i$  listed by `cand_yi`, determines the  $y_i$  that are  $\{p_j\}$ -smooth and stores them in `smooth_yi`, so that `smooth_yi->data[i]` is indeed  $\{p_j\}$ -smooth.

In a typical factorization problem, we other found ourselves in situations where each  $y_i$  is associated to another integer  $x_i$ . The  $x_i$  associated to the  $\{p_j\}$ -smooth  $y_i$  are hence stored in `xi`.

Moreover, this function implements the so-called large primes variation. If a given  $y_i$  is not  $\{p_j\}$ -smooth but is the product of a prime  $p$  by a  $\{p_j\}$ -smooth number, it is stored in the hashtable `htable`. Subsequently, if another  $y_j$  is the product of a  $\{p_j\}$ -smooth number by the same prime number  $p$ , then  $y_i*y_j/(p^2)$  is stored in `smooth_yi` and  $x_i*x_j*p^{-1}$  is stored in `xi` where  $p^{-1}$  is the inverse of  $p$  in  $\mathbb{Z}/c\mathbb{Z}$ .

The function stops when each integer from `cand_yi` has been checked for smoothness or when the `smooth_yi` array is completely filled. It then returns the index of the last integer in `cand_yi` that has been checked for smoothness.

This function uses the algorithm 2.1 described in Daniel J. Bernstein's paper: "How to find smooth parts of integers" except that this function has been tailored to better suit the factorization problem.

**Note:**

This function is very similar to `bern_21_rt_pairs_lp`. The only difference is that here no remainder tree is computed. This can sometimes be faster than the full fledged version.

**See also:**

Daniel J. Bernstein's paper: "How to find smooth parts of integers", <http://cr.yep.to/factorization/smoothparts-20040510.pdf>

**Parameters:**

- ← *n* The integer to factor.
- ← *htable* A pointer to the hashtable used for the large prime variation.
- *xi* A pointer to the  $\{x_i\}$  associated to the  $\{p_j\}$ -smooth  $y_i$  integer.
- *smooth\_yi* A pointer to the  $\{p_j\}$ -smooth  $y_i$  integer.
- ← *cand\_xi* A pointer to the list of the  $x_i$  integers.
- ← *cand\_yi* A pointer to the list of the  $y_i$  integers.
- ← *z* The product of the the  $p_j$  prime numbers in the facotr base.

**Returns:**

The index of the last integer in `cand_yi` that has been checked for smoothness.

### 5.3.3.4 uint32\_t bern\_21\_rt (mpz\_array\_t \*const smooth, const mpz\_array\_t \*const xi, const mpz\_t z)

Daniel J. Bernstein's algorithm 2.1 (with computation of a remainder tree).

Given the prime numbers  $p_j$  listed by `pj` and the positive integers  $x_i$  listed by `xi`, determines the  $\{p_j\}$ -smooth part of each  $x_i$  and stores them in `smooth`, so that `smooth->data[i]` is the  $\{p_j\}$ -smooth part of `xi->data[i]`.

The function stops when each integer from `xi` has been checked for smoothness or when the `smooth` array is completely filled. It then returns the index of the last integer in `xi` that has been checked for smoothness.

This is the algorithm 2.1 described in Daniel J. Bernstein's paper: "How to find smooth parts of integers".

**See also:**

Daniel J. Bernstein's paper: "How to find smooth parts of integers", <http://cr.yep.to/factorization/smoothparts-20040510.pdf>

**Parameters:**

- *smooth* A pointer to the  $\{p_j\}$ -smooth parts of each  $x_i$  integer.
- ← *xi* A pointer to the list of the  $x_i$  integers.
- ← *z* The product of the the  $p_j$  prime numbers in the facotr base.

**Returns:**

The index of the last integer in `xi` that has been checked for smoothness.

### 5.3.3.5 uint32\_t bern\_21\_rt\_pairs (mpz\_array\_t \*const xi, mpz\_array\_t \*const smooth\_yi, const mpz\_array\_t \*const cand\_xi, const mpz\_array\_t \*const cand\_yi, const mpz\_t z)

Daniel J. Bernstein's algorithm 2.1 modified.

Given the prime numbers  $p_j$  listed by `pj` and the positive integers  $y_i$  listed by `cand_yi`, determines the  $y_i$  that are  $\{p_j\}$ -smooth and stores them in `smooth_yi`, so that `smooth_yi->data[i]` is indeed  $\{p_j\}$ -smooth.

In a typical factorization problem, we often found ourselves in situations where each  $y_i$  is associated to another integer  $x_i$ . The  $x_i$  associated to the  $\{p_j\}$ -smooth  $y_i$  are hence stored in `xi`.

The function stops when each integer from `cand_yi` has been checked for smoothness or when the `smooth_yi` array is completely filled. It then returns the index of the last integer in `cand_yi` that has been checked for smoothness.

This function uses the algorithm 2.1 described in Daniel J. Bernstein's paper: "How to find smooth parts of integers" except that this function has been tailored to better suit the factorization problem.

#### See also:

Daniel J. Bernstein's paper: "How to find smooth parts of integers", <http://cr.yep.to/factorization/smoothparts-20040510.pdf>

#### Parameters:

- `xi` A pointer to the  $\{x_i\}$  associated to the  $\{p_j\}$ -smooth  $y_i$  integer.
- `smooth_yi` A pointer to the  $\{p_j\}$ -smooth  $y_i$  integer.
- ← `cand_xi` A pointer to the list of the  $x_i$  integers.
- ← `cand_yi` A pointer to the list of the  $y_i$  integers.
- ← `z` The product of the  $p_j$  prime numbers in the factor base.

#### Returns:

The index of the last integer in `cand_yi` that has been checked for smoothness.

### 5.3.3.6 uint32\_t bern\_21\_rt\_pairs\_lp (const mpz\_t n, hashtable\_t \*const htable, mpz\_array\_t \*const xi, mpz\_array\_t \*const smooth\_yi, const mpz\_array\_t \*const cand\_xi, const mpz\_array\_t \*const cand\_yi, const mpz\_t z)

Daniel J. Bernstein's algorithm 2.1 modified, with large primes variation.

Given  $z$ , the product of prime numbers  $p_j$  and the positive integers  $y_i$  listed by `cand_yi`, determines the  $y_i$  that are  $\{p_j\}$ -smooth and stores them in `smooth_yi`, so that `smooth_yi->data[i]` is indeed  $\{p_j\}$ -smooth.

In a typical factorization problem, we often found ourselves in situations where each  $y_i$  is associated to another integer  $x_i$ . The  $x_i$  associated to the  $\{p_j\}$ -smooth  $y_i$  are hence stored in `xi`.

Moreover, this function implements the so-called large primes variation. If a given  $y_i$  is not  $\{p_j\}$ -smooth but is the product of a prime  $p$  by a  $\{p_j\}$ -smooth number, it is stored in the hashtable `htable`. Subsequently, if another  $y_j$  is the product of a  $\{p_j\}$ -smooth number by the same prime number  $p$ , then  $y_i * y_j / (p^2)$  is stored in `smooth_yi` and  $x_i * x_j * p^{-1}$  is stored in `xi` where  $p^{-1}$  is the inverse of  $p$  in  $\mathbb{Z}/c\mathbb{Z}$ .

The function stops when each integer from `cand_yi` has been checked for smoothness or when the `smooth_yi` array is completely filled. It then returns the index of the last integer in `cand_yi` that has been checked for smoothness.



This function uses the algorithm 2.1 described in Daniel J. Bernstein's paper: "How to find smooth parts of integers" except that this function has been tailored to better suit the factorization problem.

**See also:**

Daniel J. Bernstein's paper: "How to find smooth parts of integers", <http://cr.yep.to/factorization/smoothparts-20040510.pdf>

**Parameters:**

- ← *n* The integer to factor.
- ← *htable* A pointer to the hashtable used for the large prime variation.
- *xi* A pointer to the {*x<sub>i</sub>*} associated to the {*p<sub>j</sub>*}-smooth *y<sub>i</sub>* integer.
- *smooth\_yi* A pointer to the {*p<sub>j</sub>*}-smooth *y<sub>i</sub>* integer.
- ← *cand\_xi* A pointer to the list of the *x<sub>i</sub>* integers.
- ← *cand\_yi* A pointer to the list of the *y<sub>i</sub>* integers.
- ← *z* The product of the the *p<sub>j</sub>* prime numbers in the facotr base.

**Returns:**

The index of the last integer in *cand\_yi* that has been checked for smoothness.

**5.3.3.7 uint32\_t bern\_21\_rt\_pairs\_lp\_siqs (const mpz\_t n, hashtable\_t \*const htable, mpz\_array\_t \*const xi, mpz\_array\_t \*const smooth\_yi, mpz\_array\_t \*const a\_for\_smooth\_yi, const mpz\_array\_t \*const cand\_xi, const mpz\_array\_t \*const cand\_yi, const mpz\_array\_t \*const cand\_a, const mpz\_t z)**

Daniel J. Bernstein's algorithm 2.1 modified for SIQS, with large primes variation (with computation of a remainder tree).

Given *z*, the product of prime numbers *p<sub>j</sub>* and the positive integers *y<sub>i</sub>* listed by *cand\_yi*, determines the *y<sub>i</sub>* that are {*p<sub>j</sub>*}-smooth and stores them in *smooth\_yi*, so that *smooth\_yi->data[i]* is indeed {*p<sub>j</sub>*}-smooth.

In a typical factorization problem, we other found ourselves in situations where each *y<sub>i</sub>* is associated to another integer *x<sub>i</sub>*. The *x<sub>i</sub>* associated to the {*p<sub>j</sub>*}-smooth *y<sub>i</sub>* are hence stored in *xi*.

Moreover, this function implements the so-called large primes variation. If a given *y<sub>i</sub>* is not {*p<sub>j</sub>*}-smooth but is the product of a prime *p* by a {*p<sub>j</sub>*}-smooth number, it is stored in the hashtable *htable*. Subsequently, if another *y<sub>j</sub>* is the product of a {*p<sub>j</sub>*}-smooth number by the same prime number *p*, then *y<sub>i</sub>\*y<sub>j</sub>/(p<sup>2</sup>)* is stored in *smooth\_yi* and *x<sub>i</sub>\*x<sub>j</sub>\*pinv* is stored in *xi* where *pinv* is the inverse of *p* in  $Z/cZ$ .

The function stops when each integer from *cand\_yi* has been checked for smoothness or when the *smooth\_yi* array is completely filled. It then returns the index of the last integer in *cand\_yi* that has been checked for smoothness.

This function uses the algorithm 2.1 described in Daniel J. Bernstein's paper: "How to find smooth parts of integers" except that this function has been tailored to better suit the factorization problem, particularly to our SIQS implementation where we need to keep track of additionnal *a<sub>i</sub>* integers associated to each *y<sub>i</sub>* integers. These extra integers are stored in *cand\_a* whereas the *a<sub>i</sub>* associated to the smooth *y<sub>i</sub>* will be stored in the *a\_for\_smooth\_gx* array.

**Note:**

The *a<sub>i</sub>* integers are actually the values of the first parameter of the polynomials used in the SIQS algorithm.

**See also:**

Daniel J. Bernstein's paper: "How to find smooth parts of integers", <http://cr.yz.to/factorization/smoothparts-20040510.pdf>

**Parameters:**

- ← *n* The integer to factor.
- ← *htable* A pointer to the hashtable used for the large prime variation.
- *xi* A pointer to the  $x_i$  associated to the  $\{p_j\}$ -smooth  $y_i$  integer.
- *smooth\_yi* A pointer to the  $\{p_j\}$ -smooth  $y_i$  integer.
- *a\_for\_smooth\_yi* A pointer to the array of the  $a_i$  integers.
- ← *cand\_xi* A pointer to the list of the  $x_i$  integers.
- ← *cand\_yi* A pointer to the list of the  $y_i$  integers.
- ← *cand\_a* A pointer to the list of the  $a_i$  integers associated to the  $\{p_j\}$ -smooth  $y_i$  integers.
- ← *z* The product of the  $p_j$  prime numbers in the factor base.

**Returns:**

The index of the last integer in *cand\_yi* that has been checked for smoothness.

### 5.3.3.8 uint32\_t bern\_21\_rt\_pairs\_siqs (mpz\_array\_t \*const xi, mpz\_array\_t \*const smooth\_yi, mpz\_array\_t \*const a\_for\_smooth\_gx, const mpz\_array\_t \*const cand\_xi, const mpz\_array\_t \*const cand\_yi, const mpz\_array\_t \*const cand\_a, const mpz\_t z)

Daniel J. Bernstein's algorithm 2.1 modified for SIQS (with computation of a remainder tree).

Given  $z$ , the product of prime numbers  $p_j$  and the positive integers  $y_i$  listed by *cand\_yi*, determines the  $y_i$  that are  $\{p_j\}$ -smooth and stores them in *smooth\_yi*, so that *smooth\_yi*->data[i] is indeed  $\{p_j\}$ -smooth.

In a typical factorization problem, we often find ourselves in situations where each  $y_i$  is associated to another integer  $x_i$ . The  $x_i$  associated to the  $\{p_j\}$ -smooth  $y_i$  are hence stored in *xi*.

The function stops when each integer from *cand\_yi* has been checked for smoothness or when the *smooth\_yi* array is completely filled. It then returns the index of the last integer in *cand\_yi* that has been checked for smoothness.

This function uses the algorithm 2.1 described in Daniel J. Bernstein's paper: "How to find smooth parts of integers" except that this function has been tailored to better suit the factorization problem, particularly to our SIQS implementation where we need to keep track of additional  $a_i$  integers associated to each  $y_i$  integers. These extra integers are stored in *cand\_a* whereas the  $a_i$  associated to the smooth  $y_i$  will be stored in the *a\_for\_smooth\_gx* array.

**Note:**

The  $a_i$  integers are actually the values of the first parameter of the polynomials used in the SIQS algorithm.

**See also:**

Daniel J. Bernstein's paper: "How to find smooth parts of integers", <http://cr.yz.to/factorization/smoothparts-20040510.pdf>

**Parameters:**

- *xi* A pointer to the  $x_i$  associated to the  $\{p_j\}$ -smooth  $y_i$  integer.

- *smooth\_yi* A pointer to the  $\{p_j\}$ -smooth  $y_i$  integer.
- *a\_for\_smooth\_gx* A pointer to the array of the  $a_i$  integers.
- ← *cand\_xi* A pointer to the list of the  $x_i$  integers.
- ← *cand\_yi* A pointer to the list of the  $y_i$  integers.
- ← *cand\_a* A pointer to the list of the  $a_i$  integers associated to the  $\{p_j\}$ -smooth  $y_i$  integers.
- ← *z* The product of the the  $p_j$  prime numbers in the factor base.

**Returns:**

The index of the last integer in *cand\_yi* that has been checked for smoothness.

**5.3.3.9 mpz\_t\* bern\_51 (uint32\_t b, const mpz\_t u)**

Daniel J. Bernstein's algorithm 5.1.

Given a positive integer  $b$  and an odd positive integer  $u$ , returns a non negative integer  $v < 2^b$  such that  $1 + u*v = 0 \pmod{2^b}$ .

This is the algorithm 5.1 described in Daniel J. Bernstein's paper: "How to find small factors of integers".

**See also:**

Daniel J. Bernstein's paper: "How to find small factors of integers", <http://cr.yp.to/papers/sf.pdf>

**Parameters:**

- ← *b* A positive integer.
- ← *u* An odd positive mpz\_t integer.

**Returns:**

A non negative mpz\_t integer  $v < 2^b$  such that  $1 + u*v = 0 \pmod{2^b}$ .

**5.3.3.10 mpz\_t\* bern\_53 (uint32\_t b, const mpz\_t u, const mpz\_t x)**

Daniel J. Bernstein's algorithm 5.3.

Given an odd positive integer  $u < 2^c$  and a non negative integer  $x < 2^{(b+c)}$ , returns a non negative integer  $r < 2^{(c+1)}$  such that  $r*2^b = x \pmod{u}$ .

This is the algorithm 5.3 described in Daniel J. Bernstein's paper: "How to find small factors of integers".

**See also:**

Daniel J. Bernstein's paper: "How to find small factors of integers", <http://cr.yp.to/papers/sf.pdf>

**Parameters:**

- ← *b* A positive integer.
- ← *u* An odd positive mpz\_t integer.
- ← *x* An non negative mpz\_t integer.

**Returns:**

A non negative mpz\_t integer  $r$  such that  $r*2^b = x \pmod{u}$ .

**5.3.3.11 uint32\_array\_t\* bern\_63 (const mpz\_t x, const mpz\_array\_t \*const tree)**

Daniel J. Bernstein's algorithm 6.3.

Given a non negative integer  $x$  and given the product `tree` of a sequence of odd positive integers  $p_i$ , returns the integers  $p_i$  such that:  $x \bmod p_i = 0$ .

This is the algorithm 6.3 described in Daniel J. Bernstein's paper: "How to find small factors of integers".

**See also:**

Daniel J. Bernstein's paper: "How to find small factors of integers", <http://cr.yp.to/papers/sf.pdf>

**Parameters:**

- ←  $x$  A non negative positive integer.
- ← `tree` The product tree of a sequence of odd positive integers  $p_i$ .

**Returns:**

A pointer to an `uint32_array_t` holding the integers  $p_i$  such that:  $x \bmod p_i = 0$ .

**5.3.3.12 void bern\_71 (uint32\_array\_list\_t \*const decomp\_list, const mpz\_array\_t \*const to\_be\_factored, const uint32\_array\_t \*const odd\_primes)**

Daniel J. Bernstein's algorithm 7.1.

Given a sequence of odd primes  $p_j$  given by `odd_primes` and a set of integers  $n_i$  given by `to_be_factored`, determines, for each  $n_i$ , the list of odd primes  $p_j$  such that  $(n_i \bmod p_j = 0)$  and stores them in `decomp_list`. Each entry in `decomp_list->data[i]` is a pointer to a `mpz_array_t` listing the  $p_j$  for the integer `to_be_factored->data[i]`.

This is the algorithm 7.1 described in Daniel J. Bernstein's paper: "How to find small factors of integers".

**See also:**

Daniel J. Bernstein's paper: "How to find small factors of integers", <http://cr.yp.to/papers/sf.pdf>

**Parameters:**

- `decomp_list` A pointer to the list of matching  $p_j$  for each  $n_i$ .
- ← `to_be_factored` A pointer to the set of integers  $n_i$ .
- ← `odd_primes` A pointer to the set of integers  $p_j$ .

**5.3.3.13 uint32\_t djb\_batch\_rt (smooth\_filter\_t \*const filter, unsigned long int step)**

Daniel J. Bernstein's algorithm 2.1 adapted to be used with a `smooth_filter_t`.

**If `filter->nsteps == 0`** In such a case, no early abort strategy is performed. The effect of the function is the same as `bern_21*_pairs_*` called with:

```
filter->n
filter->htable
```

```
filter->accepted_xi
filter->accepted_yi
filter->accepted_ai
filter->candidate_xi
filter->candidate_yi
filter->candidate_ai
filter->prod_pj[0]
```

If `filter->nsteps != 0` An early abort strategy is performed.

- If  $1 \leq \text{step} < \text{filter->nsteps}$ :  
Relations at step `step-1` from `filter`, (`filter->filtered_*[step-1]`) are used as "candidate" arrays to populate either `filter->accepted_*` or `filter->filtered_*[step]`.
- If `step == 0`:  
The candidate relations are taken from `filter->candidate_*`.
- If `step == filter->nsteps`:  
The candidate relations are taken from `filter->filtered_*[filter->nsteps - 1]` and 'good' relations will be stored in `filter->accepted_*`.

**See also:**

The `bern_21_*` functions.

**Warning:**

Using `filter->nsteps != 0` is not recommended. First, it certainly does not make any sense to try to early-abort the batch. Second, even if it is useful (for some weird reasons that I'm not aware of), the cases `filter->nsteps != 0` have not been tuned / fully debugged.

**Parameters:**

*filter* pointer to the `smooth_filter_t` to use  
*step* the step number in the early abort strategy

**Returns:**

The number of relations used from the "candidate" arrays.

## 5.4 bitstring\_t.h File Reference

Preprocessor defines for 'string of bit' type.

```
#include "tifa_config.h"
```

**Defines**

- `#define \_TIFA\_BITSTRING\_T\_H\_`

### 5.4.1 Detailed Description

Preprocessor defines for 'string of bit' type.

**Author:**

Jerome Milan

**Date:**

Fri Jun 10 2011

**Version:**

2011-06-10

Defines several preprocessor `define` symbols related to the type used to represent strings of bit. These symbols are kept separately to avoid too much namespace pollution.

Definition in file [bitstring\\_t.h](#).

### 5.4.2 Define Documentation

#### 5.4.2.1 `#define _TIFA_BITSTRING_T_H_`

Standard include guard.

Definition at line 37 of file [bitstring\\_t.h](#).

## 5.5 buckets.h File Reference

Structure and inline functions to implement bucket sieving.

```
#include <stdlib.h>
```

### 5.5.1 Detailed Description

Structure and inline functions to implement bucket sieving.

**Author:**

Jerome Milan

**Date:**

Fri Jun 10 2011

**Version:**

2011-06-10

Definition in file [buckets.h](#).

## 5.6 cfrac.h File Reference

The CFRAC factorization algorithm.

```
#include <stdbool.h>
#include <gmp.h>
#include "first_primes.h"
#include "array.h"
#include "lindep.h"
#include "smooth_filter.h"
#include "factoring_machine.h"
#include "exit_codes.h"
```

### Data Structures

- struct [struct\\_cfrac\\_params\\_t](#)  
*Defines the variable parameters used in the CFRAC algorithm.*

### Defines

- #define [\\_TIFA\\_CFRAC\\_H](#)
- #define [CFRAC\\_DFLT\\_NPRIMES\\_IN\\_BASE](#) (NFIRST\_PRIMES/16)
- #define [CFRAC\\_DFLT\\_NPRIMES\\_TDIV](#) (NFIRST\_PRIMES/16)
- #define [CFRAC\\_DFLT\\_NRELATIONS](#) 32
- #define [CFRAC\\_DFLT\\_LINALG\\_METHOD](#) SMART\_GAUSS\_ELIM
- #define [CFRAC\\_DFLT\\_USE\\_LARGE\\_PRIMES](#) true

### Typedefs

- typedef struct [struct\\_cfrac\\_params\\_t](#) [cfrac\\_params\\_t](#)  
*Equivalent to struct [struct\\_cfrac\\_params\\_t](#).*

### Functions

- void [set\\_cfrac\\_params\\_to\\_default](#) (const [mpz\\_t](#) n, [cfrac\\_params\\_t](#) \*const params)  
*Fills a [cfrac\\_params\\_t](#) with "good" default values.*
- [ecode\\_t](#) [cfrac](#) ([mpz\\_array\\_t](#) \*const factors, [uint32\\_array\\_t](#) \*const multis, const [mpz\\_t](#) n, const [cfrac\\_params\\_t](#) \*const params, const [factoring\\_mode\\_t](#) mode)  
*Integer factorization via the continued fraction (CFRAC) algorithm.*

### 5.6.1 Detailed Description

The CFRAC factorization algorithm.

**Author:**

Jerome Milan

**Date:**

Fri Jun 10 2011

**Version:**

2011-06-10

This is the TIFA library's implementation of the CFRAC factorization algorithm from M. A. Morrison and J. Brillhart, together with the large prime variation.

**See also:**

"A Method of Factoring and the Factorization of  $F_7$ ", M. A. Morrison and J. Brillhart, *Mathematics of Computation*, vol 29, #129, Jan 1975, pages 183-205.

Definition in file [cfrac.h](#).

### 5.6.2 Define Documentation

#### 5.6.2.1 #define \_TIFA\_CFRAC\_H\_

Standard include guard.

Definition at line 41 of file cfrac.h.

#### 5.6.2.2 #define CFRAC\_DFLT\_LINALG\_METHOD SMART\_GAUSS\_ELIM

Default linear system resolution method to use.

Definition at line 79 of file cfrac.h.

#### 5.6.2.3 #define CFRAC\_DFLT\_NPRIMES\_IN\_BASE (NFIRST\_PRIMES/16)

Default number of prime numbers composing the factor base on which to factor the residues.

Definition at line 62 of file cfrac.h.

#### 5.6.2.4 #define CFRAC\_DFLT\_NPRIMES\_TDIV (NFIRST\_PRIMES/16)

Default number of the first primes to use in the trial division of the residues.

Definition at line 68 of file cfrac.h.

#### 5.6.2.5 #define CFRAC\_DFLT\_NRELATIONS 32

Default number of congruence relations to find before attempting the factorization of the large integer.

Definition at line 74 of file cfrac.h.



**5.6.2.6 #define CFRAC\_DFLT\_USE\_LARGE\_PRIMES true**

Use the large prime variation by default.

Definition at line 84 of file cfrac.h.

**5.6.3 Function Documentation****5.6.3.1 `ecode_t cfrac (mpz_array_t *const factors, uint32_array_t *const multis, const mpz_t n, const cfrac_params_t *const params, const factoring_mode_t mode)`**

Integer factorization via the continued fraction (CFRAC) algorithm.

Attempts to factor the non perfect square integer *n* with the CFRAC algorithm, using the set of parameters given by *params* and the factoring mode given by *mode*. Found factors are then stored in *factors*. Additionally, if the factoring mode used is set to `FIND_COMPLETE_FACTORIZATION`, factors' multiplicities are stored in the array *multis*.

**Note:**

If the factoring mode used is different from `FIND_COMPLETE_FACTORIZATION`, *multis* is allowed to be a `NULL` pointer. Otherwise, using a `NULL` pointer will lead to a fatal error.

**Warning:**

If the *factors* and *multis* arrays have not enough room to store the found factors (and the multiplicities, if any), they will be automatically resized to accommodate the data. This has to be kept in mind when trying to do ingenious stuff with memory management (hint: don't try to be clever here). The "no large primes" variant is currently disabled.

**Parameters:**

- *factors* Pointer to the found factors of *n*.
- *multis* Pointer to the multiplicities of the found factors (only computed if *mode* is set to `FIND_COMPLETE_FACTORIZATION`).
- ← *n* The non perfect square integer to factor.
- ← *params* Pointer to the values of the parameters used in the CFRAC algorithm.
- ← *mode* The factoring mode to use.

**Returns:**

An exit code.

**5.6.3.2 `void set_cfrac_params_to_default (const mpz_t n, cfrac_params_t *const params)`**

Fills a `cfrac_params_t` with "good" default values.

Fills a `cfrac_params_t` with "good" default values choosen according to the size of the number *n* to factor.

**Warning:**

There is no guarantee that the choosen parameter values will be the best ones for a given number to factor. However, provided that the number to factor is between 40 and 200 bits long, the choosen values should be nearly optimal.

**Parameters:**

- ← *n* The `mpz_t` integer to factor.
- *params* A pointer to the `cfrac_params_t` structure to fill.

## 5.7 `common_funcs.h` File Reference

Miscellaneous functions and macros used by the "tool" programs.

```
#include "first_primes.h"
```

**Defines**

- #define `_TIFA_COMMON_FUNCS_H`
- #define `PRINT_ABORT_MSG()` `fprintf(stderr, "Program aborted\n");`
- #define `PRINT_NAN_ERROR(X)`
- #define `PRINT_BAD_ARGC_ERROR()`
- #define `PRINT_ENTER_NUMBER_MSG()` `printf("> Enter the integer to factor: ")`
- #define `PRINT_USAGE_WARNING_MSG()`
- #define `MAX_NDIGITS` 256
- #define `NTRIES_MILLER_RABIN` 32
- #define `NPRIMES_TRIAL_DIV` `NFIRST_PRIMES`

**Functions**

- void `print_hello_msg` (char \*name)  
*Function used by the "tool" programs to print a greeting message.*
- void `print_bye_msg` ()  
*Function used by the "tool" programs to print a bye-bye message.*

### 5.7.1 Detailed Description

Miscellaneous functions and macros used by the "tool" programs.

**Author:**

Jerome Milan

**Date:**

Fri Jun 10 2011

**Version:**

2011-06-10

Definition in file [common\\_funcs.h](#).

## 5.7.2 Define Documentation

### 5.7.2.1 #define \_TIFA\_COMMON\_FUNCS\_H\_

Standard include guard.

Definition at line 33 of file common\_funcs.h.

### 5.7.2.2 #define MAX\_NDIGITS 256

Maximal number of decimal digits of the number to factor.

Definition at line 90 of file common\_funcs.h.

### 5.7.2.3 #define NPRIMES\_TRIAL\_DIV NFIRST\_PRIMES

Default number of prime numbers used in trial division of number to factor.

Definition at line 101 of file common\_funcs.h.

### 5.7.2.4 #define NTRIES\_MILLER\_RABIN 32

Number of iterations to use in the Miller-Rabin composition tests.

Definition at line 95 of file common\_funcs.h.

### 5.7.2.5 #define PRINT\_ABORT\_MSG() fprintf(stderr, "Program aborted\n");

Macro printing an "program has aborted" message on the standard error.

Definition at line 50 of file common\_funcs.h.

### 5.7.2.6 #define PRINT\_BAD\_ARGC\_ERROR()

**Value:**

```
do {
    \
    fprintf(stderr, "\nERROR: Bad number of arguments!\n\n"); \
} while (0)
```

Macro printing a "bad number of argument" error message on the standard error.

Definition at line 67 of file common\_funcs.h.

### 5.7.2.7 #define PRINT\_ENTER\_NUMBER\_MSG() printf("> Enter the integer to factor: ")

Macro displaying a prompt asking the user to enter the integer to factor.

Definition at line 75 of file common\_funcs.h.

### 5.7.2.8 #define PRINT\_NAN\_ERROR(X)

**Value:**

```
do {
    \
    fprintf(stderr, "\nERROR: %s is not an integer!\n", X); \
    PRINT_ABORT_MSG(); \
} while (0)
```

Macro printing a "X is not an integer" error message on the standard error.

Definition at line 57 of file common\_funcs.h.

### 5.7.2.9 #define PRINT\_USAGE\_WARNING\_MSG()

**Value:**

```
do {
    fprintf(stderr, "Please, use the perl wrapper factorize.pl instead of "); \
    fprintf(stderr, "a direct invocation\nof this program.\n"); \
} while (0)
```

Macro printing a boilerplate usage warning on the standard error.

Definition at line 81 of file common\_funcs.h.

## 5.7.3 Function Documentation

### 5.7.3.1 void print\_bye\_msg ()

Function used by the "tool" programs to print a bye-bye message.

This function could be used by the "tool" programs to print a bye-bye message (it is not used right now).

### 5.7.3.2 void print\_hello\_msg (char \* name)

Function used by the "tool" programs to print a greeting message.

**Parameters:**

← *name* Name of the factoring program.

## 5.8 ecm.h File Reference

The elliptic curve method of integer factorization (ECM).

```
#include <gmp.h>
#include "array.h"
#include "factoring_machine.h"
#include "exit_codes.h"
```

### Data Structures

- struct [struct\\_ecm\\_params\\_t](#)  
*Defines the variable parameters used in ECM.*

### Defines

- #define [\\_TIFA\\_ECM\\_H\\_](#)

## Typedefs

- typedef struct [struct\\_ecm\\_params\\_t](#) [ecm\\_params\\_t](#)  
*Equivalent to struct [struct\\_ecm\\_params\\_t](#).*

## Functions

- void [set\\_ecm\\_params\\_to\\_default](#) (const mpz\_t n, [ecm\\_params\\_t](#) \*const params)  
*Fills an [ecm\\_params\\_t](#) with "good" default values.*
- [ecode\\_t](#) [ecm](#) ([mpz\\_array\\_t](#) \*const factors, [uint32\\_array\\_t](#) \*const multis, const mpz\_t n, const [ecm\\_params\\_t](#) \*const params, const [factoring\\_mode\\_t](#) mode)  
*Integer factorization with the elliptic curve method (ECM).*

### 5.8.1 Detailed Description

The elliptic curve method of integer factorization (ECM).

#### Author:

Jerome Milan

#### Date:

Fri Jun 10 2011

#### Version:

2011-06-10

This is the TIFA library's implementation of the 'ECM' factorization algorithm. The second phase of the algorithm follows the standard continuation and is implemented in a way reminiscent of the description given in the article "Implementing the Elliptic Curve Method of Factoring in Reconfigurable Hardware" by Kris Gaj et al.

#### See also:

"Implementing the Elliptic Curve Method of Factoring in Reconfigurable Hardware", K. Gaj et al., *Cryptographic Hardware and Embedded Systems - CHES 2006*.

#### Warning:

This is merely a toy-implementation of ECM without any smart optimizations. More work is certainly needed to make it competitive for small numbers. Large numbers are, of course, out of the scope of this library.

Definition in file [ecm.h](#).

### 5.8.2 Define Documentation

#### 5.8.2.1 #define [\\_TIFA\\_ECM\\_H\\_](#)

Standard include guard.

Definition at line 48 of file [ecm.h](#).

### 5.8.3 Function Documentation

#### 5.8.3.1 ecode\_t ecm (mpz\_array\_t \*const factors, uint32\_array\_t \*const multis, const mpz\_t n, const ecm\_params\_t \*const params, const factoring\_mode\_t mode)

Integer factorization with the elliptic curve method (ECM).

Attempts to factor the non perfect square integer  $n$  with the ECM, using the set of parameters given by `params` and the factoring mode given by `mode`. Found factors are then stored in `factors`. Additionally, if the factoring mode used is set to `FIND_COMPLETE_FACTORIZATION`, factors' multiplicities are stored in the array `multis`.

#### Note:

If the factoring mode used is different from `FIND_COMPLETE_FACTORIZATION`, `multis` is allowed to be a NULL pointer. Otherwise, using a NULL pointer will lead to a fatal error.

#### Warning:

If the `factors` and `multis` arrays have not enough room to store the found factors (and the multiplicities, if any), they will be automatically resized to accommodate the data. This has to be kept in mind when trying to do ingenious stuff with memory management (hint: don't try to be clever here).

#### Parameters:

- *factors* Pointer to the found factors of  $n$ .
- *multis* Pointer to the multiplicities of the found factors (only computed if `mode` is set to `FIND_COMPLETE_FACTORIZATION`).
- ← *n* The non perfect square integer to factor.
- ← *params* Pointer to the values of the parameters used in the ECM.
- ← *mode* The factoring mode to use.

#### Returns:

An exit code.

#### 5.8.3.2 void set\_ecm\_params\_to\_default (const mpz\_t n, ecm\_params\_t \*const params)

Fills an `ecm_params_t` with "good" default values.

Fills an `ecm_params_t` with "good" default values choosen according to the size of the number  $n$  to factor.

#### Warning:

This is, for the time being, a dummy function. Parameters are *not* set to suitable values *at all!* Do not use it: for the time being, you should choose the parameters by yourself! Shocking!

#### Parameters:

- ← *n* The `mpz_t` integer to factor.
- *params* A pointer to the `ecm_params_t` structure to fill.

## 5.9 exit\_codes.h File Reference

Exit codes used by/in some of the TIFA functions.

## Defines

- #define `_TIFA_EXIT_CODES_H_`
- #define `PRINT_ECODE(ECODE)` `printf("%s\n", ecode_to_str[ECODE]);`

## Typedefs

- typedef enum `ecode_enum` `ecode_t`  
*Equivalent to* `enum ecode_enum`.

## Enumerations

- enum `ecode_enum` {  
    `UNKNOWN_FACTORIZING_MODE`, `SOME_FACTORS_FOUND`, `SOME_PRIME_FACTORS_FOUND`,  
    `SOME_COPRIME_FACTORS_FOUND`,  
    `PARTIAL_FACTORIZATION_FOUND`, `COMPLETE_FACTORIZATION_FOUND`, `NO_FACTOR_FOUND`,  
    `FATAL_INTERNAL_ERROR`,  
    `QUEUE_OVERFLOW`, `NO_PROPER_FORM_FOUND`, `GIVING_UP`, `INTEGER_TOO_LARGE`,  
    `SUCCESS`, `FAILURE` }

## Variables

- static const char \*const `ecode_to_str` [14]

### 5.9.1 Detailed Description

Exit codes used by/in some of the TIFA functions.

#### Author:

Jerome Milan

#### Date:

Fri Jun 10 2011

#### Version:

2011-06-10

Defines several exit codes used by/in some of the TIFA functions together with their string representations.  
Definition in file [exit\\_codes.h](#).

### 5.9.2 Define Documentation

#### 5.9.2.1 #define `_TIFA_EXIT_CODES_H_`

Standard include guard.

Definition at line 36 of file `exit_codes.h`.

### 5.9.2.2 #define PRINT\_ECODE(ECODE) printf("%s\n", ecode\_to\_str[ECODE]);

Macro printing the string representation of the exit code `ECODE` on the standard output, followed by a newline.

Definition at line 156 of file `exit_codes.h`.

## 5.9.3 Enumeration Type Documentation

### 5.9.3.1 enum ecode\_enum

An enumeration of the possible exit codes used by/in some TIFA functions.

#### Enumerator:

**UNKNOWN\_FACTORIZING\_MODE** Used by a `factoring_machine_t` to indicate that the `factoring_mode_t` passed as parameter is not valid.

**SOME\_FACTORS\_FOUND** Used by the factorization algorithm to indicate that *some* factors were found. In that case, the factors' multiplicities are not computed.

**SOME\_PRIME\_FACTORS\_FOUND** Used by the factorization algorithm to indicate that *some* prime factors were found. In that case, the factors' multiplicities are not computed.

**SOME\_COPRIME\_FACTORS\_FOUND** Used by the factorization algorithm to indicate that *some* coprime factors were found. In that case, the factors' multiplicities are not computed.

**PARTIAL\_FACTORIZATION\_FOUND** Used by the factorization algorithm to indicate that a partial factorization (in terms of a set of coprimes and multiplicities) was found. The term "partial" refers to the fact that some found factors may not be prime. However the product of the found factors (taking into account their associated multiplicities) does yield the original number to factor.

**COMPLETE\_FACTORIZATION\_FOUND** Used by the factorization algorithm to indicate that a complete factorization (in terms of primes and multiplicities) was found.

**NO\_FACTOR\_FOUND** Used by the factorization algorithm to indicate that no factor was found.

**FATAL\_INTERNAL\_ERROR** Generic exit code used to indicate a serious internal error, possibly leading to an unpredictable behavior.

**QUEUE\_OVERFLOW** Used by the SQUFOF algorithm to indicate that the queue overflowed, thus leading to give up the factorization process.

**NO\_PROPER\_FORM\_FOUND** Used by the SQUFOF algorithm to indicate that no proper form was found, thus leading to give up the factorization process.

**GIVING\_UP** Used to indicate that an abort limit has been reached leading to give up the current operation.

**INTEGER\_TOO\_LARGE** Used by the SQUFOF and Fermat/McKee implementations to indicate that the integer to factor is too large and cannot be processed.

**SUCCESS** Generic exit code used to indicate that an operation succeeded.

**FAILURE** Generic exit code used to indicate that an operation failed.

Definition at line 47 of file `exit_codes.h`.

## 5.9.4 Variable Documentation

### 5.9.4.1 const char\* const ecode\_to\_str[14] [static]

#### Initial value:



```
{
    "unknown factoring mode",
    "some factors found",
    "some prime factors found",
    "some coprime factors found",
    "partial factorization found",
    "complete factorization found",
    "no factor found",
    "fatal internal error",
    "queue overflow",
    "no proper form found",
    "giving up",
    "number to factor is too large",
    "success",
    "failure"
}
```

Global constant array mapping exit codes to their string representations.

Definition at line 134 of file exit\_codes.h.

## 5.10 factoring\_machine.h File Reference

Abstraction of an integer factorization algorithm.

```
#include <stdbool.h>
#include <gmp.h>
#include "array.h"
#include "exit_codes.h"
```

### Data Structures

- struct [struct\\_factoring\\_machine](#)  
*Defines a structure to represent the logic behind all factorization algorithms.*

### Defines

- #define [\\_TIFA\\_FACTORIZING\\_MACHINE\\_H](#)

### Typedefs

- typedef enum [factoring\\_mode\\_enum](#) [factoring\\_mode\\_t](#)  
*Equivalent to struct factoring\_mode\_enum.*
- typedef struct [struct\\_factoring\\_machine](#) [factoring\\_machine\\_t](#)  
*Equivalent to struct\_factoring\_machine.*

### Enumerations

- enum [factoring\\_mode\\_enum](#) {

```
SINGLE_RUN, FIND_SOME_FACTORS, FIND_SOME_COPRIME_FACTORS, FIND_SOME_-\nPRIME_FACTORS,\nFIND_COMPLETE_FACTORIZATION }
```

## Functions

- `ecode_t run_machine` (`factoring_machine_t *machine`)  
*Attempt to factor an integer.*

## Variables

- static const int `mode_to_outcome` [5]

### 5.10.1 Detailed Description

Abstraction of an integer factorization algorithm.

#### Author:

Jerome Milan

#### Date:

Fri Jun 10 2011

#### Version:

2011-06-10

Implements a machine-like abstraction of an integer factorization algorithm.

Definition in file [factoring\\_machine.h](#).

### 5.10.2 Define Documentation

#### 5.10.2.1 `#define TIFA_FACTORIZING_MACHINE_H`

Standard include guard.

Definition at line 35 of file `factoring_machine.h`.

### 5.10.3 Enumeration Type Documentation

#### 5.10.3.1 `enum factoring_mode_enum`

An enumeration of the factoring mode available to the implemented factorization algorithm.

#### Enumerator:

**`SINGLE_RUN`** Perform only a single run of the factorization algorithm.

**`FIND_SOME_FACTORS`** Run the factorization algorithm until either some factors are found or the abort limit (defined on a per-algorithm basis) is reached.

***FIND\_SOME\_COPRIME\_FACTORS*** Run the factorization algorithm until either some coprime factors are found or the abort limit (defined on a per-algorithm basis) is reached.

***FIND\_SOME\_PRIME\_FACTORS*** Run the factorization algorithm until either some prime factors are found or the abort limit (defined on a per-algorithm basis) is reached.

**Note:**

This is probably not useful at all. Why would we discard found factors even if they are not prime? This should better be left to the client application.

***FIND\_COMPLETE\_FACTORIZATION*** Run the factorization algorithm until either the complete factorization (as a product of prime numbers) is found or the abort limit (defined on a per-algorithm basis) is reached.

Definition at line 53 of file factoring\_machine.h.

### 5.10.4 Function Documentation

#### 5.10.4.1 `ecode_t run_machine (factoring_machine_t * machine)`

Attempt to factor an integer.

Attempt to factor an integer with all parameters given by *machine*.

**Note:**

This function is meant to be a starting point for implementations of factorization algorithms and is obviously not intended to be directly used as a factoring function all by itself.

**Parameters:**

*machine* A pointer to the `factoring_machine_t` to use.

### 5.10.5 Variable Documentation

#### 5.10.5.1 `const int mode_to_outcome[5] [static]`

**Initial value:**

```
{
    SOME_FACTORS_FOUND,
    SOME_FACTORS_FOUND,
    SOME_COPRIME_FACTORS_FOUND,
    SOME_PRIME_FACTORS_FOUND,
    COMPLETE_FACTORIZATION_FOUND
}
```

Global constant array mapping factoring modes to their respective best outcome.

Definition at line 96 of file factoring\_machine.h.

## 5.11 factoring\_program.h File Reference

The logic common to all TIFA's factorization executable programs.

```
#include <gmp.h>
#include "array.h"
```

```
#include "exit_codes.h"
#include "factoring_machine.h"
```

### Data Structures

- struct [struct\\_factoring\\_program](#)  
*Defines a structure to represent the logic behind all factorization programs.*

### Defines

- #define [\\_TIFA\\_FACTORING\\_PROGRAM\\_H\\_](#)

### Typedefs

- typedef struct [struct\\_factoring\\_program](#) [factoring\\_program\\_t](#)  
*Equivalent to struct [struct\\_factoring\\_program](#).*

### Functions

- [ecode\\_t run\\_program](#) ([factoring\\_program\\_t](#) \*const program)  
*Run a factoring program.*

#### 5.11.1 Detailed Description

The logic common to all TIFA's factorization executable programs.

#### Author:

Jerome Milan

#### Date:

Fri Jun 10 2011

#### Version:

2011-06-10

Definition in file [factoring\\_program.h](#).

#### 5.11.2 Define Documentation

##### 5.11.2.1 #define [\\_TIFA\\_FACTORING\\_PROGRAM\\_H\\_](#)

Standard include guard.

Definition at line 33 of file [factoring\\_program.h](#).

### 5.11.3 Function Documentation

#### 5.11.3.1 `ecode_t run_program (factoring_program_t *const program)`

Run a factoring program.

Run an actual factoring program from the command line.

#### Parameters:

*program* The `factoring_program_t` to run.

## 5.12 `fermat.h` File Reference

McKee's variant of the Fermat factorization algorithm.

```
#include <stdlib.h>
#include <gmp.h>
#include "array.h"
#include "factoring_machine.h"
#include "exit_codes.h"
```

### Data Structures

- struct [struct\\_fermat\\_params\\_t](#)  
*Defines the variable parameters used in Fermat's algorithm (dummy structure).*

### Defines

- `#define` [\\_TIFA\\_FERMAT\\_H\\_](#)

### Typedefs

- typedef struct [struct\\_fermat\\_params\\_t](#) `fermat_params_t`  
*Equivalent to struct [struct\\_fermat\\_params\\_t](#).*

### Functions

- void [set\\_fermat\\_params\\_to\\_default](#) (`fermat_params_t *const params`)  
*Fills a `fermat_params_t` with default values (dummy function).*
- `ecode_t` [fermat](#) (`mpz_array_t *const factors`, `uint32_array_t *const multis`, `const mpz_t n`, `const fermat\_params\_t *const params`, `const factoring\_mode\_t mode`)  
*Integer factorization via McKee's speedup of Fermat's factorization algorithm.*

### 5.12.1 Detailed Description

McKee's variant of the Fermat factorization algorithm.

**Author:**

Jerome Milan

**Date:**

Fri Jun 10 2011

**Version:**

2011-06-10

This is the TIFA library's implementation of James McKee's proposed speedup of the Fermat factorization algorithm (SQUFOF), based on the description given by McKee in its paper "Speeding Fermat's Factoring Method".

**Note:**

This implementation can only factor numbers whose size is less than twice the size of an `unsigned long int`.

**See also:**

"Speeding Fermat's Factoring Method", James McKee. *Mathematics of Computation*, Volume 68, Number 228, pages 1729-1737.

Definition in file [fermat.h](#).

### 5.12.2 Define Documentation

#### 5.12.2.1 `#define TIFA_FERMAT_H`

Standard include guard.

Definition at line 44 of file `fermat.h`.

### 5.12.3 Function Documentation

#### 5.12.3.1 `ecode_t` `fermat` (`mpz_array_t *const factors`, `uint32_array_t *const multis`, `const mpz_t n`, `const fermap_params_t *const params`, `const factoring_mode_t mode`)

Integer factorization via McKee's speedup of Fermat's factorization algorithm.

Attempts to factor the non perfect square integer `n` using James McKee's proposed enhancement of Fermat's algorithm, using the factoring mode given by `mode`. Found factors are then stored in `factors`. Additionally, if the factoring mode used is set to `FIND_COMPLETE_FACTORIZATION`, factors' multiplicities are stored in the array `multis`.

**Warning:**

This implementation can only factor numbers whose sizes in bits are strictly less than twice the size of an `unsigned long int`. This choice was made to maximize the use of single precision operations. Such a limitation should not be much of a problem since Fermat's algorithm is mostly used to factor very small integers (up to, say, 20 decimal digits).

**Note:**

If the factoring mode used is different from `FIND_COMPLETE_FACTORIZATION`, `multis` is allowed to be a `NULL` pointer. Otherwise, using a `NULL` pointer will lead to a fatal error.

**Warning:**

If the `factors` and `multis` arrays have not enough room to store the found factors (and the multiplicities, if any), they will be automatically resized to accommodate the data. This has to be kept in mind when trying to do ingenious stuff with memory management (hint: don't try to be clever here).

**Parameters:**

- *factors* Pointer to the found factors of `n`.
- *multis* Pointer to the multiplicities of the found factors (only computed if `mode` is set to `FIND_COMPLETE_FACTORIZATION`).
- ← *n* The non perfect square integer to factor.
- ← *params* Fermat's algorithm parameters (currently unused).
- ← *mode* The factoring mode to use.

**Returns:**

An exit code.

**5.12.3.2 void set\_fermat\_params\_to\_default (fermat\_params\_t \*const params)**

Fills a `fermat_params_t` with default values (dummy function).

This function is intended to fill a `fermat_params_t` with default values.

**Warning:**

For the time being, this is a dummy function which does absolutely nothing at all, but is kept only as a placeholder should the need for user parameters arise in future code revisions.

**Parameters:**

- params* A pointer to the `fermat_params_t` structure to fill.

**5.13 first\_primes.h File Reference**

Precomputed small primes.

```
#include <inttypes.h>
#include "array.h"
#include "tifa_config.h"
```

**Defines**

- #define `_TIFA_FIRST_PRIMES_H_`
- #define `NFIRST_PRIMES` 65536

## Variables

- `const uint32_t first_primes[NFIRST_PRIMES]` [MAYBE\\_UNUSED](#)

### 5.13.1 Detailed Description

Precomputed small primes.

#### Author:

Automatically generated by `genprimes.pl`

#### Date:

Fri Jun 10 2011

#### Version:

2011-06-10

This is a list of the precomputed small primes together with a `uint32_array_t` wrapper.

Definition in file [first\\_primes.h](#).

### 5.13.2 Define Documentation

#### 5.13.2.1 `#define _TIFA_FIRST_PRIMES_H_`

Standard include guard.

Definition at line 36 of file `first_primes.h`.

#### 5.13.2.2 `#define NFIRST_PRIMES 65536`

Number of precomputed primes in the `first_primes` array.

Definition at line 47 of file `first_primes.h`.

### 5.13.3 Variable Documentation

#### 5.13.3.1 `const uint32_array_t first_primes_array` [MAYBE\\_UNUSED](#)

The `first_primes` array is a global array of `uint32_t` elements containing the first `NFIRST_PRIMES` prime numbers (from 2 and beyond).

The largest prime in the `first_primes` array.

`first_primes_array` is a `uint32_array_t` wrapper to the array `first_primes`.

#### Note:

`first_primes_array`'s `allocated` field is set to zero. Indeed, `first_primes_array` is merely a `uint32_array_t` wrapper for `first_primes`, and as such, it has no real "allocated" memory. Setting `first_primes_array.allocated` to 0 will prevent errors if `free_mmpz_array` is inadvertently called on `first_primes_array`.

Definition at line 58 of file `first_primes.h`.



## 5.14 funcs.h File Reference

Number theoretical, hash and comparison functions.

```
#include <limits.h>
#include <inttypes.h>
#include <math.h>
#include <gmp.h>
#include "macros.h"
#include "array.h"
#include "tifa_config.h"
```

### Data Structures

- struct [struct\\_mult\\_data\\_t](#)

*Ad hoc structure used in the computation of the multiplier to use.*

### Defines

- #define [\\_TIFA\\_FUNCS\\_H](#)
- #define [LARGEST\\_MULTIPLIER](#) 97
- #define [BITSIZE\\_LARGEST\\_MULTIPLIER](#) 7
- #define [MAX\\_IPRIME\\_IN\\_MULT\\_CALC](#) 31
- #define [NO\\_SQRT\\_MOD\\_P](#) (UINT32\_MAX)
- #define [NO\\_SQRT\\_MOD\\_P2](#) (ULONG\_MAX)

### Typedefs

- typedef struct [struct\\_mult\\_data\\_t](#) [mult\\_data\\_t](#)  
*Equivalent to struct [struct\\_mult\\_data\\_t](#).*

### Functions

- uint32\_t [most\\_significant\\_bit](#) (uint32\_t n)  
*Most significant bit of a positive integer.*
- static uint32\_t [floor\\_log2](#) (uint32\_t n)  
*Floor of logarithm in base 2 of a positive integer.*
- static uint32\_t [ceil\\_log2](#) (uint32\_t n)  
*Ceil of logarithm in base 2 of a positive integer.*
- static uint32\_t [ceil\\_log2\\_mp\\_limb](#) (mp\_limb\_t limb)  
*Ceil of logarithm in base 2 of a mp\_limb\_t.*

- void [find\\_coprime\\_base](#) (mpz\_array\_t \*const base, const mpz\_t n, const mpz\_array\_t \*const factors)  
*Find a coprime base from a list of factors.*
- int8\_t [kronecker\\_ui](#) (uint32\_t a, uint32\_t b)  
*Kronecker symbol restricted to positive simple precision integers.*
- uint32\_t [powm](#) (uint32\_t base, uint32\_t power, uint32\_t modulus)  
*Modular exponentiation restricted to positive simple precision integers.*
- uint32\_t [sqrtn](#) (uint32\_t a, uint32\_t p)  
*Shanks' algorithm for modular square roots computation.*
- static unsigned long int [is\\_square](#) (unsigned long int x)  
*Perfect square detection test.*
- bool [is\\_prime](#) (uint32\_t n)  
*Composition test for uint32\_t integers.*
- unsigned long int [gcd\\_ulint](#) (unsigned long int a, unsigned long int b)  
*Greatest common divisor for unsigned long int.*
- unsigned long int [modinv\\_ui](#) (unsigned long int n, unsigned long int p)  
*Modular inverse for unsigned long int.*
- unsigned long int [sqrtn\\_p2](#) (uint32\_t a, uint32\_t p)  
*Modular square root modulo the square of a prime.*
- uint32\_t [ks\\_multiplier](#) (const mpz\_t n, const uint32\_t size\_base)  
*Find best multiplier using the Knuth-Schroepfel function.*
- uint32\_t [hash\\_rj\\_32](#) (const void \*const keyptr)  
*Robert Jenkins' 32 bit mix function.*
- uint32\_t [hash\\_pjw](#) (const void \*const keyptr)  
*An hash function for strings.*
- uint32\_t [hash\\_sfh\\_ph](#) (const void \*const keyptr)  
*The "Super Fast Hash" function By Paul Hsieh.*
- int [mpz\\_cmp\\_func](#) (const void \*const mpza, const void \*const mpzb)  
*Comparison function between two mpz\_t.*
- int [uint32\\_cmp\\_func](#) (const void \*const uinta, const void \*const uintb)  
*Comparison function between two uint32\_t.*
- int [string\\_cmp\\_func](#) (const void \*const stra, const void \*const strb)  
*Comparison function between two strings.*
- int [cmp\\_mult\\_data](#) (const void \*mda, const void \*mdb)

*Comparison function between two mult\_data\_t.*

- `uint32_t n_choose_k (uint8_t n, uint8_t k)`  
*Binomial coefficient  $C(n, k)$  ( $n$  choose  $k$ ).*
- `void next_subset_lex (uint32_t n, uint32_t k, uint32_t *subset, bool *end)`  
*Generate the successor of a fixed cardinal subset from a base set, in lexicographic order.*
- `void unrank_subset_lex (uint32_t n, uint32_t k, uint32_t r, uint32_t *subset)`  
*Generate a fixed cardinal subset from a base set, according to a given rank.*
- `void unrank_subset_revdoor (uint32_t n, uint32_t k, uint32_t r, uint32_t *subset)`  
*Generate a fixed cardinal subset from a base set, according to a given rank.*
- `void tifa_srand (uint32_t seed)`  
*Initializes TIFA's basic pseudo-random generator.*
- `uint32_t tifa_rand ()`  
*Returns a pseudo-random integer.*

## Variables

- `const unsigned short qres_mod_221[221] MAYBE_UNUSED`  
*Quadratic residues mod 221.*

### 5.14.1 Detailed Description

Number theoretical, hash and comparison functions.

#### Author:

Jerome Milan

#### Date:

Fri Jun 10 2011

#### Version:

2011-06-10

Defines several number theoretical functions, hash functions and comparison functions.

Definition in file [funcs.h](#).

### 5.14.2 Define Documentation

#### 5.14.2.1 `#define _TIFA_FUNCS_H_`

Standard include guard.

Definition at line 36 of file [funcs.h](#).

**5.14.2.2 #define BITSIZE\_LARGEST\_MULTIPLIER 7**

Size in bits of the largest multiplier allowed.

Definition at line 61 of file funcs.h.

**5.14.2.3 #define LARGEST\_MULTIPLIER 97**

Largest multiplier allowed.

Definition at line 55 of file funcs.h.

**5.14.2.4 #define MAX\_IPRIME\_IN\_MULT\_CALC 31**

The `MAX_IPRIME_IN_MULT_CALC`-th smallest prime number is the largest prime used in the determination of the best multiplier.

Definition at line 68 of file funcs.h.

**5.14.2.5 #define NO\_SQRT\_MOD\_P (UINT32\_MAX)**

Value returned by the `sqrtn(n, p)` function if no modular square root of  $n \bmod p$  exists.

Definition at line 248 of file funcs.h.

**5.14.2.6 #define NO\_SQRT\_MOD\_P2 (ULONG\_MAX)**

Value returned by the `sqrtn_p2(n, p)` function if no modular square root of  $n \bmod p \cdot p$  exists.

Definition at line 255 of file funcs.h.

**5.14.3 Function Documentation****5.14.3.1 static uint32\_t ceil\_log2 (uint32\_t n) [inline, static]**

Ceil of logarithm in base 2 of a positive integer.

Returns the value of the ceil of the logarithm (in base 2) of a positive integer in essentially constant time. In other words, it returns the smallest natural  $i$  such that  $2^i \geq n$ .

**Parameters:**

←  $n$  A positive integer.

**Returns:**

Ceil of  $\log(n)$  in base 2.

Definition at line 162 of file funcs.h.

References `IS_POWER_OF_2_UI`, and `most_significant_bit()`.

Referenced by `ceil_log2_mp_limb()`.

**5.14.3.2 static uint32\_t ceil\_log2\_mp\_limb (mp\_limb\_t limb) [inline, static]**

Ceil of logarithm in base 2 of a `mp_limb_t`.

Returns the value of the ceil of the logarithm (in base 2) of a `mp_limb_t` in essentially constant time. In other words, it returns the smallest natural  $i$  such that  $2^i \geq n$ .

**Parameters:**

← *n* A positive integer as an `mp_limb_t`.

**Returns:**

Ceil of  $\log(n)$  in base 2.

Definition at line 180 of file `funcs.h`.

References `ceil_log2()`.

**5.14.3.3 `int cmp_mult_data (const void * mda, const void * mdb)`**

Comparison function between two `mult_data_t`.

This is a comparison function between two `mult_data_t` structures passed as pointers to `void`, according to the criteria set forth in Morrison and Brillhart's paper "A Method of Factoring and the Factorization of  $F_7$ " (Mathematics of Computation, vol 29, #129, Jan 1975, pages 183-205).

If *a* and *b* are the two underlying `mult_data_t` structures to compare, it returns:

- 1 if `a.count > b.count`
- -1 if `a.count < b.count`
- If `a.count == b.count`, returns:
  - 1 if `a.sum_inv_pi > b.sum_inv_pi`
  - -1 if `a.sum_inv_pi < b.sum_inv_pi`
  - If `a.sum_inv_pi == b.sum_inv_pi`, returns:
    - \* 1 if `a.multiplier < b.multiplier` (Indeed, we prefer smaller multipliers)
    - \* -1 if `a.multiplier > b.multiplier`
    - \* 0 if `a.multiplier == b.multiplier`

**Parameters:**

← *mda* A pointer to the first `mult_data_t` to compare.

← *mdb* A pointer to the second `mult_data_t` to compare.

**Returns:**

The comparison between the two `mult_data_t`.

**5.14.3.4 `void find_coprime_base (mpz_array_t *const base, const mpz_t n, const mpz_array_t *const factors)`**

Find a coprime base from a list of factors.

Finds a coprime base for the list of factors of *n* given by the array *factors* and stores it in the allocated but *uninitialized* array *base*. After invocation, we know that *n* is smooth on the returned computed base and that all elements of the base are coprime to each other.

The resulting base is obtained:

1. by completing the list of original factors with their cofactors,

2. by keeping only factors (or non-trivial divisors of factors) coprime to all others.

**Warning:**

There is absolutely no guarantee that the returned base elements are prime. If, by chance, the base only contains primes then it means that we have found the complete factorization of  $n$  (up to the prime multiplicities).

**Note:**

If the `base` array has not enough room to hold all the coprimes found, it will be resized via a call to `resize_mpz_array` with `ELONGATION` extra `mpz_t` slots to avoid too frequent resizes. Consecutive invocation of this function with the same `base` and `n` but for different `factors` arrays will build a coprime base for all elements in all the aforementioned `factors` arrays.

**Parameters:**

- ↔ *base* The found coprime base.
- ← *n* A positive integer.
- ← *factors* A pointer to an array holding some factors of  $n$ .
- ↔ *A* pointer to the *uninitialized* `mpz_array_t` to hold the coprime base.

**5.14.3.5 static uint32\_t floor\_log2 (uint32\_t n) [inline, static]**

Floor of logarithm in base 2 of a positive integer.

Returns the value of the floor of the logarithm (in base 2) of a positive integer in essentially constant time. In other words, it returns the greatest natural  $i$  such that  $2^i \leq n$ .

**Note:**

This is actually just a call to `most_significant_bit`.

**Parameters:**

- ← *n* A positive integer.

**Returns:**

Floor of  $\log(n)$  in base 2.

Definition at line 148 of file `funcs.h`.

References `most_significant_bit()`.

**5.14.3.6 unsigned long int gcd\_ulint (unsigned long int a, unsigned long int b)**

Greatest common divisor for unsigned long int.

Returns the greatest common divisor of  $a$  and  $b$  as an unsigned long int.

**Parameters:**

- ← *a* An unsigned long int.
- ← *b* An unsigned long int.

**Returns:**

The greatest common divisor of  $a$  and  $b$ .

**5.14.3.7 `uint32_t hash_pjw (const void *const keyptr)`**

An hash function for strings.

Returns the hash of a C-style character string (passed as a pointer to `void`) using an hash function attributed to P.J. Weinberger.

**Note:**

This hash function and its implementation is extracted from the famous Dragon book: "Compilers: Principles, Techniques and Tools", Aho, Sethi, & Ullman.

**Parameters:**

← *keyptr* A pointer to the character string to hash.

**Returns:**

The value of the hash function.

**5.14.3.8 `uint32_t hash_rj_32 (const void *const keyptr)`**

Robert Jenkins' 32 bit mix function.

Returns the hash of a `uint32_t` integer (passed as a pointer to `void`) using Robert Jenkins' 32 bit mix function.

**See also:**

<http://www.concentric.net/~Ttwang/tech/inthash.htm>

**Parameters:**

← *keyptr* A pointer to the `uint32_t` to hash.

**Returns:**

The value of the hash function.

**5.14.3.9 `uint32_t hash_sfh_ph (const void *const keyptr)`**

The "Super Fast Hash" function By Paul Hsieh.

Returns the hash of a C-style character string (passed as a pointer to `void`) using the so-called "Super-FastHash" function By Paul Hsieh.

**See also:**

<http://www.azillionmonkeys.com/qed/hash.html>

**Parameters:**

← *keyptr* A pointer to the character string to hash.

**Returns:**

The value of the hash function.

### 5.14.3.10 `bool is_prime (uint32_t n)`

Composition test for `uint32_t` integers.

Returns `false` if `n` is definitely composite. Returns `true` if `n` is *probably* prime.

#### Note:

This is actually a basic Miller-Rabin composition test with `NMILLER_RABIN` iterations preceded with some trial divisions if `n` is sufficiently small.

#### Parameters:

← `n` The `uint32_t` to be checked for composition.

#### Returns:

Returns `false` if `n` is found to be definitely composite. `true` otherwise.

### 5.14.3.11 `static unsigned long int is_square (unsigned long int x) [inline, static]`

Perfect square detection test.

Returns `sqrt(x)` if and only if `x` is a perfect square. Returns 0 otherwise.

#### Parameters:

← `x` The integer to test.

#### Returns:

`sqrt(x)` if `x` is a perfect square. 0 otherwise.

Definition at line 335 of file `funcs.h`.

### 5.14.3.12 `int8_t kronecker_ui (uint32_t a, uint32_t b)`

Kronecker symbol restricted to positive simple precision integers.

Returns the value of the Kronecker symbol ( $a/b$ ) where `a` and `b` are positive integers.

#### Parameters:

← `a` A positive integer.

← `b` A positive integer.

#### Returns:

The value of the kronecker symbol ( $a/b$ ).

### 5.14.3.13 `uint32_t ks_multiplier (const mpz_t n, const uint32_t size_base)`

Find best multiplier using the Knuth-Schroepfel function.

Given the size of factor base `size_base`, returns the "best" multiplier to factor `n`, using the modified version of the Knuth-Schroepfel function described by Silverman in: "The Multiple Quadratic Sieve".



**Note:**

The greatest multiplier considered is given by `LARGEST_MULTIPLIER`.

**See also:**

"The Multiple Quadratic Sieve", Robert D. Silverman, *Mathematics of Computation*, Volume 48, Number 177, January 1987, pages 329-339.

**Parameters:**

- ← *n* The number to factor
- ← *size\_base* The desired size of the factor base

**Returns:**

The "best" multiplier to factor *n*.

**5.14.3.14 unsigned long int modinv\_ui (unsigned long int *n*, unsigned long int *p*)**

Modular inverse for unsigned long int.

Returns the modular inverse of *n* modulo the odd prime *p* as an unsigned long int.

**Warning:**

*p* must be a positive odd prime, strictly less than `LONG_MAX` (yes, `LONG_MAX` and not `ULONG_MAX`!) and, of course,  $n \% p$  must be non-null.

**Parameters:**

- ← *n* An unsigned long int.
- ← *p* An odd prime unsigned long int.

**Returns:**

The modular inverse of  $n \bmod p$ .

**5.14.3.15 uint32\_t most\_significant\_bit (uint32\_t *n*)**

Most significant bit of a positive integer.

Returns the value of the most significant bit of the integer *n* in essentially constant time, or in other words, its logarithm in base 2. The returned result is an integer from 0 (the least significant bit) to 31 included (the most significant bit).

**Note:**

This function is adapted from public domain code from the Bit Twiddling Hacks web page: <http://graphics.stanford.edu/~seander/bithacks.html>

**Parameters:**

- ← *n* A positive integer.

**Returns:**

$\log_2(n)$  in base 2.

Referenced by `ceil_log2()`, and `floor_log2()`.

#### 5.14.3.16 int mpz\_cmp\_func (const void \*const *mpza*, const void \*const *mpzb*)

Comparison function between two `mpz_t`.

This is a natural order comparison function between two `mpz_t` elements passed as pointers to `void`. It returns:

- 1 if the first `mpz_t` is greater than the second one.
- 0 if the first `mpz_t` is equal to the second one.
- -1 if the first `mpz_t` is less than the second one.

#### Note:

This function is actually nothing more than a wrapper for `mpz_cmp`.

#### Parameters:

- ← *mpza* A pointer to a `mpz_t`.
- ← *mpzb* A pointer to another `mpz_t`.

#### Returns:

The comparison between the two `mpz_t`.

#### 5.14.3.17 uint32\_t n\_choose\_k (uint8\_t *n*, uint8\_t *k*)

Binomial coefficient  $C(n, k)$  ( $n$  choose  $k$ ).

Returns the binomial coefficient  $C(n, k)$  (i.e  $n$  choose  $k$ ).

Note that this single precision function only returns correct results if the actual value of the binomial coefficient fits in 32 bits.

#### Parameters:

- ← *n*
- ← *k*

#### Returns:

The binomial coefficient  $C(n, k)$ .

#### 5.14.3.18 void next\_subset\_lex (uint32\_t *n*, uint32\_t *k*, uint32\_t \* *subset*, bool \* *end*)

Generate the successor of a fixed cardinal subset from a base set, in lexicographic order.

Starting with a subset of cardinal  $k$  of a base set of cardinal  $n$ , generates the subset's successor in the lexicographic order. The new subset is stored in `subset` and thus overrides the previous one.

Subsets are described by an array of length  $k$  holding indexes in the interval  $[1, n]$ .

The first  $k$ -subset in the lexicographic order is given by  $\{1, 2, 3, \dots, k\}$ . After a call to `next_subset_lex` `end` is `true` if and only if the last  $k$ -subset has been reached (i.e. the next one will be  $\{1, 2, 3, \dots, k\}$ ).

This is actually algorithm 2.6 from the book "*Combinatorial Algorithms - Generation, Enumeration, and Search*" by Donald L. Kreher and Douglas Stinson.

**Parameters:**

- ← *n* Cardinal of the base set.
- ← *k* Cardinal of the subset.
- in/out]* subset Current subset to be replaced by its successor.
- ← *end* Have we reached the end of the cycle?

**5.14.3.19 `uint32_t powm (uint32_t base, uint32_t power, uint32_t modulus)`**

Modular exponentiation restricted to positive simple precision integers.

Returns  $(base^{power}) \bmod modulus$  as an unsigned integer.

**Parameters:**

- ← *base* The base of the modular exponential.
- ← *power* The power of the modular exponential.
- ← *modulus* The modulus of the modular exponential.

**Returns:**

The modular exponential  $(base^{power}) \bmod modulus$ .

**5.14.3.20 `uint32_t sqrtm (uint32_t a, uint32_t p)`**

Shanks' algorithm for modular square roots computation.

Returns the modular square root of  $a \pmod{p}$  (where  $p$  is an *odd prime*) using Shanks' algorithm, that is, returns the positive integer  $s$  such that  $s^2 = a \pmod{p}$ . If no such integer exists, returns `NO_SQRT_MOD_P`.

**Warning:**

The primality of  $p$  is not checked by `sqrtm`. It is the responsibility of the caller to check whether  $p$  is indeed prime. Failure to assure such a precondition will lead to an infinite loop.

**Parameters:**

- ← *a* The modular square.
- ← *p* The modulus.

**Returns:**

The modular square root of  $a \pmod{p}$  if it exists. `NO_SQRT_MOD_P` otherwise.

**5.14.3.21 `unsigned long int sqrtm_p2 (uint32_t a, uint32_t p)`**

Modular square root modulo the square of a prime.

Provided that  $a$  verifies  $1 \leq a < p * p$ , returns the modular square root of  $a \pmod{p * p}$  (where  $p$  is an *odd prime*) that is, returns a positive integer  $s$  such that  $s^2 = a \pmod{p * p}$ . If no such integer exists, returns `NO_SQRT_MOD_P2`.

**Warning:**

In order to use only single precision computation, the product  $p*p$  should be strictly less than `LONG_MAX`.

The primality of  $p$  is not checked by `sqrtm_p2`. It is the responsibility of the caller to check whether  $p$  is indeed prime. Failure to assure such a precondition will lead to an infinite loop.

**Parameters:**

- ←  $a$  The modular square.
- ←  $p$  The square root of the modulus.

**Returns:**

The modular square root of  $a \pmod{p*p}$  if it exists. `NO_SQRT_MOD_P2` otherwise.

**5.14.3.22 `int string_cmp_func (const void *const stra, const void *const strb)`**

Comparison function between two strings.

This is a lexicographical order comparison function between two C-style character strings passed as pointers to `void`. It returns:

- 1 if the first string is greater than the second one.
- 0 if the first string is equal to the second one.
- -1 if the first string is less than the second one.

**Note:**

This function is actually nothing more than a wrapper for `strcmp`.

**Parameters:**

- ← *stra* A pointer to a C-style character string.
- ← *strb* A pointer to another C-style character string.

**Returns:**

The lexicographical comparison between the two strings.

**5.14.3.23 `uint32_t tifa_rand ()`**

Returns a pseudo-random integer.

Returns a pseudo-random integer using TIFA's basic random number generator.

**Parameters:**

- ← *seed* The seed as a `uint32_t`.

#### 5.14.3.24 void tifa\_srand (uint32\_t seed)

Initializes TIFA's basic pseudo-random generator.

Initializes TIFA's basic random number generator with a user defined seed.

##### Parameters:

← *seed* The seed as a `uint32_t`.

#### 5.14.3.25 int uint32\_cmp\_func (const void \*const uinta, const void \*const uintb)

Comparison function between two `uint32_t`.

This is a natural order comparison function between two `uint32_t` elements passed as pointers to `void`. It returns:

- 1 if the first `uint32_t` is greater than the second one.
- 0 if the first `uint32_t` is equal to the second one.
- -1 if the first `uint32_t` is less than the second one.

##### Parameters:

← *uinta* A pointer to a `uint32_t`.

← *uintb* A pointer to another `uint32_t`.

##### Returns:

The comparison between the two `uint32_t`.

#### 5.14.3.26 void unrank\_subset\_lex (uint32\_t n, uint32\_t k, uint32\_t r, uint32\_t \*subset)

Generate a fixed cardinal subset from a base set, according to a given rank.

Starting with a base set of cardinal  $n$ , constructs a subset of cardinal  $k$  and rank  $r$  (in  $[0, c(n, k)]$ ) where the rank is given by the lexicographic order. The constructed subset is stored in `subset` and thus overrides the previous data.

Subsets are described by an array of length  $k$  holding indexes in the interval  $[1, n]$ .

This is actually algorithm 2.8 from the book "*Combinatorial Algorithms - Generation, Enumeration, and Search*" by Donald L. Kreher and Douglas Stinson.

##### Parameters:

← *n* Cardinal of the base set.

← *k* Cardinal of the subset.

← *r* Rank of the subset (assuming lexicographic order).

→ *subset* Subset to be returned.

**5.14.3.27 void unrank\_subset\_revdoor (uint32\_t n, uint32\_t k, uint32\_t r, uint32\_t \* subset)**

Generate a fixed cardinal subset from a base set, according to a given rank.

Starting with a base set of cardinal  $n$ , constructs a subset of cardinal  $k$  and rank  $r$  (in  $[0, c(n, k)]$ ) where the rank is given by the minimal change order. The constructed subset is stored in `subset` and thus overrides the previous data.

Subsets are described by an array of length  $k$  holding indexes in the interval  $[1, n]$ .

This is actually algorithm 2.12 from the book *"Combinatorial Algorithms - Generation, Enumeration, and Search"* by Donald L. Kreher and Douglas Stinson.

**Parameters:**

- ←  $n$  Cardinal of the base set.
- ←  $k$  Cardinal of the subset.
- ←  $r$  Rank of the subset (assuming minimal change order).
- `subset` Subset to be returned.

**5.14.4 Variable Documentation****5.14.4.1 const uint32\_array\_t first\_primes\_array MAYBE\_UNUSED**

Quadratic residues mod 221.

Quadratic residues mod 315.

Quadratic residues mod 256.

$x$  is a square mod 221 if `qres_mod_221[x % 221] == 1`.

$x$  is a square mod 256 if `qres_mod_256[x % 256] == 1`.

$x$  is a square mod 315 if `qres_mod_315[x % 315] == 1`.

The largest prime in the `first_primes` array.

`first_primes_array` is a `uint32_array_t` wrapper to the array `first_primes`.

**Note:**

`first_primes_array`'s allocated field is set to zero. Indeed, `first_primes_array` is merely a `uint32_array_t` wrapper for `first_primes`, and as such, it has no real "allocated" memory. Setting `first_primes_array.allocated` to 0 will prevent errors if `free_mpz_array` is inadvertently called on `first_primes_array`.

Definition at line 317 of file `funcs.h`.

**5.15 gauss\_elim.h File Reference**

Gaussian elimination over GF(2) (from a paper by D. Parkinson and M. Wunderlich).

```
#include <inttypes.h>
```

```
#include "matrix.h"
```

```
#include "x_array_list.h"
```

## Defines

- #define [\\_TIFA\\_GAUSS\\_ELIM\\_H\\_](#)

## Functions

- void [gaussian\\_elim](#) ([uint32\\_array\\_list\\_t](#) \*relations, [binary\\_matrix\\_t](#) \*const matrix)  
*Gaussian elimination on a [binary\\_matrix\\_t](#).*

### 5.15.1 Detailed Description

Gaussian elimination over GF(2) (from a paper by D. Parkinson and M. Wunderlich).

#### Author:

Jerome Milan

#### Date:

Fri Jun 10 2011

#### Version:

2011-06-10

Gaussian elimination over GF(2) as presented in the paper "A compact algorithm for Gaussian elimination over GF(2) implemented on highly parallel computers" written by Dennis Parkinson and Marvin Wunderlich (*Parallel Computing* 1, 1984).

#### See also:

"A compact algorithm for Gaussian elimination over GF(2) implemented on highly parallel computers", D. Parkinson and M. Wunderlich, *Parallel Computing* 1, 1984, pages 65-73.

Definition in file [gauss\\_elim.h](#).

### 5.15.2 Define Documentation

#### 5.15.2.1 #define [\\_TIFA\\_GAUSS\\_ELIM\\_H\\_](#)

Standard include guard.

Definition at line 43 of file [gauss\\_elim.h](#).

### 5.15.3 Function Documentation

#### 5.15.3.1 void [gaussian\\_elim](#) ([uint32\\_array\\_list\\_t](#) \*relations, [binary\\_matrix\\_t](#) \*const matrix)

Gaussian elimination on a [binary\\_matrix\\_t](#).

Performs a gaussian elimination on a [binary\\_matrix\\_t](#) as described in the paper "A compact algorithm for Gaussian elimination over GF(2) implemented on highly parallel computers", by D. Parkinson and M. Wunderlich (*Parallel Computing* 1 (1984) 65-73).

Solutions (if any) of this linear system are stored in `relations` where each entry is a `uint32_array_t` containing the indexes of the rows (from the *original* matrix) composing a solution. In other words, for each entry, the sum of the indexed rows (from the original matrix) is a nul binary vector.

#### Parameters:

- ← *matrix* A pointer to the `binary_matrix_t` giving the linear system to solve.
- *relations* A pointer to a `uint32_array_list_t` holding the solutions of the system, if any.

## 5.16 gmp\_utils.h File Reference

Various GMP small utilities.

```
#include <gmp.h>
#include "hashtable.h"
```

### Data Structures

- struct [struct\\_mpz\\_pair\\_t](#)  
A pair of `mpz_t` integers.

### Defines

- `#define` [\\_TIFA\\_GMP\\_UTILS\\_H\\_](#)

### Typedefs

- typedef struct [struct\\_mpz\\_pair\\_t](#) `mpz_pair_t`  
Equivalent to struct [struct\\_mpz\\_pair\\_t](#).

### Functions

- static void [init\\_mpz\\_pair](#) (`mpz_pair_t` \*pair)  
*inits* a `mpz_pair_t`.
- static void [clear\\_mpz\\_pair](#) (`mpz_pair_t` \*pair)  
*Clears* a `mpz_pair_t`.
- void [empty\\_mpzpair\\_htable](#) (`hashtable_t` \*const htable)  
*Empties* a `hashtable_t` holding `mpz_pair_t`'s.
- static void [free\\_mpzpair\\_htable](#) (`hashtable_t` \*htable)  
*Clears* a `hashtable_t` holding `mpz_pair_t`'s.
- float [mpz\\_log10](#) (`mpz_t` n)  
*Logarithm in base 10 of a multi-precision integer.*



### 5.16.1 Detailed Description

Various GMP small utilities.

**Author:**

Jerome Milan

**Date:**

Fri Jun 10 2011

**Version:**

2011-06-10

GMP small utilities' definitions should go here.

Definition in file [gmp\\_utils.h](#).

### 5.16.2 Define Documentation

#### 5.16.2.1 #define \_TIFA\_GMP\_UTILS\_H\_

Standard include guard.

Definition at line 35 of file [gmp\\_utils.h](#).

### 5.16.3 Function Documentation

#### 5.16.3.1 static void clear\_mpz\_pair (mpz\_pair\_t \*pair) [inline, static]

Clears a `mpz_pair_t`.

Clears a `mpz_pair_t`.

**Parameters:**

← *pair* A pointer to the `mpz_pair_t` to clear.

Definition at line 87 of file [gmp\\_utils.h](#).

References `struct_mpz_pair_t::x`, and `struct_mpz_pair_t::y`.

#### 5.16.3.2 void empty\_mpzpair\_htable (hashtable\_t \*const htable)

Empties a `hashtable_t` holding `mpz_pair_t`'s.

Empties a `hashtable_t` holding `mpz_pair_t`'s and clears the memory associated to the keys and their associated data.

**Parameters:**

← *htable* A pointer to the `hashtable_t` to empty.

Referenced by `free_mpzpair_htable()`.

### 5.16.3.3 static void free\_mpzpair\_htable (hashtable\_t \* htable) [inline, static]

Clears a hashtable\_t holding mpz\_pair\_t's.

Clears a hashtable\_t holding mpz\_pair\_t's. It clears the memory associated to the keys, their associated data and the hashtable itself.

#### Parameters:

← *htable* A pointer to the hashtable\_t to clear.

Definition at line 111 of file gmp\_utils.h.

References empty\_mpzpair\_htable(), and free\_hashtable().

### 5.16.3.4 static void init\_mpz\_pair (mpz\_pair\_t \* pair) [inline, static]

inits a mpz\_pair\_t.

Inits a mpz\_pair\_t by initializing each of its mpz\_t element.

#### Parameters:

← *pair* A pointer to the mpz\_pair\_t to init.

Definition at line 75 of file gmp\_utils.h.

References struct\_mpz\_pair\_t::x, and struct\_mpz\_pair\_t::y.

### 5.16.3.5 float mpz\_log10 (mpz\_t n)

Logarithm in base 10 of a multi-precision integer.

Returns an *crude approximation* of the logarithm (in base 10) of a positive multi-precision integer n. The approximation is usually valid up to the 4th decimal.

#### Parameters:

← *n* A positive multi-precision integer.

#### Returns:

An approximation of log(n) in base 10.

## 5.17 hashtable.h File Reference

Generic hashtable.

```
#include <inttypes.h>
#include "linked_list.h"
```

### Data Structures

- struct [struct\\_hashtable\\_t](#)  
*A basic implementation of a hashtable.*
- struct [struct\\_hashtable\\_entry\\_t](#)  
*The structure of a hashtable's entry.*

## Defines

- `#define _TIFA_HASHTABLE_H_`

## Typedefs

- typedef struct `struct_hashtable_t` `hashtable_t`  
*Equivalent to struct `struct_hashtable_t`.*
- typedef struct `struct_hashtable_entry_t` `hashtable_entry_t`  
*Equivalent to struct `struct_hashtable_entry_t`.*

## Functions

- `hashtable_t * alloc_init_hashtable` (`uint32_t` size, `int(*cmp_func)(const void *const key_a, const void *const key_b)`, `uint32_t(*hash_func)(const void *const key)`)  
*Allocates and returns a new `hashtable_t`.*
- void `free_hashtable` (`hashtable_t *htable`)  
*Clears a `hashtable_t`.*
- void `add_entry_in_hashtable` (`hashtable_t *const htable`, `const void *const key`, `const void *const data`)  
*Adds an entry in a `hashtable_t`.*
- void \* `get_entry_in_hashtable` (`hashtable_t *const htable`, `const void *const key`)  
*Gets an entry's data from a `hashtable_t`.*
- void \* `remove_entry_in_hashtable` (`hashtable_t *const htable`, `const void *const key`)  
*Removes an entry from a `hashtable_t`.*

### 5.17.1 Detailed Description

Generic hashtable.

**Author:**

Jerome Milan

**Date:**

Fri Jun 10 2011

**Version:**

2011-06-10

Yet another implementation of a generic hashtable.

Definition in file [hashtable.h](#).

## 5.17.2 Define Documentation

### 5.17.2.1 #define \_TIFA\_HASHTABLE\_H\_

Standard include guard.

Definition at line 35 of file hashtable.h.

## 5.17.3 Function Documentation

### 5.17.3.1 void add\_entry\_in\_hashtable (hashtable\_t \*const *htable*, const void \*const *key*, const void \*const *data*)

Adds an entry in a `hashtable_t`.

Creates an entry with its `data` field given by the pointer `data` and its `key` field given by the pointer `key` and adds it in a `hashtable_t`.

#### Warning:

This function does not copy the actual content of the variable referenced by `key` and `data` but merely copies these references in the `hashtable_entry_t` structure.

#### Parameters:

- ← *htable* A pointer to the `hashtable_t`.
- ← *key* A pointer to the key of the new entry.
- ← *data* A pointer to the data of the new entry.

### 5.17.3.2 hashtable\_t\* alloc\_init\_hashtable (uint32\_t *size*, int(\*) (const void \*const *key\_a*, const void \*const *key\_b*) *cmp\_func*, uint32\_t(\*) (const void \*const *key*) *hash\_func*)

Allocates and returns a new `hashtable_t`.

Allocates and returns a pointer to a new `hashtable_t` with `size` allocated buckets, using the comparison function pointed by `cmp_func` and the hash function given by `hash_func`.

#### Note:

If `size` is not a power of two, the lowest power of two greater than `size` is used instead.

#### Parameters:

- ← *size* The number of allocated buckets.
- ← *cmp\_func* A pointer to the comparison function.
- ← *hash\_func* A pointer to the hash function.

### 5.17.3.3 void free\_hashtable (hashtable\_t \* *htable*)

Clears a `hashtable_t`.

Clears the `hashtable_t` pointed by `htable`.

**Warning:**

This function merely clears the memory used by the linked lists but *does not* frees the memory space used by the `key` and `data` pointers of the `hashtable_entry_t`.

Do not call `free(htable)` in client code after a call to `free_hashtable(htable)`: it would result in an error.

**Parameters:**

← *htable* A pointer to the `hashtable_t` to clear.

Referenced by `free_mpzpair_htable()`.

**5.17.3.4 void\* get\_entry\_in\_hashtable (hashtable\_t \*const htable, const void \*const key)**

Gets an entry's data from a `hashtable_t`.

Gets the `data` field of the entry from the hashtable `htable` whose key is given by `key`.

**Parameters:**

← *htable* A pointer to the `hashtable_t`.

← *key* A pointer to the key of the entry to read.

**Returns:**

The `data` field of the entry whose key is given by `key`, if any.

NULL if no such entry is found in the hashtable.

**5.17.3.5 void\* remove\_entry\_in\_hashtable (hashtable\_t \*const htable, const void \*const key)**

Removes an entry from a `hashtable_t`.

Removes the entry from the hashtable `htable` whose key is given by `key` and returns its `data` field.

**Warning:**

The `key` field of the removed entry is freed if a matching entry is found. This means that if `key` is a pointer to a structure containing some other pointers, all the memory may not be freed since the real type of `key` is not known by the hashtable. This is why it is strongly recommended to use *only* pointers to integers or strings as keys.

**Parameters:**

← *htable* A pointer to the `hashtable_t`.

← *key* A pointer to the key of the entry to remove.

**Returns:**

The `data` field of the removed entry.

NULL if no matching entry is found in the hashtable.

## 5.18 lindep.h File Reference

Functions used in the resolution of the linear systems.

```
#include <inttypes.h>
#include "array.h"
#include "x_array_list.h"
#include "matrix.h"
#include "exit_codes.h"
```

### Defines

- `#define \_TIFA\_LINDEP\_H`

### Typedefs

- typedef enum [linalg\\_method\\_enum](#) [linalg\\_method\\_t](#)  
*Equivalent to* enum [linalg\\_method\\_enum](#).

### Enumerations

- enum [linalg\\_method\\_enum](#) { [SMART\\_GAUSS\\_ELIM](#) = 0 }

### Functions

- void [fill\\_matrix\\_trial\\_div](#) ([binary\\_matrix\\_t](#) \*const matrix, [mpz\\_array\\_t](#) \*const partially\_factored, const [mpz\\_array\\_t](#) \*const to\_factor, const [uint32\\_array\\_t](#) \*const factor\_base)  
*Fills a binary matrix via trial divisions.*
- void [fill\\_trial\\_div\\_decomp](#) ([binary\\_matrix\\_t](#) \*const matrix, [byte\\_matrix\\_t](#) \*const decomp\_matrix, [mpz\\_array\\_t](#) \*const partially\_factored, const [mpz\\_array\\_t](#) \*const to\_factor, const [uint32\\_array\\_t](#) \*const factor\_base)  
*Similar to* [fill\\_matrix\\_trial\\_div](#) *but also stores valuations.*
- void [fill\\_matrix\\_from\\_list](#) ([binary\\_matrix\\_t](#) \*const matrix, const [mpz\\_array\\_t](#) \*const smooth\_array, const [uint32\\_array\\_list\\_t](#) \*const list, const [uint32\\_array\\_t](#) \*const factor\_base)  
*Fills a binary matrix from a list of factors.*
- void [fill\\_matrix\\_from\\_list\\_decomp](#) ([binary\\_matrix\\_t](#) \*const matrix, [byte\\_matrix\\_t](#) \*const decomp\_matrix, const [mpz\\_array\\_t](#) \*const smooth\_array, const [uint32\\_array\\_list\\_t](#) \*const list, const [uint32\\_array\\_t](#) \*const factor\_base)  
*Similar to* [fill\\_matrix\\_from\\_list](#) *but also stores valuations.*
- [uint32\\_array\\_list\\_t](#) \* [find\\_dependencies](#) ([binary\\_matrix\\_t](#) \*const matrix, [linalg\\_method\\_t](#) method)  
*Solves a linear system over GF(2).*
- [ecode\\_t](#) [find\\_factors](#) ([mpz\\_array\\_t](#) \*const factors, const [mpz\\_t](#) n, const [mpz\\_array\\_t](#) \*const xi\_array, const [mpz\\_array\\_t](#) \*const yi\_array, const [uint32\\_array\\_list\\_t](#) \*const dependencies)

*Find factors of an integer from congruence relations.*

- `ecode_t find_factors_decomp` (`mpz_array_t` \*const factors, const `mpz_t` n, const `mpz_array_t` \*const xi\_array, const `byte_matrix_t` \*const yi\_decomp\_matrix, const `uint32_array_list_t` \*const dependencies, const `uint32_array_t` \*const factor\_base)

*Similar to `find_factors` but uses the factorization of each `y_i`.*

## Variables

- static const char \*const `linalg_method_to_str` [1]

### 5.18.1 Detailed Description

Functions used in the resolution of the linear systems.

#### Author:

Jerome Milan

#### Date:

Fri Jun 10 2011

#### Version:

2011-06-10

Functions used in the resolution of the linear systems over GF(2) found in factorization problems and in the very last stage of the factorization process (determination of factors after linear algebra phase).

Definition in file [lindep.h](#).

### 5.18.2 Define Documentation

#### 5.18.2.1 `#define _TIFA_LINDEP_H_`

Standard include guard.

Definition at line 37 of file `lindep.h`.

### 5.18.3 Enumeration Type Documentation

#### 5.18.3.1 `enum linalg_method_enum`

Enumeration listing the different linear system resolution method implemented.

For the time being, only one method is available.

#### Enumerator:

`SMART_GAUSS_ELIM` "Smart" gaussian elimination described in: "A compact algorithm for Gaussian elimination over GF(2) implemented on highly parallel computers", by D. Parkinson and M. Wunderlich (Parallel Computing 1 (1984) 65-73).

Definition at line 58 of file `lindep.h`.

## 5.18.4 Function Documentation

### 5.18.4.1 void fill\_matrix\_from\_list (binary\_matrix\_t \*const matrix, const mpz\_array\_t \*const smooth\_array, const uint32\_array\_list\_t \*const list, const uint32\_array\_t \*const factor\_base)

Fills a binary matrix from a list of factors.

Fills the binary matrix `matrix` from a previously computed list giving all known factors.

#### Note:

`list` contains the previously computed factors of each integers in `smooth_array`, in other words, we know that `smooth_array->data[i]` is divisible by all the integers of the `uint32_array_t` given by `list->data[i]`.

The binary matrix is filled so that:

- There is a '1' in the (i-th row, 1st col) position in the matrix if `smooth_factor->data[i]` is negative.
- There is a '1' in the (i-th row, j-th col) position in the matrix if `smooth_factor->data[i]` is divisible by an odd power of `list->data[i]->data[k]`. Here `j` is found so that `factor_base->data[j] = list->data[i]->data[k]`.
- In all other cases, the (i-th row, j-th col) position in the matrix contains a 0.

#### Parameters:

- *matrix* A pointer to the binary matrix to fill.
- *smooth\_array* A pointer to the array giving the integers to factor.
- ← *list* A pointer to the factor list for each integer to factor.
- ← *factor\_base* A pointer to the array listing the integers to trial divide by.

### 5.18.4.2 void fill\_matrix\_from\_list\_decomp (binary\_matrix\_t \*const matrix, byte\_matrix\_t \*const decomp\_matrix, const mpz\_array\_t \*const smooth\_array, const uint32\_array\_list\_t \*const list, const uint32\_array\_t \*const factor\_base)

Similar to `fill_matrix_from_list` but also stores valuations.

Fills the binary matrix `matrix` from a previously computed list giving all known factors.

Also stores in `decomp_matrix` the valuation of each integer from `smooth_array` for each prime in the factor base. For example the valuation of `smooth_array->data[i]` for the prime given by `factor_base->data[j]` will be stored in `decomp_matrix->data[i][j]`.

#### Note:

`list` contains the previously computed factors of each integers in `smooth_array`, in other words, we know that `smooth_array->data[i]` is divisible by all the integers of the `uint32_array_t` given by `list->data[i]`.

The binary matrix is filled so that:

- There is a '1' in the (i-th row, 1st col) position in the matrix if `smooth_factor->data[i]` is negative.



- There is a '1' in the (i-th row, j-th col) position in the matrix if `smooth_factor->data[i]` is divisible by an odd power of `list->data[i]->data[k]`. Here j is found so that `factor_base->data[j] = list->data[i]->data[k]`.
- In all other cases, the (i-th row, j-th col) position in the matrix contains a 0.

**Parameters:**

- *matrix* A pointer to the binary matrix to fill.
- *decomp\_matrix* A pointer to the byte matrix to fill.
- *smooth\_array* A pointer to the array giving the integers to factor.
- ← *list* A pointer to the factor list for each integer to factor.
- ← *factor\_base* A pointer to the array listing the integers to trial divide by.

**5.18.4.3 void fill\_matrix\_trial\_div (binary\_matrix\_t \*const matrix, mpz\_array\_t \*const partially\_factored, const mpz\_array\_t \*const to\_factor, const uint32\_array\_t \*const factor\_base)**

Fills a binary matrix via trial divisions.

Fills the binary matrix `matrix` by trial divisions of the integers listed in `to_factor` by the integers listed in `factor_base`. After these trial divisions, each partially factored integer from `to_factor` are stored in `partially_factored`.

**Note:**

The binary matrix is filled so that:

- There is a '1' in the (i-th row, 1st col) position in the matrix if `to_factor->data[i]` is negative.
- There is a '1' in the (i-th row, j-th col) position in the matrix if `to_factor->data[i]` is divisible by an odd power of `factor_base->data[j]`.
- In all other cases, the (i-th row, j-th col) position in the matrix contains a 0.

**Parameters:**

- *matrix* A pointer to the binary matrix to fill.
- *partially\_factored* A pointer to the partially factored integers.
- ← *to\_factor* A pointer to the array listing the integers to factor.
- ← *factor\_base* A pointer to the array listing the integers to trial divide by.

**5.18.4.4 void fill\_trial\_div\_decomp (binary\_matrix\_t \*const matrix, byte\_matrix\_t \*const decomp\_matrix, mpz\_array\_t \*const partially\_factored, const mpz\_array\_t \*const to\_factor, const uint32\_array\_t \*const factor\_base)**

Similar to `fill_matrix_trial_div` but also stores valuations.

Fills the binary matrix `matrix` by trial divisions of the integers listed in `to_factor` by the integers listed in `factor_base`. After these trial divisions, each partially factored integer from `to_factor` are stored in `partially_factored`.

Also stores in `decomp_matrix` the valuation of each integer from `to_factor` for each prime in the factor base. For example the valuation of `to_factor->data[i]` for the prime given by `factor_base->data[j]` will be stored in `decomp_matrix->data[i][j]`.

**Note:**

The binary matrix is filled so that:

- There is a '1' in the (i-th row, 1st col) position in the matrix if `to_factor->data[i]` is negative.
- There is a '1' in the (i-th row, j-th col) position in the matrix if `to_factor->data[i]` is divisible by an odd power of `factor_base->data[j]`.
- In all other cases, the (i-th row, j-th col) position in the matrix contains a 0.

**Parameters:**

- *matrix* A pointer to the binary matrix to fill.
- *decomp\_matrix* A pointer to the byte matrix to fill.
- *partially\_factored* A pointer to the partially factored integers.
- ← *to\_factor* A pointer to the array listing the integers to factor.
- ← *factor\_base* A pointer to the array listing the integers to trial divide by.

#### 5.18.4.5 `uint32_array_list_t* find_dependencies (binary_matrix_t *const matrix, linalg_method_t method)`

Solves a linear system over GF(2).

Solves the linear system over GF(2) given by the binary matrix `matrix`, using the resolution method `method`.

**Note:**

For the time being, the only implemented method is `SMART_GAUSS_ELIM`.

**Parameters:**

- ↔ *matrix* A pointer to the binary matrix giving the system to solve.
- ← *method* The linear system resolution method to use.

#### 5.18.4.6 `ecode_t find_factors (mpz_array_t *const factors, const mpz_t n, const mpz_array_t *const xi_array, const mpz_array_t *const yi_array, const uint32_array_list_t *const dependencies)`

Find factors of an integer from congruence relations.

Find factors of the integer `n` from congruence relations of the form  $\{(x_i)^2\}_i = \{y_i\}_i \pmod{n}$  where  $\{y_i\}_i$  is a perfect square.

Each entry in `dependencies` gives the list of the aforementioned indexes `i` so that such a previous relation will hold.

Upon termination, returns the following `ecode_t`:

- `SOME_FACTORS_FOUND` if some factors were found
- `NO_FACTOR_FOUND` if no factor was found
- `FATAL_INTERNAL_ERROR` is case of... a really ugly error!

**Parameters:**

- *factors* The factors of  $n$  found.
- ← *n* The integer to factor.
- ← *xi\_array* A pointer to an array giving the available  $x_i$  values.
- ← *yi\_array* A pointer to an array giving the available  $y_i$  values.
- ← *dependencies* A pointer to an array list giving the sets of indexes from which a congruence relation can be computed.

**Returns:**

An exit code.

#### 5.18.4.7 `ecode_t find_factors_decomp (mpz_array_t *const factors, const mpz_t n, const mpz_array_t *const xi_array, const byte_matrix_t *const yi_decomp_matrix, const uint32_array_list_t *const dependencies, const uint32_array_t *const factor_base)`

Similar to `find_factors` but uses the factorization of each  $y_i$ .

Find factors of the integer  $n$  from congruence relations of the form  $\{(x_i)^2\}_i = \{y_i\}_i \pmod{n}$  where  $\{y_i\}_i$  is a perfect square.

Each entry in `dependencies` gives the list of the aforementioned indexes  $i$  so that such a previous relation will hold.

The difference with the `find_factors` function is that here the  $y_i$  are not given directly but rather by their factorizations on the factor base by `yi_decomp_matrix`. For example the valuation of  $y_i$  for the prime given by `factor_base->data[j]` is stored in `yi_decomp_matrix->data[i][j]`.

Upon termination, returns the following `ecode_t`:

- `SOME_FACTORS_FOUND` if some factors were found
- `NO_FACTOR_FOUND` if no factor was found
- `FATAL_INTERNAL_ERROR` is case of... a really ugly error!

**Parameters:**

- *factors* The factors of  $n$  found.
- ← *n* The integer to factor.
- ← *xi\_array* A pointer to an array giving the available  $x_i$  values.
- ← *yi\_decomp\_matrix* A pointer to a byte matrix giving the factorization of the  $y_i$ .
- ← *dependencies* A pointer to an array list giving the sets of indexes from which a congruence relation can be computed.
- ← *factor\_base* A pointer to the array listing the primes in the factor base.

**Returns:**

An exit code.

### 5.18.5 Variable Documentation

#### 5.18.5.1 const char\* const linalg\_method\_to\_str[1] [static]

Initial value:

```
{  
    "smart gaussian elimination"  
}
```

Global constant array mapping linalg methods to their string representations.

Definition at line 78 of file lindep.h.

## 5.19 linked\_list.h File Reference

Standard singly-linked list.

```
#include <inttypes.h>
```

### Data Structures

- struct [struct\\_linked\\_list\\_node\\_t](#)  
*A basic implementation of a linked list node.*
- struct [struct\\_linked\\_list\\_t](#)  
*A basic implementation of a linked list.*

### Defines

- #define [\\_TIFA\\_LINKED\\_LIST\\_H\\_](#)

### Typedefs

- typedef struct [struct\\_linked\\_list\\_t](#) [linked\\_list\\_t](#)  
*Equivalent to struct [struct\\_linked\\_list\\_t](#).*
- typedef struct [struct\\_linked\\_list\\_node\\_t](#) [linked\\_list\\_node\\_t](#)  
*Equivalent to struct [struct\\_linked\\_list\\_node\\_t](#).*

### Functions

- void [init\\_linked\\_list](#) ([linked\\_list\\_t](#) \*const list, int(\*cmp\_func)(const void \*const data\_a, const void \*const data\_b))  
*Initializes a [linked\\_list\\_t](#).*
- void [clear\\_linked\\_list](#) ([linked\\_list\\_t](#) \*const list)  
*Clears a [linked\\_list\\_t](#).*

- void `append_to_linked_list` (`linked_list_t` \*const list, void \*const data)  
*Appends a node in a `linked_list_t`.*
- void `prepend_to_linked_list` (`linked_list_t` \*const list, void \*const data)  
*Prepends a node in a `linked_list_t`.*
- void \* `pop_linked_list` (`linked_list_t` \*const list)  
*Deletes the last node of a `linked_list_t`.*
- void \* `push_linked_list` (`linked_list_t` \*const list)  
*Deletes the first node of a `linked_list_t`.*
- void `insert_in_linked_list` (`linked_list_t` \*const list, void \*const data)  
*Inserts a node in a `linked_list_t`.*
- `linked_list_node_t` \* `get_node_in_linked_list` (`linked_list_t` \*const list, void \*const data)  
*Gets a node in a `linked_list_t`.*
- `linked_list_node_t` \* `remove_from_linked_list` (`linked_list_t` \*const list, void \*const data)  
*Gets a node in a `linked_list_t` and removes it from the list.*
- void `remove_node_from_linked_list` (`linked_list_t` \*const list, `linked_list_node_t` \*const node)  
*Removes a given node from a `linked_list_t`.*
- void `delete_in_linked_list` (`linked_list_t` \*const list, void \*const data)  
*Finds and deletes a node from a `linked_list_t`.*

### 5.19.1 Detailed Description

Standard singly-linked list.

**Author:**

Jerome Milan

**Date:**

Fri Jun 10 2011

**Version:**

2011-06-10

Defines generic singly-linked lists and their associated functions.

Definition in file [linked\\_list.h](#).

### 5.19.2 Define Documentation

#### 5.19.2.1 `#define _TIFA_LINKED_LIST_H_`

Standard include guard.

Definition at line 35 of file `linked_list.h`.

### 5.19.3 Function Documentation

#### 5.19.3.1 void append\_to\_linked\_list (linked\_list\_t \*const list, void \*const data)

Appends a node in a `linked_list_t`.

Appends a node (whose data is given by the pointer `data`) in the linked list `list`.

**Parameters:**

← *list* A pointer to the `linked_list_t`.

← *data* A pointer to the new node's data.

#### 5.19.3.2 void clear\_linked\_list (linked\_list\_t \*const list)

Clears a `linked_list_t`.

Clears a linked list `list` by freeing its nodes.

**Warning:**

Each node's `data` field is freed. However, if `data` is a pointer to a structure containing some other pointers, all the memory may not be freed.

**Parameters:**

← *list* A pointer to the `linked_list_t` to clear.

#### 5.19.3.3 void delete\_in\_linked\_list (linked\_list\_t \*const list, void \*const data)

Finds and deletes a node from a `linked_list_t`.

Deletes the node whose data is given by the pointer `data` from the linked list `list`. If the node is not found, the linked list is left unchanged.

**Warning:**

If a matching node is found, its `data` field is freed. However, if `data` is a pointer to a structure containing some other pointers, all the memory may not be freed.

**Parameters:**

← *list* A pointer to the `linked_list_t`.

← *data* A pointer to the data of the node to delete.

#### 5.19.3.4 linked\_list\_node\_t\* get\_node\_in\_linked\_list (linked\_list\_t \*const list, void \*const data)

Gets a node in a `linked_list_t`.

Returns a pointer to a node (whose data is given by the pointer `data`) from the linked list `list`.

**Parameters:**

← *list* A pointer to the `linked_list_t`.

← *data* A pointer to the sought node data.

**Returns:**

A pointer to the node with data pointed by `data`, if such a node exists.  
NULL if no matching node is found in the linked list.

**5.19.3.5 void init\_linked\_list (linked\_list\_t \*const list, int(\*)(const void \*const data\_a, const void \*const data\_b) cmp\_func)**

Initializes a `linked_list_t`.

Initializes a linked list `list`:

- Sets its `head` to NULL.
- Sets its `tail` to NULL.
- Sets its `cmp_func` to the `cmp_func` argument.
- Sets its `length` to 0.

**Parameters:**

- ← *list* A pointer to the `linked_list_t` to initialize.
- ← *cmp\_func* A pointer to the comparison function.

**5.19.3.6 void insert\_in\_linked\_list (linked\_list\_t \*const list, void \*const data)**

Inserts a node in a `linked_list_t`.

Inserts a node (whose data is given by the pointer `data`) in the linked list `list`, so that all the previous nodes have `data` fields pointing to datas less than the new node's data.

**Parameters:**

- ← *list* A pointer to the `linked_list_t`.
- ← *data* A pointer to the new node's data.

**5.19.3.7 void\* pop\_linked\_list (linked\_list\_t \*const list)**

Deletes the last node of a `linked_list_t`.

Returns the data of the last node of the linked list `list` and deletes this node, similar to Perl's `pop` function.

**Parameters:**

- ← *list* A pointer to the `linked_list_t`.

**5.19.3.8 void prepend\_to\_linked\_list (linked\_list\_t \*const list, void \*const data)**

Prepends a node in a `linked_list_t`.

Prepends a node (whose data is given by the pointer `data`) in the linked list `list`.

**Parameters:**

- ← *list* A pointer to the `linked_list_t`.
- ← *data* A pointer to the new node's data.

### 5.19.3.9 void\* push\_linked\_list (linked\_list\_t \*const list)

Deletes the first node of a `linked_list_t`.

Returns the data of the first node of the linked list `list` and deletes this node, similar to Perl's `push` function.

#### Parameters:

← *list* A pointer to the `linked_list_t`.

### 5.19.3.10 linked\_list\_node\_t\* remove\_from\_linked\_list (linked\_list\_t \*const list, void \*const data)

Gets a node in a `linked_list_t` and removes it from the list.

Returns a pointer to a node (whose data is given by the pointer `data`) from the linked list `list` and removes this node from the list.

#### Parameters:

← *list* A pointer to the `linked_list_t`.

← *data* A pointer to the seeked node data.

#### Returns:

A pointer to the node with data pointed by `data`, if such a node exists.  
NULL if no matching node is found in the linked list.

### 5.19.3.11 void remove\_node\_from\_linked\_list (linked\_list\_t \*const list, linked\_list\_node\_t \*const node)

Removes a given node from a `linked_list_t`.

Removes the node whose data is given by the pointer `data` from the linked list `list`. If the node is not found, the linked list is left unchanged.

#### Parameters:

← *list* A pointer to the `linked_list_t`.

← *node* A pointer to the node to remove from the list.

## 5.20 macros.h File Reference

Various CPP macros.

### Defines

- #define [\\_TIFA\\_MACROS\\_H](#)
- #define [MPN\\_NORMALIZE](#)(dest, nlimbs)
- #define [SIZ](#)(x) ((x) → `_mp_size`)
- #define [ABSIZ](#)(x) (ABS(SIZ(x)))
- #define [MPZ\\_TO\\_ABS](#)(x) (SIZ(x) = ABSIZ(x))



- #define [PTR](#)(x) ((x) → \_mp\_d)
- #define [ALLOC](#)(x) ((x) → \_mp\_alloc)
- #define [MPZ\\_LIMB\\_VALUE](#)(x, i) ( PTR(x)[(i)] & GMP\_NUMB\_MASK )
- #define [MPZ\\_LAST\\_LIMB\\_VALUE](#)(x) ( PTR(x)[SIZ(x) - 1] & GMP\_NUMB\_MASK )
- #define [MAX](#)(a, b) ( ((a) > (b)) ? (a) : (b) )
- #define [MIN](#)(a, b) ( ((a) < (b)) ? (a) : (b) )
- #define [ABS](#)(a) ( ((a) < 0) ? -(a) : (a) )
- #define [IS\\_POWER\\_OF\\_2\\_UI](#)(ui) ( ((ui) & ((ui) - 1)) == 0 )
- #define [IS\\_EVEN](#)(ui) (((ui) & 1) == 0)
- #define [IS\\_ODD](#)(ui) (((ui) & 1) != 0)
- #define [ARE\\_EVEN](#)(uia, uib) (((uia) | (uib)) & 1) == 0)
- #define [ARE\\_ODD](#)(uia, uib) (((uia) | (uib)) & 1) != 0)
- #define [BIT](#)(N, i) ( ((N) & (1 << (i))) ? 1 : 0 )
- #define [DUFF\\_DEVICE](#)(COUNT, STATEMENT,...)
- #define [MPZ\\_IS\\_SQUARE](#)(X) (0 != mpz\_perfect\_square\_p(X))
- #define [NMILLER\\_RABIN](#) 32
- #define [MPZ\\_IS\\_PRIME](#)(X) (0 != mpz\_probab\_prime\_p((X), NMILLER\_RABIN))
- #define [MPN\\_ADD](#)(A, B, C)
- #define [MPN\\_ADD\\_CS](#)(A, B, C)
- #define [MPN\\_SUB](#)(A, B, C)
- #define [MPN\\_SUB\\_N](#)(A, B, C)
- #define [MPN\\_TDIV\\_QR](#)(Q, R, N, D)
- #define [MPN\\_MUL](#)(A, B, C)
- #define [MPN\\_MUL\\_N](#)(A, B, C)
- #define [MPN\\_MUL\\_CS](#)(A, B, C)
- #define [MPN\\_MUL\\_CS\\_S](#)(A, B, C)
- #define [DECLARE\\_MPZ\\_SWAP\\_VARS](#)
- #define [MPZ\\_SWAP](#)(A, B)
- #define [TIFA\\_DEBUG\\_MSG](#)(...)

### 5.20.1 Detailed Description

Various CPP macros.

**Author:**

Jerome Milan

**Date:**

Fri Jun 10 2011

**Version:**

2011-06-10

Defines some C preprocessor macros that should be kept internal to the TIFA library to avoid polluting client code.

Definition in file [macros.h](#).

## 5.20.2 Define Documentation

### 5.20.2.1 #define \_TIFA\_MACROS\_H\_

Standard include guard.

Definition at line 36 of file macros.h.

### 5.20.2.2 #define ABS(a) ((a) < 0) ? -(a) : (a)

Standard macro returning the absolute value of a.

#### Note:

As usual, be careful of possible side effects when using this kind of macro. The standard disclaimers apply.

Definition at line 204 of file macros.h.

### 5.20.2.3 #define ABSIZ(x) (ABS(SIZ(x)))

Macro from the GMP library: Returns the absolute value of `SIZ(x)`.

Returns the absolute value of `SIZ(x)` that is to say the number of `mp_limbs_t` integers needed to represent the value of `x`.

#### Note:

This macro is the `ABSIZ` macro from the GMP library. It is redistributed under the GNU LGPL license.

Definition at line 115 of file macros.h.

### 5.20.2.4 #define ALLOC(x) ((x) → \_mp\_alloc)

Macro from the GMP library: Returns the `_mp_alloc` field of an `mpz_t` integer.

Returns the `_mp_alloc` field of an `mpz_t` integer, that is to say the size (in units of `mp_limb_t`) of the `x->_mp_d` array.

#### Note:

This macro is the `ALLOC` macro from the GMP library. It is redistributed under the GNU LGPL license.

Definition at line 154 of file macros.h.

### 5.20.2.5 #define ARE\_EVEN(ua, ub) (((ua) | (ub)) & 1) == 0

Macro returning True if both of the unsigned integers `ua` and `ub` are even, False otherwise.

Definition at line 237 of file macros.h.

### 5.20.2.6 #define ARE\_ODD(ua, ub) (((ua) | (ub)) & 1) != 0

Macro returning True if both of the unsigned integers `ua` and `ub` are odd, False otherwise.

Definition at line 244 of file macros.h.

**5.20.2.7 #define BIT(N, i) ((N) & (1<<(i))) ? 1 : 0**

Macro returning the value of the i-th least significant bit of N. `BIT(N, 0)` returns the least significant bit of N.

Definition at line 251 of file macros.h.

**5.20.2.8 #define DECLARE\_MPZ\_SWAP\_VARS**

**Value:**

```
mp_ptr __TMPPTR__MACROS_H__a9b3c01__; \
mp_size_t __TMPSIZ__MACROS_H__a9b3c01__;
```

Macro declaring local variables needed by the `MPZ_SWAP` macro. Should be called *once* prior to any use of the `MPZ_SWAP` macro.

**Warning:**

Declares the variables `__TMPPTR__MACROS_H__a9b3c01__` and `__TMPSIZ__MACROS_H__a9b3c01__`. Hopefully their names are fancy enough to avoid any local conflict.

Definition at line 562 of file macros.h.

**5.20.2.9 #define DUFF\_DEVICE(COUNT, STATEMENT, ...)**

**Value:**

```
do { \
    long int __count__ = (COUNT); \
    long int __niter__ = (__count__ + 7) >> 3; \
    switch (__count__ & 7) { \
        case 0: do { STATEMENT; __VA_ARGS__; \
        case 7: STATEMENT; __VA_ARGS__; \
        case 6: STATEMENT; __VA_ARGS__; \
        case 5: STATEMENT; __VA_ARGS__; \
        case 4: STATEMENT; __VA_ARGS__; \
        case 3: STATEMENT; __VA_ARGS__; \
        case 2: STATEMENT; __VA_ARGS__; \
        case 1: STATEMENT; __VA_ARGS__; \
                __niter__--; \
        } while (__niter__ > 0); \
    } \
} while (0)
```

Implements the so-called "Duff device" which is a fairly well-known (and so ugly looking!) loop unrolling technique. `COUNT` is the number of times to perform the operations given by `STATEMENTS`.

**Warning:**

`COUNT` should be strictly positive. Using `COUNT` equals to zero will yield wrong results.

**Note:**

This macro was actually inspired (borrowed? stolen?) from the example given in the article "A Reusable Duff Device" written by Ralf Holly.

**See also:**

Tom Duff's comments about this technique at <http://www.lysator.liu.se/c/duffs-device.html> (URL last accessed on Thu 17 Feb 2011)

"A Reusable Duff Device", Ralf Holly, *Dr. Dobbs's Journal*, August 2005. Available online at: <http://www.drdoobbs.com/high-performance-computing/184406208> (URL last accessed on Thu 17 Feb 2011)

Definition at line 277 of file macros.h.

**5.20.2.10 #define IS\_EVEN(ui) (((ui) & 1) == 0)**

Macro returning True if the unsigned integer `ui` is even, False otherwise.

Definition at line 223 of file macros.h.

**5.20.2.11 #define IS\_ODD(ui) (((ui) & 1) != 0)**

Macro returning True if the unsigned integer `ui` is odd, False otherwise.

Definition at line 230 of file macros.h.

**5.20.2.12 #define IS\_POWER\_OF\_2\_UI(ui) ((ui) & ((ui) - 1) == 0)**

Macro returning a non-zero value if the unsigned integer `ui` is a power of 2.

**Note:**

As usual, be careful of possible side effects when using this kind of macro. The standard disclaimers apply.

Definition at line 216 of file macros.h.

Referenced by `ceil_log2()`.

**5.20.2.13 #define MAX(a, b) ((a) > (b) ? (a) : (b))**

Standard macro returning the maximum of `a` and `b`.

**Note:**

As usual, be careful of possible side effects when using this kind of macro. The standard disclaimers apply.

Definition at line 180 of file macros.h.

**5.20.2.14 #define MIN(a, b) ((a) < (b) ? (a) : (b))**

Standard macro returning the minimum of `a` and `b`.

**Note:**

As usual, be careful of possible side effects when using this kind of macro. The standard disclaimers apply.

Definition at line 192 of file macros.h.

**5.20.2.15 #define MPN\_ADD(A, B, C)****Value:**

```
do {
    if (mpn_add(PTR(A), PTR(B), SIZ(B), PTR(C), SIZ(C))) { \
        SIZ(A) = SIZ(B); \
        MPN_NORMALIZE(PTR(A), SIZ(A)); \
        PTR(A)[SIZ(A)] = 1; \
        SIZ(A)++; \
    } else { \
        SIZ(A) = SIZ(B); \
        MPN_NORMALIZE(PTR(A), SIZ(A)); \
    } \
} while (0)
```

Syntactic sugar macro wrapping a call to `mpn_add`. Performs size normalization on the result and takes care of the possible carry out. Does not perform any reallocation: the user should make sure the result has enough space to accommodate the possible carry out.

Takes as parameters three `mpz_t` (and not arrays of `mp_limb_t`). `SIZ(B)` should be greater than or equal to `SIZ(C)`.

**Warning:**

B and C should be both positive or the result will be unpredictable.

**See also:**

The GMP documentation for more information on the `mpn_add` function.

Definition at line 339 of file `macros.h`.

**5.20.2.16 #define MPN\_ADD\_CS(A, B, C)****Value:**

```
do {
    if (SIZ(B) > SIZ(C)) { \
        MPN_ADD(A, B, C); \
    } else { \
        MPN_ADD(A, C, B); \
    } \
} while (0)
```

Syntactic sugar macro wrapping a call to `mpn_add`. Performs size normalization on the result, takes care of the possible carry out, and Checks the Sizes of the operands to call `mpn_add` with the proper parameters' order. However, does not perform any reallocation: the user should make sure the result has enough space to accommodate the possible carry out.

Takes as parameters three `mpz_t` (and not arrays of `mp_limb_t`). B and C can be used interchangeably.

**Warning:**

B and C should be both positive or the result will be unpredictable.

**See also:**

The GMP documentation for more information on the `mpn_add` function.

Definition at line 371 of file `macros.h`.

**5.20.2.17 #define MPN\_MUL(A, B, C)****Value:**

```
do {
    mpn_mul (PTR(A), PTR(B), SIZ(B), PTR(C), SIZ(C));
    SIZ(A) = SIZ(B) + SIZ(C);
    MPN_NORMALIZE (PTR(A), SIZ(A));
} while (0)
```

Syntactic sugar macro wrapping a call to `mpn_mul`. Performs size normalization on the result.

Takes as parameters three `mpz_t` (and not arrays of `mp_limb_t`). `SIZ(B)` should be greater than or equal to `SIZ(C)`.

**Warning:**

B and C should be both positive or the result will be unpredictable.

**See also:**

The GMP documentation for more information on the `mpn_mul` function.

Definition at line 466 of file `macros.h`.

**5.20.2.18 #define MPN\_MUL\_CS(A, B, C)****Value:**

```
do {
    if (SIZ(B) > SIZ(C)) {
        mpn_mul (PTR(A), PTR(B), SIZ(B), PTR(C), SIZ(C));
    } else {
        mpn_mul (PTR(A), PTR(C), SIZ(C), PTR(B), SIZ(B));
    }
    SIZ(A) = SIZ(B) + SIZ(C);
    MPN_NORMALIZE (PTR(A), SIZ(A));
} while (0)
```

Syntactic sugar macro wrapping a call to `mpn_mul`. Performs size normalization on the result, and Checks the Sizes of the operands to call `mpn_mul` with the proper parameters' order.

Takes as parameters three `mpz_t` (and not arrays of `mp_limb_t`). B and C can be used interchangeably.

**Warning:**

B and C should be both positive or the result will be unpredictable.

**See also:**

The GMP documentation for more information on the `mpn_mul` function.

Definition at line 511 of file `macros.h`.

**5.20.2.19 #define MPN\_MUL\_CS\_S(A, B, C)****Value:**

```

do {
    if (ABSIZ(B) > ABSIZ(C)) {
        mpn_mul(PTR(A), PTR(B), ABSIZ(B), PTR(C), ABSIZ(C));
    } else {
        mpn_mul(PTR(A), PTR(C), ABSIZ(C), PTR(B), ABSIZ(B));
    }
    SIZ(A) = ABSIZ(B) + ABSIZ(C);
    MPN_NORMALIZE(PTR(A), SIZ(A));
    if ((SIZ(B) ^ SIZ(C)) < 0) {
        SIZ(A) = -SIZ(A);
    }
} while (0)

```

Syntactic sugar macro wrapping a call to `mpn_mul`. Performs size normalization on the result, and Checks the Sizes and the Signs of the operands to call `mpn_mul` with the proper parameters' order.

Takes as parameters three `mpz_t` (and not arrays of `mp_limb_t`). B and C can be used interchangeably.

**Note:**

B and C are allowed to be negative.

**See also:**

The GMP documentation for more information on the `mpn_mul` function.

Definition at line 537 of file macros.h.

### 5.20.2.20 #define MPN\_MUL\_N(A, B, C)

**Value:**

```

do {
    mpn_mul_n(PTR(A), PTR(B), PTR(C), SIZ(B));
    SIZ(A) = SIZ(B) << 1;
    MPN_NORMALIZE(PTR(A), SIZ(A));
} while (0)

```

Syntactic sugar macro wrapping a call to `mpn_mul_n`. Performs size normalization on the result.

Takes as parameters three `mpz_t` (and not arrays of `mp_limb_t`). `SIZ(B)` and `SIZ(C)` should be the same.

**Warning:**

B and C should be both positive or the result will be unpredictable.

**See also:**

The GMP documentation for more information on the `mpn_mul_n` function.

Definition at line 488 of file macros.h.

### 5.20.2.21 #define MPN\_NORMALIZE(dest, nlimbs)

**Value:**

```
do {
    while (((nlimbs) > 0) && ((dest)[(nlimbs) - 1] == 0)) {
        (nlimbs)--;
    }
} while (0)
```

Macro from the GMP library: Computes the effective size of an MPN number.

Given *dest*, a pointer to an array of *nlimbs* *mp\_limb\_t* integers giving the representation of a multi-precision integer *n*, computes the absolute value of the effective size of *n*, i.e the number of significant *mp\_size\_t* integers needed to represent *n* and modifies the value of *nlimbs* accordingly.

**Note:**

This macro is originally the `MPN_NORMALIZE` macro from the GMP library. It has been slightly modified.

Definition at line 79 of file `macros.h`.

### 5.20.2.22 #define MPN\_SUB(A, B, C)

**Value:**

```
do {
    mpn_sub(PTR(A), PTR(B), SIZ(B), PTR(C), SIZ(C));
    SIZ(A) = SIZ(B);
    MPN_NORMALIZE(PTR(A), SIZ(A));
} while (0)
```

Syntactic sugar macro wrapping a call to `mpn_sub`. Performs size normalization on the result but does not take care of the possible borrow out.

Takes as parameters three *mpz\_t* (and not arrays of *mp\_limb\_t*). *B* should be greater than or equal to *C*.

**Warning:**

*B* and *C* should be both positive or the result will be unpredictable.

**See also:**

The GMP documentation for more information on the `mpn_sub` function.

Definition at line 396 of file `macros.h`.

### 5.20.2.23 #define MPN\_SUB\_N(A, B, C)

**Value:**

```
do {
    mpn_sub_n(PTR(A), PTR(B), PTR(C), SIZ(B));
    SIZ(A) = SIZ(B);
    MPN_NORMALIZE(PTR(A), SIZ(A));
} while (0)
```

Syntactic sugar macro wrapping a call to `mpn_sub_n`. Performs size normalization on the result but does not take care of the possible borrow out.

Takes as parameters three *mpz\_t* (and not arrays of *mp\_limb\_t*). *B* should be greater than or equal to *C*.



**Warning:**

B and C should be both positive or the result will be unpredictable.

**See also:**

The GMP documentation for more information on the `mpn_sub_n` function.

Definition at line 419 of file macros.h.

**5.20.2.24 #define MPN\_TDIV\_QR(Q, R, N, D)****Value:**

```
do {
    if (SIZ(N) >= SIZ(D)) {
        mpn_tdiv_qr(PTR(Q), PTR(R), 0, PTR(N), SIZ(N), PTR(D), SIZ(D)); \
        SIZ(Q) = SIZ(N) - SIZ(D) + 1; \
        MPN_NORMALIZE(PTR(Q), SIZ(Q)); \
        SIZ(R) = SIZ(D); \
        MPN_NORMALIZE(PTR(R), SIZ(R)); \
    }
} while (0)
```

Syntactic sugar macro wrapping a call to `mpn_tdiv_qr`. Performs size normalization on both the quotient and remainder.

Takes as parameters four `mpz_t` (and not arrays of `mp_limb_t`).

**Warning:**

N and D should be both positive or the result will be unpredictable.

**See also:**

The GMP documentation for more information on the `mpn_tdiv_qr` function.

Definition at line 440 of file macros.h.

**5.20.2.25 #define MPZ\_IS\_PRIME(X) (0 != mpz\_probab\_prime\_p(X, NMILLER\_RABIN))**

Syntactic sugar macro wrapping a call to `mpz_probab_prime_p`. "Returns" true if and only if the `mpz_t` X is (probably) prime.

Takes as parameter an `mpz_t`.

Definition at line 320 of file macros.h.

**5.20.2.26 #define MPZ\_IS\_SQUARE(X) (0 != mpz\_perfect\_square\_p(X))**

Syntactic sugar macro wrapping a call to `mpz_perfect_square_p`. "Returns" true if and only if the `mpz_t` X is a perfect square.

Takes as parameter an `mpz_t`.

Definition at line 303 of file macros.h.

**5.20.2.27 #define MPZ\_LAST\_LIMB\_VALUE(x) ( PTR(x)[SIZ(x) - 1] & GMP\_NUMB\_MASK )**

Returns the value of the most significant limb of the `mpz_t` integer `x`. Is equivalent to `MPZ_LIMB_VALUE(x, SIZ(x) - 1)`.

Definition at line 169 of file `macros.h`.

**5.20.2.28 #define MPZ\_LIMB\_VALUE(x, i) ( PTR(x)[i] & GMP\_NUMB\_MASK )**

Returns the value of the `i`-th limb of the `mpz_t` integer `x`. The least significant limb is given by `i = 0`.

Definition at line 162 of file `macros.h`.

**5.20.2.29 #define MPZ\_SWAP(A, B)****Value:**

```
do {
    __TMPPTR__MACROS_H__a9b3c01__ = PTR(A);          \
    __TMPsiz__MACROS_H__a9b3c01__ = SIZ(A);          \
    PTR(A) = PTR(B);                                  \
    SIZ(A) = SIZ(B);                                  \
    PTR(B) = __TMPPTR__MACROS_H__a9b3c01__;         \
    SIZ(B) = __TMPsiz__MACROS_H__a9b3c01__;         \
} while (0)
```

Macro swapping the values of the two `mpz_t` `A` and `B`.

**Warning:**

The macro `DECLARE_MPZ_SWAP_VARS` should be called *once* before using `MPZ_SWAP`.

Definition at line 575 of file `macros.h`.

**5.20.2.30 #define MPZ\_TO\_ABS(x) (SIZ(x) = ABSIZ(x))**

Sets the `mpz_t` `x` to its absolute value.

Definition at line 123 of file `macros.h`.

**5.20.2.31 #define NMILLER\_RABIN 32**

Number of Miller-Rabin iterations to perform for each compositeness test.

Definition at line 310 of file `macros.h`.

**5.20.2.32 #define PTR(x) ((x) → \_mp\_d)**

Macro from the GMP library: Returns the `_mp_d` field of an `mpz_t` integer.

Returns the `_mp_d` field of an `mpz_t` integer, that is to say a pointer to an array of `mp_limbs_t` integers giving the representation of the value of `x`.

**Note:**

This macro is the `PTR` macro from the GMP library. It is redistributed under the GNU LGPL license.

Definition at line 139 of file `macros.h`.

### 5.20.2.33 #define SIZ(x) ((x) → \_mp\_size)

Macro from the GMP library: Returns the `_mp_size` field of an `mpz_t` integer.

Returns the `_mp_size` field of the variable `x` of type `mpz_t`, that is to say the number of `mp_limb_t` integers needed to represent the value of `x`. The sign of the returned value is given by the sign of `x`'s value.

#### Note:

This macro is the `SIZ` macro from the GMP library. It is redistributed under the GNU LGPL license.

Definition at line 100 of file `macros.h`.

### 5.20.2.34 #define TIFA\_DEBUG\_MSG(...)

Macro printing debug message with filename and line number.

#### Warning:

The symbol `ENABLE_TIFA_DEBUG_MSG` should be defined to non zero *before* including this file.

Definition at line 601 of file `macros.h`.

## 5.21 mainpage.h File Reference

### Defines

- #define [\\_TIFA\\_MAINPAGE\\_H\\_](#)

#### 5.21.1 Detailed Description

##### Author:

Jerome Milan

Definition in file [mainpage.h](#).

#### 5.21.2 Define Documentation

##### 5.21.2.1 #define \_TIFA\_MAINPAGE\_H\_

Standard include guard.

Definition at line 6 of file `mainpage.h`.

## 5.22 matrix.h File Reference

Byte and binary matrices and associated functions.

```
#include "tifa_config.h"
```

```
#include <inttypes.h>
```

```
#include "bitstring_t.h"
```

## Data Structures

- struct [struct\\_binary\\_matrix\\_t](#)  
*Defines a matrix of bits.*
- struct [struct\\_byte\\_matrix\\_t](#)  
*Defines a matrix of bytes.*

## Defines

- #define [\\_TIFA\\_MATRIX\\_H\\_](#)
- #define [NO\\_SUCH\\_ROW](#) [UINT32\\_MAX](#)

## Typedefs

- typedef struct [struct\\_binary\\_matrix\\_t](#) [binary\\_matrix\\_t](#)  
*Equivalent to struct [struct\\_binary\\_matrix\\_t](#).*
- typedef struct [struct\\_byte\\_matrix\\_t](#) [byte\\_matrix\\_t](#)  
*Equivalent to struct [struct\\_byte\\_matrix\\_t](#).*

## Functions

- [binary\\_matrix\\_t](#) \* [alloc\\_binary\\_matrix](#) ([uint32\\_t](#) nrows, [uint32\\_t](#) ncols)  
*Allocates and returns a new [binary\\_matrix\\_t](#).*
- [binary\\_matrix\\_t](#) \* [clone\\_binary\\_matrix](#) (const [binary\\_matrix\\_t](#) \*const matrix)  
*Allocates and returns a cloned [binary\\_matrix\\_t](#).*
- void [reset\\_binary\\_matrix](#) ([binary\\_matrix\\_t](#) \*const matrix)  
*Sets a [binary\\_matrix\\_t](#) to zero.*
- void [free\\_binary\\_matrix](#) ([binary\\_matrix\\_t](#) \*const matrix)  
*Clears a [binary\\_matrix\\_t](#).*
- void [print\\_binary\\_matrix](#) (const [binary\\_matrix\\_t](#) \*const matrix)  
*Prints a [binary\\_matrix\\_t](#).*
- static [uint8\\_t](#) [get\\_matrix\\_bit](#) ([uint32\\_t](#) row, [uint32\\_t](#) col, const [binary\\_matrix\\_t](#) \*const matrix)  
*Returns the value of a given bit in a [binary\\_matrix\\_t](#).*
- static void [set\\_matrix\\_bit\\_to\\_one](#) ([uint32\\_t](#) row, [uint32\\_t](#) col, [binary\\_matrix\\_t](#) \*const matrix)  
*Sets to one the value of a given bit in a [binary\\_matrix\\_t](#).*
- static void [set\\_matrix\\_bit\\_to\\_zero](#) ([uint32\\_t](#) row, [uint32\\_t](#) col, [binary\\_matrix\\_t](#) \*const matrix)  
*Sets to zero the value of a given bit in a [binary\\_matrix\\_t](#).*

- static void `flip_matrix_bit` (uint32\_t row, uint32\_t col, `binary_matrix_t` \*const matrix)  
*Flips the value of a given bit in a `binary_matrix_t`.*
- static uint32\_t `first_row_with_one_on_col` (uint32\_t col, const `binary_matrix_t` \*const matrix)  
*Returns the index of the first row of a `binary_matrix_t` with a one in a given column.*
- `byte_matrix_t` \* `alloc_byte_matrix` (uint32\_t nrows, uint32\_t ncols)  
*Allocates and returns a new `byte_matrix_t`.*
- `byte_matrix_t` \* `clone_byte_matrix` (const `byte_matrix_t` \*const matrix)  
*Allocates and returns a cloned `byte_matrix_t`.*
- void `reset_byte_matrix` (`byte_matrix_t` \*const matrix)  
*Sets a `byte_matrix_t` to zero.*
- void `free_byte_matrix` (`byte_matrix_t` \*const matrix)  
*Clears a `byte_matrix_t`.*
- void `print_byte_matrix` (const `byte_matrix_t` \*const matrix)  
*Prints a `byte_matrix_t`.*

### 5.22.1 Detailed Description

Byte and binary matrices and associated functions.

**Author:**

Jerome Milan

**Date:**

Fri Jun 10 2011

**Version:**

2011-06-10

Defines binary matrices (i.e. matrices over GF(2)), byte matrices, and their associated functions.

Definition in file [matrix.h](#).

### 5.22.2 Define Documentation

#### 5.22.2.1 `#define _TIFA_MATRIX_H_`

Standard include guard.

Definition at line 36 of file `matrix.h`.

### 5.22.2.2 #define NO\_SUCH\_ROW UINT32\_MAX

Value returned by the `first_row_with_one_on_col(col, matrix)` function if no row of the matrix has a bit 1 in its `col`-th column.

Definition at line 53 of file `matrix.h`.

Referenced by `first_row_with_one_on_col()`.

## 5.22.3 Function Documentation

### 5.22.3.1 binary\_matrix\_t\* alloc\_binary\_matrix (uint32\_t nrows, uint32\_t ncols)

Allocates and returns a new `binary_matrix_t`.

Allocates and returns a new `binary_matrix_t` such that:

- its `nrows_allocated` field is set to `nrows`.
- its `ncols_allocated` field is set to the minimum number of `TIFA_BITSTRING_T` integers needed to store `ncols` bits.
- its `nrows` field is set to `nrows`.
- its `ncols` field is set to `ncols`.
- its `data` array of arrays is completely filled with zeroes.

#### Note:

The behaviour of this `alloc` function differs from the ones in [array.h](#). This discrepancy will be corrected in later versions.

#### Parameters:

← *nrows* The maximum number of rows of the `binary_matrix_t` to allocate.

← *ncols* The maximum number of bits per row of the `binary_matrix_t` to allocate.

#### Returns:

A pointer to the newly allocated `binary_matrix_t` structure. Note that this matrix may hold more than `ncols` bits per column if `ncols` is not a multiple of `8 * sizeof(TIFA_BITSTRING_T)`.

### 5.22.3.2 byte\_matrix\_t\* alloc\_byte\_matrix (uint32\_t nrows, uint32\_t ncols)

Allocates and returns a new `byte_matrix_t`.

Allocates and returns a new `byte_matrix_t` such that:

- its `nrows_allocated` field is set to `nrows`.
- its `ncols_allocated` field is set to `ncols`.
- its `nrows` field is set to `nrows`.
- its `ncols` field is set to `ncols`.
- its `data` array of arrays is completely filled with zeroes.

**Note:**

The behaviour of this alloc function differs from the ones in [array.h](#). This discrepancy will be corrected in later versions.

**Parameters:**

- ← *rows* The maximum number of rows of the `byte_matrix_t` to allocate.
- ← *cols* The maximum number of columns `byte_matrix_t` to allocate.

**Returns:**

A pointer to the newly allocated `byte_matrix_t` structure.

**5.22.3.3 `binary_matrix_t* clone_binary_matrix (const binary_matrix_t *const matrix)`**

Allocates and returns a cloned `binary_matrix_t`.

Allocates and returns a clone of the `binary_matrix_t` pointed by `matrix`.

**Parameters:**

- ← *matrix* A pointer to the binary matrix to clone.

**Returns:**

A pointer to the newly allocated `binary_matrix_t` clone.

**5.22.3.4 `byte_matrix_t* clone_byte_matrix (const byte_matrix_t *const matrix)`**

Allocates and returns a cloned `byte_matrix_t`.

Allocates and returns a clone of the `byte_matrix_t` pointed by `matrix`.

**Parameters:**

- ← *matrix* A pointer to the byte matrix to clone.

**Returns:**

A pointer to the newly allocated `byte_matrix_t` clone.

**5.22.3.5 `static uint32_t first_row_with_one_on_col (uint32_t col, const binary_matrix_t *const matrix)` [inline, static]**

Returns the index of the first row of a `binary_matrix_t` with a one in a given column.

Returns the index of the first row of a `binary_matrix_t` which has a one on its `col`-th column. It returns `NO_SUCH_ROW` if no such row is found.

**Parameters:**

- ← *col* The column of the matrix.
- ← *matrix* A pointer to the `binary_matrix_t`.

**Returns:**

- An unsigned integer `row` between 0 and `matrix->nrows-1` such that `(matrix->data[row][col] == 1)`
- `NO_SUCH_ROW` if, for all valid `i`, `(matrix->data[i][col] != 1)`.

**Note:**

This function is needed in the gaussian elimination algorithm described in the paper "A compact algorithm for Gaussian elimination over GF(2) implemented on highly parallel computers", by D. Parkinson and M. Wunderlich (Parallel Computing 1 (1984) 65-73).

It could be argued that such a function should then be declared and implemented in the files relevant to the aforementioned algorithm. However, this would lead to a very inefficient implementation of this function since proper programming practices would lead to consider the matrix as some kind of opaque structure. Granted, nothing could have prevented us to implement `first_row_with_one_on_col` exactly as in `matrix.c`, but the future maintainer would have the burden to check and update code scattered around several files should the inner structure of `binary_matrix_t` be modified.

This can be seen as a moot point: after all, the TIFA code does not strictly enforce type encapsulation. Indeed, some parts of the code do assume (a minimal!) knowledge of the internal structures of some types (have a look at `siqs.c` for instance). That does not make it the right thing to do though. Unless when facing a real bottleneck, let's try to keep the "programmer's omniscience" to a manageable level...

Definition at line 316 of file `matrix.h`.

References `struct_binary_matrix_t::data`, `NO_SUCH_ROW`, and `struct_binary_matrix_t::nrows`.

### 5.22.3.6 `static void flip_matrix_bit (uint32_t row, uint32_t col, binary_matrix_t *const matrix)` `[inline, static]`

Flips the value of a given bit in a `binary_matrix_t`.

Flips the value of the bit at the `row`-th row and the `col`-th column of the `binary_array_t` pointed by `array`.

**Parameters:**

- ← ***row*** The row of the bit to flip.
- ← ***col*** The column of the bit to flip.
- ← ***matrix*** A pointer to the `binary_matrix_t`.

Definition at line 265 of file `matrix.h`.

References `struct_binary_matrix_t::data`.

### 5.22.3.7 `void free_binary_matrix (binary_matrix_t *const matrix)`

Clears a `binary_matrix_t`.

Clears a `binary_matrix_t`, or, more precisely, clears the memory space used by the arrays pointed by the `data` field of a `binary_matrix_t`. Also set its `nrows_allocated`, `ncols_allocated`, `nrows` and `ncols` fields to zero.

**Parameters:**

- ← ***matrix*** A pointer to the `binary_matrix_t` to clear.



**5.22.3.8 void free\_byte\_matrix (byte\_matrix\_t \*const matrix)**

Clears a `byte_matrix_t`.

Clears a `byte_matrix_t`, or, more precisely, clears the memory space used by the arrays pointed by the data field of a `byte_matrix_t`. Also set its `nrows_allocated`, `ncols_allocated`, `nrows` and `ncols` fields to zero.

**Parameters:**

← *matrix* A pointer to the `byte_matrix_t` to clear.

**5.22.3.9 static uint8\_t get\_matrix\_bit (uint32\_t row, uint32\_t col, const binary\_matrix\_t \*const matrix) [inline, static]**

Returns the value of a given bit in a `binary_matrix_t`.

Returns the value of the bit at the `row`-th row and the `col`-th column of the `binary_array_t` pointed by `array`, as either 0 or 1.

**Parameters:**

← *row* The row of the bit to read.

← *col* The column of the bit to read.

← *matrix* A pointer to the `binary_matrix_t`.

**Returns:**

The value of the bit at the (`row,col`) position: either 0 or 1.

Definition at line 186 of file `matrix.h`.

References `struct_binary_matrix_t::data`.

**5.22.3.10 void print\_binary\_matrix (const binary\_matrix\_t \*const matrix)**

Prints a `binary_matrix_t`.

Prints a `binary_matrix_t`'s on the standard output.

**Parameters:**

← *matrix* A pointer to the `binary_matrix_t` to print.

**5.22.3.11 void print\_byte\_matrix (const byte\_matrix\_t \*const matrix)**

Prints a `byte_matrix_t`.

Prints a `byte_matrix_t`'s on the standard output.

**Parameters:**

← *matrix* A pointer to the `byte_matrix_t` to print.

**5.22.3.12 void reset\_binary\_matrix (binary\_matrix\_t \*const matrix)**

Sets a `binary_matrix_t` to zero.

Sets the `binary_matrix_t` `matrix` to the zero matrix.

**Parameters:**

← *matrix* A pointer to the `binary_matrix_t` to reset.

**5.22.3.13 void reset\_byte\_matrix (byte\_matrix\_t \*const matrix)**

Sets a `byte_matrix_t` to zero.

Sets the `byte_matrix_t` `matrix` to the zero matrix.

**Parameters:**

← *matrix* A pointer to the `byte_matrix_t` to reset.

**5.22.3.14 static void set\_matrix\_bit\_to\_one (uint32\_t row, uint32\_t col, binary\_matrix\_t \*const matrix) [inline, static]**

Sets to one the value of a given bit in a `binary_matrix_t`.

Sets to one the value of the bit at the `row`-th row and the `col`-th column of the `binary_array_t` pointed by `array`.

**Parameters:**

← *row* The row of the bit to set.

← *col* The column of the bit to set.

← *matrix* A pointer to the `binary_matrix_t`.

Definition at line 214 of file `matrix.h`.

References `struct_binary_matrix_t::data`.

**5.22.3.15 static void set\_matrix\_bit\_to\_zero (uint32\_t row, uint32\_t col, binary\_matrix\_t \*const matrix) [inline, static]**

Sets to zero the value of a given bit in a `binary_matrix_t`.

Sets to zero the value of the bit at the `row`-th row and the `col`-th column of the `binary_array_t` pointed by `array`.

**Parameters:**

← *row* The row of the bit to set.

← *col* The column of the bit to set.

← *matrix* A pointer to the `binary_matrix_t`.

Definition at line 240 of file `matrix.h`.

References `struct_binary_matrix_t::data`.

## 5.23 messages.h File Reference

Status / error messages output macros.

```
#include "timer.h"
#include "tifa_config.h"
#include <stdio.h>
#include "exit_codes.h"
```

### Defines

- #define [\\_TIFA\\_MESSAGES\\_H\\_](#)

### 5.23.1 Detailed Description

Status / error messages output macros.

#### Author:

Jerome Milan

#### Date:

Fri Jun 10 2011

#### Version:

2011-06-10

This file defines some macros used to output status or error messages if some of the \*\_VERBOSE and/or \*\_TIMING symbols are set to non-zero.

#### Warning:

The \_\_VERBOSE\_\_, \_\_TIMING\_\_ and \_\_PREFIX\_\_ symbols should be defined in the file including this header. It is under the responsibility of the including file to check for these symbol definitions or to define them, if needed.

Definition in file [messages.h](#).

### 5.23.2 Define Documentation

#### 5.23.2.1 #define [\\_TIFA\\_MESSAGES\\_H\\_](#)

Standard include guard.

Definition at line 41 of file messages.h.

## 5.24 print\_error.h File Reference

Error printing macro.

```
#include "tifa_config.h"
```

## Defines

- [#define \\_TIFA\\_PRINT\\_ERROR\\_H\\_](#)

### 5.24.1 Detailed Description

Error printing macro.

#### Author:

Jerome Milan

#### Date:

Fri Jun 10 2011

#### Version:

2011-06-10

This file defines a macro used to output critical error messages on stderr if the global symbol TIFA\_PRINT\_ERROR is set to non-zero.

Definition in file [print\\_error.h](#).

### 5.24.2 Define Documentation

#### 5.24.2.1 [#define \\_TIFA\\_PRINT\\_ERROR\\_H\\_](#)

Standard include guard.

Definition at line 37 of file [print\\_error.h](#).

## 5.25 res\_tdiv.h File Reference

Trial division of residues with optional early abort.

```
#include <inttypes.h>
#include "smooth_filter.h"
```

## Defines

- [#define \\_TIFA\\_RES\\_TDIV\\_H\\_](#)

## Functions

- `uint32_t res_tdiv (smooth_filter_t *const filter, unsigned long int step)`  
*Trial divide residues using data from a smooth\_filter\_t.*

### 5.25.1 Detailed Description

Trial division of residues with optional early abort.

**Author:**

Jerome Milan

**Date:**

Fri Jun 10 2011

**Version:**

2011-06-10

This file defines functions used to trial divide residues on a factor base using optional multi-step early abort.

C. Pomerance, *Analysis and Comparison of Some Integer Factoring Algorithms*, in Mathematical Centre Tracts 154.

Definition in file [res\\_tdiv.h](#).

### 5.25.2 Define Documentation

#### 5.25.2.1 #define \_TIFA\_RES\_TDIV\_H\_

Standard include guard.

Definition at line 39 of file [res\\_tdiv.h](#).

### 5.25.3 Function Documentation

#### 5.25.3.1 uint32\_t res\_tdiv (smooth\_filter\_t \*const filter, unsigned long int step)

Trial divide residues using data from a `smooth_filter_t`.

Filters the relations given by `filter->candidate_*` via trial division at the `step`-th early abort step and stores the 'good' relations in `filter->accepted_*`. The `step` parameter has no effect if `filter->method == TDIV` (i.e. no early abort variation).

**Warning:**

This function is only meant to be used if `filter->method == TDIV` is either `TDIV` or `TDIV_early_abort`.

**Parameters:**

← *filter* a pointer to the `smooth_filter_t` to use.

← *step* the step in the early abort strategy to perform.

## 5.26 siqs.h File Reference

The Self-Initializing Quadratic Sieve factorization algorithm.

```
#include <stdbool.h>
```

```
#include <inttypes.h>
#include <gmp.h>
#include "array.h"
#include "lindep.h"
#include "factoring_machine.h"
#include "exit_codes.h"
```

### Data Structures

- struct [struct\\_siqs\\_params\\_t](#)  
*Defines the variable parameters used in the SIQS algorithm.*

### Defines

- #define [\\_TIFA\\_SIQS\\_H\\_](#)
- #define [SIQS\\_DFLT\\_SIEVE\\_HALF\\_WIDTH](#) 500000
- #define [SIQS\\_DFLT\\_NPRIMES\\_IN\\_BASE](#) NFIRST\_PRIMES/16
- #define [SIQS\\_DFLT\\_NPRIMES\\_TDIV](#) NFIRST\_PRIMES/16
- #define [SIQS\\_DFLT\\_NRELATIONS](#) 24
- #define [SIQS\\_DFLT\\_LINALG\\_METHOD](#) SMART\_GAUSS\_ELIM
- #define [SIQS\\_DFLT\\_USE\\_LARGE\\_PRIMES](#) true

### Typedefs

- typedef struct [struct\\_siqs\\_params\\_t](#) [siqs\\_params\\_t](#)  
*Equivalent to struct [struct\\_siqs\\_params\\_t](#).*

### Functions

- void [set\\_siqs\\_params\\_to\\_default](#) (const mpz\_t n, [siqs\\_params\\_t](#) \*const params)  
*Fills a [siqs\\_params\\_t](#) with default values.*
- [ecode\\_t](#) [siqs](#) ([mpz\\_array\\_t](#) \*const factors, [uint32\\_array\\_t](#) \*const multis, const mpz\_t n, const [siqs\\_params\\_t](#) \*const params, const [factoring\\_mode\\_t](#) mode)  
*Integer factorization via the self-initializing quadratic sieve (SIQS) algorithm.*

#### 5.26.1 Detailed Description

The Self-Initializing Quadratic Sieve factorization algorithm.

#### Author:

Jerome Milan

**Date:**

Fri Jun 10 2011

**Version:**

2011-06-10

Definition in file [siqs.h](#).

**5.26.2 Define Documentation****5.26.2.1 #define \_TIFA\_SIQS\_H\_**

Standard include guard.

Definition at line 33 of file siqs.h.

**5.26.2.2 #define SIQS\_DFLT\_LINALG\_METHOD SMART\_GAUSS\_ELIM**

Default linear system resolution method to use.

Definition at line 75 of file siqs.h.

**5.26.2.3 #define SIQS\_DFLT\_NPRIMES\_IN\_BASE NFIRST\_PRIMES/16**

Default number of prime numbers composing the factor base on which to factor the residues.

Definition at line 58 of file siqs.h.

**5.26.2.4 #define SIQS\_DFLT\_NPRIMES\_TDIV NFIRST\_PRIMES/16**

Default number of the first primes to use in the trial division of the residues.

Definition at line 64 of file siqs.h.

**5.26.2.5 #define SIQS\_DFLT\_NRELATIONS 24**

Default number of congruence relations to find before attempting the factorization of the large integer.

Definition at line 70 of file siqs.h.

**5.26.2.6 #define SIQS\_DFLT\_SIEVE\_HALF\_WIDTH 500000**

Default sieving half-width.

Definition at line 52 of file siqs.h.

**5.26.2.7 #define SIQS\_DFLT\_USE\_LARGE\_PRIMES true**

Use the large prime variation by default.

Definition at line 80 of file siqs.h.

### 5.26.3 Function Documentation

#### 5.26.3.1 void set\_siqs\_params\_to\_default (const mpz\_t n, siqs\_params\_t \*const params)

Fills a `siqs_params_t` with default values.

Fills a `siqs_params_t` with default values.

##### Parameters:

- ← *n* The number to factor.
- *params* A pointer to the `siqs_params_t` structure to fill.

#### 5.26.3.2 ecode\_t siqs (mpz\_array\_t \*const factors, uint32\_array\_t \*const multis, const mpz\_t n, const siqs\_params\_t \*const params, const factoring\_mode\_t mode)

Integer factorization via the self-initializing quadratic sieve (SIQS) algorithm.

Attempts to factor the non perfect square integer `n` with the SIQS algorithm, using the set of parameters given by `params` and the factoring mode given by `mode`. Found factors are then stored in `factors`. Additionally, if the factoring mode used is set to `FIND_COMPLETE_FACTORIZATION`, factors' multiplicities are stored in the array `multis`.

##### Note:

If the factoring mode used is different from `FIND_COMPLETE_FACTORIZATION`, `multis` is allowed to be a NULL pointer. Otherwise, using a NULL pointer will lead to a fatal error.

##### Warning:

If the `factors` and `multis` arrays have not enough room to store the found factors (and the multiplicities, if any), they will be automatically resized to accommodate the data. This has to be kept in mind when trying to do ingenious stuff with memory management (hint: don't try to be clever here).

##### Parameters:

- *factors* Pointer to the found factors of `n`.
- *multis* Pointer to the multiplicities of the found factors (only computed if `mode` is set to `FIND_COMPLETE_FACTORIZATION`).
- ← *n* The non perfect square integer to factor.
- ← *params* Pointer to the values of the parameters used in the SIQS algorithm.
- ← *mode* The factoring mode to use.

##### Returns:

An exit code.

## 5.27 siqs\_poly.h File Reference

Structure and functions related to the polynomials used in the SIQS algorithm.

```
#include <stdint.h>
#include <stdbool.h>
#include <gmp.h>
```



```
#include "exit_codes.h"
#include "array.h"
#include "approx.h"
```

### Data Structures

- struct [struct\\_siqs\\_poly\\_t](#)  
*Defines polynomials used by SIQS.*

### Typedefs

- typedef struct [struct\\_siqs\\_poly\\_t](#) [siqs\\_poly\\_t](#)  
*Equivalent to [struct\\_siqs\\_poly\\_t](#).*

### Functions

- [siqs\\_poly\\_t \\* alloc\\_siqs\\_poly](#) ([mpz\\_t](#) target\_a, [mpz\\_t](#) n, [uint32\\_array\\_t \\*const](#) factor\_base, [uint32\\_array\\_t \\*const](#) sqrtm\_pi)  
*Allocates and returns a new [siqs\\_poly\\_t](#).*
- void [free\\_siqs\\_poly](#) ([siqs\\_poly\\_t \\*poly](#))  
*Frees a previously allocated [siqs\\_poly\\_t](#).*
- [ecode\\_t](#) [update\\_polynomial](#) ([siqs\\_poly\\_t \\*const](#) poly)  
*Updates a polynomial.*
- int [na\\_used](#) ([siqs\\_poly\\_t \\*const](#) poly)  
*Returns the number of "full" initialization performed.*

#### 5.27.1 Detailed Description

Structure and functions related to the polynomials used in the SIQS algorithm.

**Author:**

Jerome Milan

**Date:**

Fri Jun 10 2011

**Version:**

2011-06-10

Definition in file [siqs\\_poly.h](#).

## 5.27.2 Function Documentation

### 5.27.2.1 `siqs_poly_t* alloc_siqs_poly (mpz_t target_a, mpz_t n, uint32_array_t *const factor_base, uint32_array_t *const sqrtm_pi)`

Allocates and returns a new `siqs_poly_t`.

#### Parameters:

*target\_a* the target leading coefficient to approximate.

*n* the number to factor (or a small multiple).

*factor\_base* the factor base.

*sqrtm\_pi* the modular square roots of *n*.

#### Returns:

A pointer to the newly allocated `siqs_poly_t`.

### 5.27.2.2 `void free_siqs_poly (siqs_poly_t *poly)`

Frees a previously allocated `siqs_poly_t`.

Frees all memory used by the pointed `siqs_poly_t` and then frees the `poly` pointer.

#### Warning:

Do not call `free(poly)` in client code after a call to `free_siqs_poly(poly)`: it would result in an error.

#### Parameters:

*poly* the `siqs_poly_t` to free.

### 5.27.2.3 `int na_used (siqs_poly_t *const poly)`

Returns the number of "full" initialization performed.

This is also the number of distinct *a* used.

#### Parameters:

*poly* the polynomial used.

#### Returns:

The number of "full" initialization performed.

### 5.27.2.4 `ecode_t update_polynomial (siqs_poly_t *const poly)`

Updates a polynomial.

Updates the polynomial `poly` by either, deriving a new *b* value (the so-called "fast" initialization) or by computing a new leading coefficient (the "full" or "slow" initialization).

**Parameters:**

*poly* the polynomial to update.

**Returns:**

An error code (either SUCCESS or FATAL\_INTERNAL\_ERROR)

## 5.28 siqs\_sieve.h File Reference

Structure and functions related to the sieve used in the SIQS algorithm.

```
#include <stdint.h>
#include <stdbool.h>
#include <gmp.h>
#include "exit_codes.h"
#include "array.h"
#include "approx.h"
#include "buckets.h"
#include "siqs_poly.h"
#include "stopwatch.h"
```

**Data Structures**

- struct [struct\\_siqs\\_sieve\\_t](#)  
*Defines the sieve used by SIQS.*

**Typedefs**

- typedef struct [struct\\_siqs\\_sieve\\_t](#) [siqs\\_sieve\\_t](#)  
*Equivalent to [struct\\_siqs\\_sieve\\_t](#).*

**Functions**

- [siqs\\_sieve\\_t \\* alloc\\_siqs\\_sieve](#) (mpz\_t n, [uint32\\_array\\_t](#) \*const factor\_base, [byte\\_array\\_t](#) \*const log\_primes, [uint32\\_array\\_t](#) \*const sqrtm\_pi, [uint32\\_t](#) half\_width)  
*Allocates and returns a new [siqs\\_sieve\\_t](#).*
- void [free\\_siqs\\_sieve](#) ([siqs\\_sieve\\_t](#) \*sieve)  
*Frees a previously allocated [siqs\\_sieve\\_t](#).*
- [ecode\\_t fill\\_sieve](#) ([siqs\\_sieve\\_t](#) \*const sieve)  
*Fills the next chunk of an [siqs\\_sieve\\_t](#).*
- [ecode\\_t scan\\_sieve](#) ([siqs\\_sieve\\_t](#) \*const sieve, [int32\\_array\\_t](#) \*const survivors, [uint32\\_t](#) nsurvivors)  
*Scans a chunk of an [siqs\\_sieve\\_t](#).*

- void `set_siqs_sieve_threshold` (`siqs_sieve_t *const sieve`, `uint32_t threshold`)  
*Sets the `siqs_sieve_t`'s threshold.*
- void `print_init_poly_timing` (`siqs_sieve_t *const sieve`)  
*Prints an `siqs_sieve_t`'s poly init timing.*
- void `print_fill_timing` (`siqs_sieve_t *const sieve`)  
*Prints an `siqs_sieve_t`'s fill timing.*
- void `print_scan_timing` (`siqs_sieve_t *const sieve`)  
*Prints an `siqs_sieve_t`'s scan timing.*

### 5.28.1 Detailed Description

Structure and functions related to the sieve used in the SIQS algorithm.

**Author:**

Jerome Milan

**Date:**

Fri Jun 10 2011

**Version:**

2011-06-10

Definition in file [siqs\\_sieve.h](#).

### 5.28.2 Function Documentation

#### 5.28.2.1 `siqs_sieve_t* alloc_siqs_sieve` (`mpz_t n`, `uint32_array_t *const factor_base`, `byte_array_t *const log_primes`, `uint32_array_t *const sqrtm_pi`, `uint32_t half_width`)

Allocates and returns a new `siqs_sieve_t`.

**Parameters:**

*n* the number to factor (or a small multiple)

*factor\_base* the factor base

*log\_primes* logarithms (in base 2) of the primes in the base

*sqrtm\_pi* modular square roots of *n* for each prime in the base

*half\_width* the (approximate) *half\_width* of the sieving interval (the real *half\_width* will be adjusted to be a multiple of *chunk\_size* if `ROUND_HALF_WIDTH` is defined as non zero)

**Returns:**

A pointer to the newly allocated `siqs_sieve_t`.

### 5.28.2.2 `ecode_t fill_sieve (siqs_sieve_t *const sieve)`

Fills the next chunk of an `siqs_sieve_t`.

Fills the next chunk of `sieve`, transparently updating (if needed) the polynomial used.

#### Parameters:

*sieve* the `siqs_sieve_t` to fill.

#### Returns:

An exit code.

### 5.28.2.3 `void free_siqs_sieve (siqs_sieve_t *sieve)`

Frees a previously allocated `siqs_sieve_t`.

Frees all memory used by the pointed `siqs_sieve_t` and then frees the `sieve` pointer.

#### Warning:

Do not call `free(sieve)` in client code after a call to `free_siqs_sieve(sieve)`: it would result in an error.

#### Parameters:

*sieve* the `siqs_sieve_t` to free.

### 5.28.2.4 `void print_fill_timing (siqs_sieve_t *const sieve)`

Prints an `siqs_sieve_t`'s fill timing.

Prints the time taken by `sieve` to fill its sieve chunks.

#### Parameters:

*sieve* the `siqs_sieve_t` to read.

### 5.28.2.5 `void print_init_poly_timing (siqs_sieve_t *const sieve)`

Prints an `siqs_sieve_t`'s poly init timing.

Prints the time taken by `sieve` to initialize its polynomials.

#### Parameters:

*sieve* the `siqs_sieve_t` to read.

### 5.28.2.6 `void print_scan_timing (siqs_sieve_t *const sieve)`

Prints an `siqs_sieve_t`'s scan timing.

Prints the time taken by `sieve` to scan its sieve chunks.

#### Parameters:

*sieve* the `siqs_sieve_t` to read.

**5.28.2.7** `ecode_t scan_sieve (siqs_sieve_t *const sieve, int32_array_t *const survivors, uint32_t nsurvivors)`

Scans a chunk of an `siqs_sieve_t`.

Scans the last filled chunk of `sieve`.

**Parameters:**

*sieve* the `siqs_sieve_t` to scan.

**Returns:**

An exit code.

**5.28.2.8** `void set_siqs_sieve_threshold (siqs_sieve_t *const sieve, uint32_t threshold)`

Sets the `siqs_sieve_t`'s threshold.

Sets `sieve`'s threshold (all positions `xi` with `sieve[xi] < threshold` will be tested for smoothness).

**Parameters:**

*sieve* the `siqs_sieve_t` to update.

*threshold* the new threshold's value.

**5.29** `smooth_filter.h` File Reference

Smooth integer filter.

```
#include <inttypes.h>
#include <array.h>
#include <hashtable.h>
#include <gmp.h>
```

**Data Structures**

- struct [struct\\_smooth\\_filter\\_t](#)  
*Structure grouping variables needed for multi-step early abort strategy.*

**Defines**

- #define [\\_TIFA\\_SMOOTH\\_FILTER\\_H\\_](#)
- #define [MAX\\_NSTEPS](#) 4

**Typedefs**

- typedef struct [struct\\_smooth\\_filter\\_t](#) [smooth\\_filter\\_t](#)  
*Equivalent to struct [struct\\_smooth\\_filter\\_t](#).*
- typedef enum [smooth\\_filter\\_method\\_enum](#) [smooth\\_filter\\_method\\_t](#)  
*Equivalent to enum [smooth\\_filter\\_method\\_enum](#).*

## Enumerations

- enum `smooth_filter_method_enum` { `TDIV = 0`, `TDIV_EARLY_ABORT`, `DJB_BATCH` }

## Functions

- void `complete_filter_init` (`smooth_filter_t *const filter`, `uint32_array_t *const base`)  
*Complete initialization of a `smooth_filter_t`.*
- void `clear_smooth_filter` (`smooth_filter_t *const filter`)  
*Clears a `smooth_filter_t`.*
- void `filter_new_relations` (`smooth_filter_t *const filter`)  
*Filters new relations to keep 'good' ones.*
- void `print_filter_status` (`smooth_filter_t *const filter`)  
*Prints the status of the buffers of a `smooth_filter_t`.*

## Variables

- static const char \*const `filter_method_to_str` [3]

### 5.29.1 Detailed Description

Smooth integer filter.

#### Author:

Jerome Milan

#### Date:

Fri Jun 10 2011

#### Version:

2011-06-10

The `smooth_filter_t` structure and its associated functions implement the multi-step early abort strategy in a way reminiscent of Pomerance's suggestion in "Analysis and Comparison of Some Integer Factoring Algorithm" with the exception that the smoothness tests are performed by batch (see [bernsteinisms.h](#)) instead of trial division.

**How to use a `smooth_filter_t` structure?** The following code snippet, while incomplete, illustrates the way a `smooth_filter_t` should be used.

```
//  
// Fill the with the smooth_filter_t with our parameters...  
//  
smooth_filter_t filter;  
filter.n          = n;    // number to factor  
filter.kn         = kn;   // number to factor x multiplier
```

```
filter.batch_size = 1024; // number of relations to perform a batch
filter.methodid   = TDIV_EARLY_ABORT; // use the early abort strategy
filter.nsteps     = 2; // use a 2-step early abort strategy

filter.htable     =htable;
filter.use_large_primes = true;
filter.use_sigs_batch_variant = false;

filter.base_size  = factor_base->length; // size of factor base
filter.candidate_xi = candidate_xi; // candidate relations stored
filter.candidate_yi = candidate_yi; // in candidate_* arrays
filter.accepted_xi  = accepted_xi; // 'good' relations stored
filter.accepted_yi  = accepted_yi; // in accepted_* arrays
//
// Complete the filter initialization by allocating its internal
// buffers, computing the early abort bounds and the intermediate
// factor bases...
//
complete_filter_init(&filter, factor_base);

while (accepted_yi->length != nrels_to_collect) {
    //
    // While we don't have enough relations, create new ones and
    // stores them in the candidate_* arrays such that
    // yi = xi^2 (mod kn). (The generate_relations function here
    // is completely fictitious)
    //
    generate_relations(candidate_xi, candidate_yi);

    //
    // Select 'good' relations such that yi = xi^2 (mod kn) with
    // yi smooth. Note that pointers to the candidate_* and
    // accepted_* arrays were given in the filter structure.
    //
    filter_new_relations(&filter);
}
//
// This clears _only_ the memory allocated by complete_init_filter.
//
clear_smooth_filter(&filter);
```

Definition in file [smooth\\_filter.h](#).

## 5.29.2 Define Documentation

### 5.29.2.1 `#define TIFA_SMOOTH_FILTER_H_`

Standard include guard.

Definition at line 95 of file `smooth_filter.h`.

### 5.29.2.2 `#define MAX_NSTEPS 4`

Maximum number of steps used in the multi-step early abort strategy.

Definition at line 110 of file `smooth_filter.h`.

## 5.29.3 Enumeration Type Documentation

### 5.29.3.1 `enum smooth_filter_method_enum`



An enumeration of the possible methods used to test residue smoothness.

**Enumerator:**

*TDIV* Simple trial division.

*TDIV\_EARLY\_ABORT* Simple trial division with (multi-step) early abort.

*DJB\_BATCH* D. Bernstein's batch method described in "How to find smooth parts of integers",  
<http://cr.yep.to/factorization/smoothparts-20040510.pdf>.

Definition at line 117 of file `smooth_filter.h`.

### 5.29.4 Function Documentation

#### 5.29.4.1 `void clear_smooth_filter (smooth_filter_t *const filter)`

Clears a `smooth_filter_t`.

Clears the memory of a `smooth_filter_t` that was allocated by `complete_filter_init()`.

**Warning:**

This clears *only* the internal buffers allocated by by `complete_filter_init()`, and not the whole structure. For example, it is still the responsibility of the client code to properly clear the `candidate_*` arrays or the `htable` hashtable.

#### 5.29.4.2 `void complete_filter_init (smooth_filter_t *const filter, uint32_array_t *const base)`

Complete initialization of a `smooth_filter_t`.

Complete the initialization of a `smooth_filter_t` by allocating needed memory space.

**Warning:**

It is the responsibility of the client code to set the following structure variables *before* calling this function:

- `n`
- `kn`
- `nsteps`
- `batch_size`
- `base_size`
- `htable`
- `candidate_xi`
- `candidate_yi`
- `accepted_xi`
- `accepted_yi`
- `use_large_primes`

- use\_sigs\_batch\_variant

No pointer ownership is transferred. For example, it is still the responsibility of the client code to properly clear the `candidate_*` arrays since the structure just *refers* to them, but does not *own* them.

**Note:**

If `nsteps > MAX_NSTEPS` then `complete_filter_init` will set it to `MAX_NSTEPS`.

**Warning:**

If `method == DJB_BATCH` then `nsteps` will be set to 0 and no early abort will be performed.

**Parameters:**

- filter* a pointer to the `smooth_filter_t` to initialize
- base* a pointer to the complete factor base used

**5.29.4.3 void filter\_new\_relations (smooth\_filter\_t \*const filter)**

Filters new relations to keep 'good' ones.

Filters the relations given by `filter->candidate_*` via a smoothness detecting batch using a `filter->nsteps` steps early abort strategy and stores the 'good' relations in `filter->accepted_*`. Has no effect if the `filter->candidate_*` are not full since we need `filter->batch_size` relations to perform a batch.

**Parameters:**

- filter* a pointer to the `smooth_filter_t` used

**5.29.4.4 void print\_filter\_status (smooth\_filter\_t \*const filter)**

Prints the status of the buffers of a `smooth_filter_t`.

Prints a status summary of the internal buffers of a `smooth_filter_t` on the standard output.

**Note:**

This function is mostly intended for debugging purposes as the output is not particularly well structured.

**Parameters:**

- filter* a pointer to the `smooth_filter_t` to inspect

**5.29.5 Variable Documentation****5.29.5.1 const char\* const filter\_method\_to\_str[3] [static]****Initial value:**

```
{
    "trial division",
    "trial division + early abort",
    "batch",
}
```

Global constant array mapping filter methods to their string representations.

Definition at line 143 of file `smooth_filter.h`.

## 5.30 `sqrt_cont_frac.h` File Reference

Continued fraction expansion for square root of integers.

```
#include <inttypes.h>
```

```
#include <gmp.h>
```

### Data Structures

- struct [struct\\_cont\\_frac\\_state\\_t](#)  
*An ad-hoc structure for the computation of the continued fraction of a square root.*

### Defines

- #define [\\_TIFA\\_SQRT\\_CONT\\_FRAC\\_H\\_](#)

### Typedefs

- typedef struct [struct\\_cont\\_frac\\_state\\_t](#) [cont\\_frac\\_state\\_t](#)  
*Equivalent to struct [struct\\_cont\\_frac\\_state\\_t](#).*

### Functions

- void [init\\_cont\\_frac\\_state](#) ([cont\\_frac\\_state\\_t](#) \*const state, const [mpz\\_t](#) n)  
*Initializes a [cont\\_frac\\_state\\_t](#).*
- void [clear\\_cont\\_frac\\_state](#) ([cont\\_frac\\_state\\_t](#) \*const state)  
*Clears a [cont\\_frac\\_state\\_t](#).*
- static void [step\\_cont\\_frac\\_state](#) ([cont\\_frac\\_state\\_t](#) \*const state, [uint32\\_t](#) nsteps)  
*Computes another term of a continued fraction.*

#### 5.30.1 Detailed Description

Continued fraction expansion for square root of integers.

#### Author:

Jerome Milan

#### Date:

Fri Jun 10 2011

**Version:**

2011-06-10

Defines the continued fraction expansion for the square root of non-perfect square integers.

The expansion is computed via an iterative process, each step giving the value of a new numerator. All the variables needed to perform this computation is stored in an ad-hoc structure called `struct_cont_frac_state_t`.

**Note:**

Since the denominator of the continued fraction is not used in the CFRAC algorithm, it is not computed here. Also, the numerator of the fraction is only given modulo  $n$ . These restrictions are completely trivial to fix should one need the complete approximation  $a/b$  of a square root.

Definition in file `sqrt_cont_frac.h`.

**5.30.2 Define Documentation****5.30.2.1 `#define _TIFA_SQRT_CONT_FRAC_H_`**

Standard include guard.

Definition at line 47 of file `sqrt_cont_frac.h`.

**5.30.3 Function Documentation****5.30.3.1 `void clear_cont_frac_state (cont_frac_state_t *const state)`**

Clears a `cont_frac_state_t`.

Clears a `cont_frac_state_t`.

**Parameters:**

← *state* A pointer to the `cont_frac_state_t` to clear.

**5.30.3.2 `void init_cont_frac_state (cont_frac_state_t *const state, const mpz_t n)`**

Initializes a `cont_frac_state_t`.

Initializes a `cont_frac_state_t` to begin the computation of a continued fraction. After invocation of this function, the fields of *state* corresponds to the calculation of the second term of the computed fraction, the first term being of course `ceil(sqrt(n))`.

**Parameters:**

← *state* A pointer to the `cont_frac_state_t` to initialize.

← *n* The non perfect square integer whose square root will be approximated by the computation of a continued fraction.

**5.30.3.3** `static void step_cont_frac_state (cont_frac_state_t *const state, uint32_t nsteps)`  
[inline, static]

Computes another term of a continued fraction.

Computes another coefficient in the expansion of a continued fraction and updates the structure `state`. The parameter `nsteps` gives the number of iteration to perform. A new term is computed at each iteration.

**Note:**

This function is actually given by `state->step_function`.

**Parameters:**

- ← `state` A pointer to the `cont_frac_state_t`.
- ← `nsteps` Number of steps to perform.

Definition at line 192 of file `sqrt_cont_frac.h`.

References `struct_cont_frac_state_t::step_function`.

## 5.31 squfof.h File Reference

The SQUFOF factorization algorithm.

```
#include <stdlib.h>
#include <gmp.h>
#include "array.h"
#include "factoring_machine.h"
#include "exit_codes.h"
```

### Data Structures

- struct [struct\\_squfof\\_params\\_t](#)  
*Defines the variable parameters used in the SQUFOF algorithm (dummy structure).*

### Defines

- #define [\\_TIFA\\_SQUFOF\\_H\\_](#)

### Typedefs

- typedef struct [struct\\_squfof\\_params\\_t](#) [squfof\\_params\\_t](#)  
*Equivalent to struct [struct\\_squfof\\_params\\_t](#).*

### Functions

- void [set\\_squfof\\_params\\_to\\_default](#) ([squfof\\_params\\_t](#) \*const params)

Fills a `squfof_params_t` with default values (dummy function).

- `ecode_t squfof` (`mpz_array_t *const factors`, `uint32_array_t *const multis`, `const mpz_t n`, `const squfof_params_t *const params`, `const factoring_mode_t mode`)

Integer factorization via the square form factorization (SQUFOF) algorithm.

### 5.31.1 Detailed Description

The SQUFOF factorization algorithm.

**Author:**

Jerome Milan

**Date:**

Fri Jun 10 2011

**Version:**

2011-06-10

This is the TIFA library's implementation of Shanks' square form factorization algorithm (SQUFOF), based on the description given by Jason Gower and Samuel Wagstaff in their paper "Square Form Factorization" to be published in *Mathematics of Computation*.

**Note:**

This implementation can only factor numbers whose size is less than twice the size of an unsigned long int.

**See also:**

"Square Form Factorization", Jason E. Gower & Samuel S. Wagstaff Jr. *Mathematics of Computation*, S 0025-5718(07)02010-8, Article electronically published on May 14, 2007.

"Square Form Factorization", Jason E. Gower, PhD thesis, Purdue University, December 2004.

For a description of the "large step algorithm" used to quickly jump over several forms, see: "On the Parallel Generation of the Residues for the Continued Fraction Factoring Algorithm", Hugh C. Williams, Marvin C. Wunderlich, *Mathematics of Computation*, Volume 48, Number 177, January 1987, pages 405-423

Definition in file [squfof.h](#).

### 5.31.2 Define Documentation

#### 5.31.2.1 `#define _TIFA_SQUFOF_H_`

Standard include guard.

Definition at line 54 of file `squfof.h`.

### 5.31.3 Function Documentation

#### 5.31.3.1 `void set_squfof_params_to_default (squfof_params_t *const params)`

Fills a `squfof_params_t` with default values (dummy function).

This function is intended to fill a `squfof_params_t` with default values.

#### Warning:

For the time being, this is a dummy function which does absolutely nothing at all, but is kept only as a placeholder should the need for user parameters arise in future code revisions.

#### Parameters:

*params* A pointer to the `squfof_params_t` structure to fill.

#### 5.31.3.2 `ecode_t squfof (mpz_array_t *const factors, uint32_array_t *const multis, const mpz_t n, const squfof_params_t *const params, const factoring_mode_t mode)`

Integer factorization via the square form factorization (SQUFOF) algorithm.

Attempts to factor the non perfect square integer *n* with the SQUFOF algorithm, using the factoring mode given by *mode*. Found factors are then stored in *factors*. Additionally, if the factoring mode used is set to `FIND_COMPLETE_FACTORIZATION`, factors' multiplicities are stored in the array *multis*.

#### Warning:

This implementation can only factor numbers whose sizes in bits are strictly less than twice the size of an `unsigned long int` (the exact limit depending on the number to factor and the multiplier used). This choice was made because most of the computations are then performed using only single precision operations. Such a limitation should not be much of a problem since SQUFOF is mostly used to factor very small integers (up to, say, 20 decimal digits).

#### Note:

If the factoring mode used is different from `FIND_COMPLETE_FACTORIZATION`, *multis* is allowed to be a `NULL` pointer. Otherwise, using a `NULL` pointer will lead to a fatal error.

#### Warning:

If the *factors* and *multis* arrays have not enough room to store the found factors (and the multiplicities, if any), they will be automatically resized to accommodate the data. This has to be kept in mind when trying to do ingenious stuff with memory management (hint: don't try to be clever here).

#### Parameters:

- *factors* Pointer to the found factors of *n*.
- *multis* Pointer to the multiplicities of the found factors (only computed if *mode* is set to `FIND_COMPLETE_FACTORIZATION`).
- ← *n* The non perfect square integer to factor.
- ← *params* SQUFOF's parameters (currently unused).
- ← *mode* The factoring mode to use.

#### Returns:

An exit code.

## 5.32 stopwatch.h File Reference

A very basic stopwatch-like timer.

```
#include <sys/resource.h>
#include <sys/time.h>
#include <stdint.h>
#include <stdbool.h>
```

### Data Structures

- struct [struct\\_stopwatch\\_t](#)  
*Defines a very basic stopwatch-like timer.*

### Defines

- #define [\\_TIFA\\_STOPWATCH\\_H\\_](#)

### Typedefs

- typedef struct [struct\\_stopwatch\\_t](#) [stopwatch\\_t](#)  
*Equivalent to struct [struct\\_stopwatch\\_t](#).*

### Functions

- void [init\\_stopwatch](#) ([stopwatch\\_t](#) \*const watch)  
*Inits a [stopwatch\\_t](#).*
- void [start\\_stopwatch](#) ([stopwatch\\_t](#) \*const watch)  
*Starts a [stopwatch\\_t](#).*
- void [stop\\_stopwatch](#) ([stopwatch\\_t](#) \*const watch)  
*Stop a [stopwatch\\_t](#).*
- void [reset\\_stopwatch](#) ([stopwatch\\_t](#) \*const watch)  
*Reset a [stopwatch\\_t](#).*
- double [get\\_stopwatch\\_elapsed](#) ([stopwatch\\_t](#) \*const watch)  
*Returns the elapsed time measured.*

#### 5.32.1 Detailed Description

A very basic stopwatch-like timer.



**Author:**

Jerome Milan

**Date:**

Fri Jun 10 2011

**Version:**

2011-06-10

This file implements a very basic stopwatch-like timer (with microsecond precision) based on the `rusage` structure and using the `get_rusage` function.

Definition in file [stopwatch.h](#).

**5.32.2 Define Documentation****5.32.2.1 #define \_TIFA\_STOPWATCH\_H\_**

Standard include guard.

Definition at line 37 of file `stopwatch.h`.

**5.32.3 Function Documentation****5.32.3.1 double get\_stopwatch\_elapsed (stopwatch\_t \*const watch)**

Returns the elapsed time measured.

Returns the elapsed time measured by `watch` in seconds.

**Warning:**

The returned result is only meaningful if the stopwatch is not running (i.e. it has been stopped with the `stop_stopwatch` function).

**Parameters:**

← *watch* The `stopwatch_t` used for timing.

**5.32.3.2 void init\_stopwatch (stopwatch\_t \*const watch)**

Initiates a `stopwatch_t`.

Initializes the `stopwatch_t` pointed to by `watch`.

**Parameters:**

*watch* The `stopwatch_t` to init.

**5.32.3.3 void reset\_stopwatch (stopwatch\_t \*const watch)**

Reset a `stopwatch_t`.

Reset the `stopwatch_t` pointed to by `watch`. The stopwatch is *not* stopped and will continue to run unless it was already stopped.

**Parameters:**

*watch* The stopwatch\_t to reset.

**5.32.3.4 void start\_stopwatch (stopwatch\_t \*const watch)**

Starts a stopwatch\_t.

Starts the stopwatch\_t pointed to by watch.

**Note:**

Consecutive calls to start\_stopwatch are without effect.

**Parameters:**

*watch* The stopwatch\_t to start.

**5.32.3.5 void stop\_stopwatch (stopwatch\_t \*const watch)**

Stop a stopwatch\_t.

Stop the stopwatch\_t pointed to by watch. Successive calls to start\_stopwatch and stop\_stopwatch are cumulative. In other words, the stopwatch's state holds the time elapsed during all previous time intervals defined by a call to start\_stopwatch followed by a call to stop\_stopwatch (provided that the stopwatch was not reset with reset\_stopwatch).

**Note:**

Consecutive calls to stop\_stopwatch are without effect.

**Parameters:**

*watch* The stopwatch\_t to stop.

**5.33 tdiv.h File Reference**

The trial division factorization algorithm.

```
#include <inttypes.h>
#include <gmp.h>
#include "array.h"
#include "factoring_machine.h"
#include "exit_codes.h"
```

**Defines**

- #define `_TIFA_TDIV_H_`
- #define `TDIV_DFLT_NPRIMES_TDIV` (NFIRST\_PRIMES/32)

## Functions

- `ecode_t tdiv (mpz_array_t *const factors, uint32_array_t *const multis, const mpz_t n, const uint32_t nprimes)`

*Integer factorization via trial division (TDIV).*

### 5.33.1 Detailed Description

The trial division factorization algorithm.

#### Author:

Jerome Milan

#### Date:

Fri Jun 10 2011

#### Version:

2011-06-10

Naive (partial) factorization via trial divisions by a few small primes.

Definition in file [tdiv.h](#).

### 5.33.2 Define Documentation

#### 5.33.2.1 `#define _TIFA_TDIV_H_`

Standard include guard.

Definition at line 35 of file [tdiv.h](#).

#### 5.33.2.2 `#define TDIV_DFLT_NPRIMES_TDIV (NFIRST_PRIMES/32)`

Default number of the first primes to use for trial division.

Definition at line 52 of file [tdiv.h](#).

### 5.33.3 Function Documentation

#### 5.33.3.1 `ecode_t tdiv (mpz_array_t *const factors, uint32_array_t *const multis, const mpz_t n, const uint32_t nprimes)`

Integer factorization via trial division (TDIV).

Attempts to factor the integer `n` via trial division by the first `nprimes` primes. Found factors are then stored in the array `factors` and multiplicities are stored in `multis`.

Returns:

- `COMPLETE_FACTORIZATION_FOUND` if the complete factorization of `n` was found.

- `SOME_FACTORS_FOUND` if some factors were found but could not account for the complete factorization of `n`. In that case, the unfactored part of `n` is stored in `factors->data[factors->lenth - 1]`.
- `NO_FACTOR_FOUND` if no factor were found.

**Warning:**

The prime numbers are not computed but read from a table. Consequently the number of primes `nprimes` should be less than or equal to `NFIRST_PRIMES` (defined in [array.h](#)). If `nprimes` is zero, then the default value `DFLT_TDIV_NPRIMES` will be used instead.

**Parameters:**

- *factors* Pointer to the found factors of `n`.
- *multis* Pointer to the multiplicities of the found factors.
- ← *n* The integer to factor.
- ← *nprimes* The number of primes to trial divide `n` by.

**Returns:**

An exit code.

## 5.34 tifa.h File Reference

Library wide public include file.

```
#include "tifa_config.h"
#include "cfrac.h"
#include "ecm.h"
#include "fermat.h"
#include "qs.h"
#include "siqs.h"
#include "squfof.h"
#include "tdiv.h"
#include "tifa_factor.h"
#include "first_primes.h"
#include "array.h"
#include "exit_codes.h"
#include "factoring_machine.h"
```

**Defines**

- `#define \_TIFA\_TIFA\_H`

### 5.34.1 Detailed Description

Library wide public include file.

**Author:**

Jerome Milan

**Date:**

Fri Jun 10 2011

**Version:**

2011-06-10

Includes only TIFA's structures and functions needed from client code perspective.

Definition in file [tifa.h](#).

### 5.34.2 Define Documentation

#### 5.34.2.1 #define \_TIFA\_TIFA\_H\_

Standard include guard.

Definition at line 36 of file tifa.h.

## 5.35 tifa\_factor.h File Reference

TIFA's generic factorization function.

```
#include <gmp.h>
#include "array.h"
#include "factoring_machine.h"
#include "exit_codes.h"
```

**Defines**

- #define [\\_TIFA\\_TIFA\\_FACTOR\\_H\\_](#)

**Functions**

- [ecode\\_t tifa\\_factor](#) ([mpz\\_array\\_t](#) \*const factors, [uint32\\_array\\_t](#) \*const multis, const [mpz\\_t](#) n, const [factoring\\_mode\\_t](#) mode)

*Generic Integer factorization.*

### 5.35.1 Detailed Description

TIFA's generic factorization function.

**Author:**

Jerome Milan

**Date:**

Fri Jun 10 2011

**Version:**

2011-06-10

This is the TIFA library's generic factorization function: it picks the most suitable factoring algorithm depending on the size of the number to factor.

Definition in file [tifa\\_factor.h](#).

### 5.35.2 Define Documentation

#### 5.35.2.1 #define \_TIFA\_TIFA\_FACTOR\_H\_

Standard include guard.

Definition at line 36 of file [tifa\\_factor.h](#).

### 5.35.3 Function Documentation

#### 5.35.3.1 `ecode_t tifa_factor (mpz_array_t *const factors, uint32_array_t *const multis, const mpz_t n, const factoring_mode_t mode)`

Generic Integer factorization.

Attempts to factor the non perfect square integer *n* with the most suitable algorithm (chosen according to the size of *n*) and with the factoring mode given by *mode*. Found factors are then stored in *factors*. Additionally, if the factoring mode used is set to `FIND_COMPLETE_FACTORIZATION`, factors' multiplicities are stored in the array *multis*. For the time being, no trial divisions are performed so depending on the situation, it could be worthwhile to carry out such a step *before* calling `tifa_factor`.

**Note:**

If the factoring mode used is different from `FIND_COMPLETE_FACTORIZATION`, *multis* is allowed to be a `NULL` pointer. Otherwise, using a `NULL` pointer will lead to a fatal error.

**Warning:**

If the *factors* and *multis* arrays have not enough room to store the found factors (and the multiplicities, if any), they will be automatically resized to accommodate the data. This has to be kept in mind when trying to do ingenious stuff with memory management (hint: don't try to be clever here).

**Parameters:**

- *factors* Pointer to the found factors of *n*.
- *multis* Pointer to the multiplicities of the found factors (only computed if *mode* is set to `FIND_COMPLETE_FACTORIZATION`).
- ← *n* The non perfect square integer to factor.
- ← *mode* The factoring mode to use.

**Returns:**

An exit code.

## 5.36 tifa\_internals.h File Reference

Library wide include file (complete with internal structures / functions).

```
#include "tifa_config.h"
#include "cfrac.h"
#include "ecm.h"
#include "fermat.h"
#include "qs.h"
#include "siqs.h"
#include "squfof.h"
#include "tdiv.h"
#include "tifa_factor.h"
#include "first_primes.h"
#include "array.h"
#include "bernsteinisms.h"
#include "bitstring_t.h"
#include "exit_codes.h"
#include "factoring_machine.h"
#include "funcs.h"
#include "gauss_elim.h"
#include "gmp_utils.h"
#include "hashtable.h"
#include "lindep.h"
#include "linked_list.h"
#include "macros.h"
#include "matrix.h"
#include "messages.h"
#include "print_error.h"
#include "res_tdiv.h"
#include "smooth_filter.h"
#include "sqrt_cont_frac.h"
#include "timer.h"
#include "x_array_list.h"
#include "x_tree.h"
```

### Defines

- #define [\\_TIFA\\_TIFA\\_INTERNALS\\_H\\_](#)

### 5.36.1 Detailed Description

Library wide include file (complete with internal structures / functions).

**Author:**

Jerome Milan

**Date:**

Fri Jun 10 2011

**Version:**

2011-06-10

Includes all TIFA's structures and functions.

**Warning:**

Usually, only the [tifa.h](#) include file is needed. [tifa\\_internals.h](#) should only be included to access some internal structures or functions. Be warned that conflicts with client code or external libraries are then more likely to occur.

Definition in file [tifa\\_internals.h](#).

### 5.36.2 Define Documentation

#### 5.36.2.1 #define \_TIFA\_TIFA\_INTERNALS\_H\_

Standard include guard.

Definition at line 41 of file [tifa\\_internals.h](#).

## 5.37 timer.h File Reference

This file defines some macros used to perform timing measurements.

```
#include "stopwatch.h"
```

**Defines**

- #define [\\_TIFA\\_TIMER\\_H\\_](#)
- #define [TIMING\\_FORMAT](#) "%8.3f"
- #define [INIT\\_NAMED\\_TIMER](#)(NAME)
- #define [RESET\\_NAMED\\_TIMER](#)(NAME)
- #define [START\\_NAMED\\_TIMER](#)(NAME)
- #define [STOP\\_NAMED\\_TIMER](#)(NAME)
- #define [GET\\_NAMED\\_TIMING](#)(NAME) `get_stopwatch_elapsed(&__TIFA_STOPWATCH_##NAME)`
- #define [INIT\\_TIMER](#) `INIT_NAMED_TIMER()`
- #define [RESET\\_TIMER](#) `RESET_NAMED_TIMER()`
- #define [START\\_TIMER](#) `START_NAMED_TIMER()`
- #define [STOP\\_TIMER](#) `STOP_NAMED_TIMER()`
- #define [GET\\_TIMING](#) `GET_NAMED_TIMING()`



### 5.37.1 Detailed Description

This file defines some macros used to perform timing measurements.

**Author:**

Jerome Milan

**Date:**

Fri Jun 10 2011

**Version:**

2011-06-10

**Warning:**

The `__TIMING__` symbol should be defined in the file including this header. It is under the responsibility of the including file to check for its definition or to define it, if needed.

If `__TIMING__` is set to 0, then the macros defined in this file do nothing.

Definition in file [timer.h](#).

### 5.37.2 Define Documentation

#### 5.37.2.1 `#define _TIFA_TIMER_H_`

Standard include guard.

Definition at line 40 of file timer.h.

#### 5.37.2.2 `#define GET_NAMED_TIMING(NAME) get_stopwatch_elapsed(&__TIFA_STOPWATCH_ ##NAME)`

Return the timing of the timer named NAME as seconds.

**Warning:**

The returned result is only meaningful if the timer is not running (i.e. it has been stopped via `STOP_NAMED_TIMER`).

Definition at line 118 of file timer.h.

#### 5.37.2.3 `#define GET_TIMING GET_NAMED_TIMING()`

Get timing from an unnamed timer.

Definition at line 149 of file timer.h.

#### 5.37.2.4 `#define INIT_NAMED_TIMER(NAME)`

**Value:**

```
stopwatch_t __TIFA_STOPWATCH_ ##NAME; \
    init_stopwatch(&__TIFA_STOPWATCH_ ##NAME);
```

Initialize a timer named NAME.

**Warning:**

The timer name should not be enclosed in quotes, e.g. `INIT_NAMED_TIMER(my_timer)` is correct, but `INIT_NAMED_TIMER("my_timer")` is wrong and will result in a compilation error.

This warning holds for all of the `*_NAMED_TIMER` macros.

Definition at line 70 of file timer.h.

**5.37.2.5 #define INIT\_TIMER INIT\_NAMED\_TIMER()**

Initialize an unnamed timer.

Definition at line 125 of file timer.h.

**5.37.2.6 #define RESET\_NAMED\_TIMER(NAME)****Value:**

```
do {
    reset_stopwatch(&__TIFA_STOPWATCH_ ##NAME); \
} while (0)
```

Reset the timer named NAME to zero.

Definition at line 78 of file timer.h.

**5.37.2.7 #define RESET\_TIMER RESET\_NAMED\_TIMER()**

Reset an unnamed timer.

Definition at line 131 of file timer.h.

**5.37.2.8 #define START\_NAMED\_TIMER(NAME)****Value:**

```
do {
    start_stopwatch(&__TIFA_STOPWATCH_ ##NAME); \
} while (0)
```

Start the timer named NAME.

**Note:**

Consecutive "calls" to `START_NAMED_TIMER` are without effect.

Definition at line 89 of file timer.h.

**5.37.2.9 #define START\_TIMER START\_NAMED\_TIMER()**

Start an unnamed timer.

Definition at line 137 of file timer.h.

### 5.37.2.10 #define STOP\_NAMED\_TIMER(NAME)

**Value:**

```
do {
    stop_stopwatch(&__TIFA_STOPWATCH_ ##NAME); \
} while (0)
```

Stop the timer named NAME. Successive "calls" to START\_NAMED\_TIMER and STOP\_NAMED\_TIMER are cumulative. In other words, the timer's state holds the time elapsed during all previous time intervals defined by a "call" to START\_NAMED\_TIMER followed by a "call" to STOP\_NAMED\_TIMER (provided that the timer was not reset via RESET\_NAMED\_TIMER).

**Note:**

Consecutive "calls" to STOP\_NAMED\_TIMER are without side effects.

Definition at line 106 of file timer.h.

### 5.37.2.11 #define STOP\_TIMER STOP\_NAMED\_TIMER()

Stop an unnamed timer.

Definition at line 143 of file timer.h.

### 5.37.2.12 #define TIMING\_FORMAT "%8.3f"

Format used to print timing measurements.

Definition at line 57 of file timer.h.

## 5.38 tool\_utils.h File Reference

Miscellaneous helpful functions.

```
#include <inttypes.h>
```

```
#include <stdbool.h>
```

**Defines**

- #define [\\_TIFA\\_TOOL\\_UTILS\\_H](#)

**Functions**

- bool [is\\_a\\_number](#) (const char \*const str\_n, uint32\_t length)  
*Does a string str\_n read as a number?*
- void [chomp](#) (char \*const str\_n, uint32\_t length)  
*NULL terminates a string.*

### 5.38.1 Detailed Description

Miscellaneous helpful functions.

**Author:**

Jerome Milan

**Date:**

Fri Jun 10 2011

**Version:**

2011-06-10

Miscellaneous functions used by the "tool programs".

Definition in file [tool\\_utils.h](#).

### 5.38.2 Define Documentation

#### 5.38.2.1 #define \_TIFA\_TOOL\_UTILS\_H\_

Standard include guard.

Definition at line 35 of file tool\_utils.h.

### 5.38.3 Function Documentation

#### 5.38.3.1 void chomp (char \*const str\_n, uint32\_t length)

NULL terminates a string.

NULL terminates the string `str_n` at the first occurrence of a newline encountered. If no newline is found `str_n` is left unchanged.

**Note:**

This function is actually quite different from the Perl builtin `chomp` function. It's name should probably be changed to avoid possible confusion.

**Parameters:**

- ← *str\_n* The string to NULL terminate.
- ← *length* The maximum length of the string to check.

#### 5.38.3.2 bool is\_a\_number (const char \*const str\_n, uint32\_t length)

Does a string `str_n` read as a number?

Returns `true` if the string `str_n` represents a number in the decimal base, `false` otherwise.

**Parameters:**

- ← *str\_n* The string to check.
- ← *length* The maximum length of the string to check.

## 5.39 x\_array\_list.h File Reference

Higher level lists of arrays and associated functions.

```
#include <inttypes.h>
#include "array.h"
```

### Data Structures

- struct [struct\\_uint32\\_array\\_list\\_t](#)  
*Defines a list of uint32\_array\_t.*
- struct [struct\\_mpz\\_array\\_list\\_t](#)  
*Defines a list of mpz\_array\_t.*

### Defines

- #define [\\_TIFA\\_X\\_ARRAY\\_LIST\\_H\\_](#)

### Typedefs

- typedef struct [struct\\_uint32\\_array\\_list\\_t](#) [uint32\\_array\\_list\\_t](#)  
*Equivalent to struct [struct\\_uint32\\_array\\_list\\_t](#).*
- typedef struct [struct\\_mpz\\_array\\_list\\_t](#) [mpz\\_array\\_list\\_t](#)  
*Equivalent to struct [struct\\_mpz\\_array\\_list\\_t](#).*

### Functions

- [uint32\\_array\\_list\\_t \\* alloc\\_uint32\\_array\\_list](#) ([uint32\\_t](#) allocated)  
*Allocates and returns a new uint32\_array\_list\_t.*
- static void [add\\_entry\\_in\\_uint32\\_array\\_list](#) ([uint32\\_array\\_t](#) \*const entry, [uint32\\_array\\_list\\_t](#) \*const list)  
*Adds an entry to a uint32\_array\_list\_t.*
- void [free\\_uint32\\_array\\_list](#) ([uint32\\_array\\_list\\_t](#) \*const list)  
*Clears a uint32\_array\_list\_t.*
- void [print\\_uint32\\_array\\_list](#) (const [uint32\\_array\\_list\\_t](#) \*const list)  
*Prints a uint32\_array\_list\_t.*
- [mpz\\_array\\_list\\_t \\* alloc\\_mpz\\_array\\_list](#) ([uint32\\_t](#) allocated)  
*Allocates and returns a new mpz\_array\_list\_t.*
- static void [add\\_entry\\_in\\_mpz\\_array\\_list](#) ([mpz\\_array\\_t](#) \*const entry, [mpz\\_array\\_list\\_t](#) \*const list)  
*Adds an entry to a mpz\_array\_list\_t.*

- void `free_mpz_array_list` (`mpz_array_list_t *const list`)  
*Clears a `mpz_array_list_t`.*
- void `print_mpz_array_list` (`const mpz_array_list_t *const list`)  
*Prints a `mpz_array_list_t`.*

### 5.39.1 Detailed Description

Higher level lists of arrays and associated functions.

**Author:**

Jerome Milan

**Date:**

Fri Jun 10 2011

**Version:**

2011-06-10

Defines higher level lists of arrays and their associated functions. This terminology is actually a bit confusing since they are actually more arrays of arrays rather than lists strictly speaking.

Definition in file [x\\_array\\_list.h](#).

### 5.39.2 Define Documentation

#### 5.39.2.1 `#define _TIFA_X_ARRAY_LIST_H`

Standard include guard.

Definition at line 37 of file `x_array_list.h`.

### 5.39.3 Function Documentation

#### 5.39.3.1 `static void add_entry_in_mpz_array_list` (`mpz_array_t *const entry`, `mpz_array_list_t *const list`) [`inline`, `static`]

Adds an entry to a `mpz_array_list_t`.

Adds the `entry` pointer to `list` and increments its `length` field.

**Warning:**

This function transfers the ownership of the `mpz_array_t` pointed to by `entry` to `list`. This means that any client code *should not* clear any `mpz_array_t` that has been added to a `mpz_array_list_t` since this is the exclusive responsibility of the `mpz_array_list_t`.

**Parameters:**

← `entry` A pointer to the `mpz_array_t` to add in the list.

← *list* A pointer to the `mpz_array_list_t`.

**Returns:**

A pointer to the newly allocated `mpz_array_list_t` structure.

Definition at line 225 of file `x_array_list.h`.

References `struct_mpz_array_list_t::data`, and `struct_mpz_array_list_t::length`.

**5.39.3.2 static void add\_entry\_in\_uint32\_array\_list (uint32\_array\_t \*const entry, uint32\_array\_list\_t \*const list) [inline, static]**

Adds an entry to a `uint32_array_list_t`.

Adds the `entry` pointer to `list` and increments its `length` field.

**Warning:**

This function transfers the ownership of the `uint32_array_t` pointed to by `entry` to `list`. This means that any client code *should not* clear any `uint32_array_t` that has been added to a `uint32_array_list_t` since this is the exclusive responsibility of the `uint32_array_list_t`.

**Parameters:**

← *entry* A pointer to the array to add.

← *list* A pointer to the `uint32_array_list_t`.

**Returns:**

A pointer to the newly allocated `uint32_array_list_t` structure.

Definition at line 117 of file `x_array_list.h`.

References `struct_uint32_array_list_t::allocated`, `struct_uint32_array_list_t::data`, and `struct_uint32_array_list_t::length`.

**5.39.3.3 mpz\_array\_list\_t\* alloc\_mpz\_array\_list (uint32\_t allocated)**

Allocates and returns a new `mpz_array_list_t`.

Allocates and returns a new `mpz_array_list_t` such that:

- its `allocated` field is set to the parameter `allocated`.
- its `length` field set to zero.
- its `data` array is left *uninitialized*.

**Parameters:**

← *allocated* The allocated length of the `mpz_array_list_t` to allocate.

**Returns:**

A pointer to the newly allocated `mpz_array_list_t` structure.

#### 5.39.3.4 uint32\_array\_list\_t\* alloc\_uint32\_array\_list (uint32\_t *allocated*)

Allocates and returns a new `uint32_array_list_t`.

Allocates and returns a new `uint32_array_list_t` such that:

- its `allocated` field is set to the parameter `allocated`.
- its `length` field set to zero.
- its `data` array is left *uninitialized*.

##### Parameters:

← *allocated* The allocated length of the `uint32_array_list_t` to allocate.

##### Returns:

A pointer to the newly allocated `uint32_array_list_t` structure.

#### 5.39.3.5 void free\_mpz\_array\_list (mpz\_array\_list\_t \*const *list*)

Clears a `mpz_array_list_t`.

Clears a `mpz_array_list_t`, or, more precisely, clears the memory space used by the array pointed by the `data` field of a `mpz_array_list_t`. Also set its `allocated` and `length` fields to zero.

##### Parameters:

← *list* A pointer to the `mpz_array_list_t` to clear.

#### 5.39.3.6 void free\_uint32\_array\_list (uint32\_array\_list\_t \*const *list*)

Clears a `uint32_array_list_t`.

Clears a `uint32_array_list_t`, or, more precisely, clears the memory space used by the array pointed by the `data` field of a `uint32_array_list_t`. Also set its `allocated` and `length` fields to zero.

##### Parameters:

← *list* A pointer to the `uint32_array_list_t` to clear.

#### 5.39.3.7 void print\_mpz\_array\_list (const mpz\_array\_list\_t \*const *list*)

Prints a `mpz_array_list_t`.

Prints a `mpz_array_list_t` on the standard output.

##### Note:

This function is mostly intended for debugging purposes as the output is not particularly well structured

##### Parameters:

← *list* A pointer to the `mpz_array_list_t` to print.



**5.39.3.8 void print\_uint32\_array\_list (const uint32\_array\_list\_t \*const list)**

Prints a `uint32_array_list_t`.

Prints a `uint32_array_list_t` on the standard output.

**Note:**

This function is mostly intended for debugging purposes as the output is not particularly well structured

**Parameters:**

← *list* A pointer to the `uint32_array_list_t` to print.

**5.40 x\_tree.h File Reference**

Product and remainder trees.

```
#include <gmp.h>
```

```
#include "array.h"
```

**Defines**

- `#define TIFA_X_TREE_H`

**Typedefs**

- `typedef mpz_array_t mpz_tree_t`  
*Equivalent to `mpz_array_t`.*

**Functions**

- `mpz_tree_t * prod_tree (const mpz_array_t *const array)`  
*Computes the product tree of some `mpz_t` integers.*
- `mpz_tree_t * prod_tree_mod (const mpz_array_t *const array, const mpz_t n)`  
*Computes the product tree of some `mpz_t` integers modulo a positive integer.*
- `mpz_tree_t * prod_tree_ui (const uint32_array_t *const array)`  
*Computes the product tree of some `uint32_t` integers.*
- `mpz_tree_t * rem_tree (const mpz_t z, const mpz_tree_t *const ptree)`  
*Computes a remainder tree.*
- `void free_mpz_tree (mpz_tree_t *tree)`  
*Clears a tree of `mpz_t` integers.*
- `void print_mpz_tree (const mpz_tree_t *const tree)`  
*Prints a tree of `mpz_t` integers.*

### 5.40.1 Detailed Description

Product and remainder trees.

**Author:**

Jerome Milan

**Date:**

Fri Jun 10 2011

**Version:**

2011-06-10

Implementation of the product and remainder trees used in D. J. Bernstein's algorithms.

Definition in file [x\\_tree.h](#).

### 5.40.2 Define Documentation

#### 5.40.2.1 `#define _TIFA_X_TREE_H_`

Standard include guard.

Definition at line 36 of file `x_tree.h`.

### 5.40.3 Typedef Documentation

#### 5.40.3.1 `mpz_tree_t`

Equivalent to `mpz_array_t`.

While an `mpz_tree_t` is just an `mpz_array_t`, its memory is allocated in a different manner than in the `mpz_array_t` case. Indeed, the elements of an `mpz_tree_t` array should NOT be modified later on since the memory used is allocated in one huge block to prevent overhead from multiple `malloc` calls. So the allocated memory of the `mpz_t`'s in the tree can NOT be increased.

The `mpz_tree_t` typedef is introduced only as a reminder of this different underlying memory allocation. `free_mpz_tree` should be used to clear the memory space occupied by an `mpz_tree_t`. Do NOT call `free_mpz_array` on an `mpz_tree_t`!

Definition at line 61 of file `x_tree.h`.

### 5.40.4 Function Documentation

#### 5.40.4.1 `void free_mpz_tree (mpz_tree_t * tree)`

Clears a tree of `mpz_t` integers.

Clears a tree of `mpz_t` integers returned by `prod_tree`, `prod_tree_ui` or `rem_tree`.

**Note:**

This function is actually different from `free_mpz_array`. Indeed, even if the `mpz_tree_t` type is merely a typedef of `mpz_array_t`, the memory used by the `mpz_t` elements is allocated in a completely different manner, hence the need for a different function.

**Parameters:**

← *tree* Pointer to the `mpz_tree_t` to clear.

**5.40.4.2 void print\_mpz\_tree (const mpz\_tree\_t \*const tree)**

Prints a tree of `mpz_t` integers.

Prints a tree of `mpz_t` integers on the standard output. Useful only for debugging purposes and for relatively small trees.

**Parameters:**

← *tree* Pointer to the `mpz_array_t` containing the tree to print.

**5.40.4.3 mpz\_tree\_t\* prod\_tree (const mpz\_array\_t \*const array)**

Computes the product tree of some `mpz_t` integers.

Computes the product tree of the `mpz_t` integers given by *array* and returns it as a newly allocated `mpz_tree_t`.

**Note:**

The product tree is implemented as a single `mpz_array_t` *tree* with the usual compact representation: `tree->data[2i+1]` and `tree->data[2i+2]` are the children of the node `tree->data[i]`.

Hence, in order to avoid useless nodes (i.e. nodes with value 1), it is recommended to have `array->length` equals to a power of 2. If this is not the case, the product tree will be computed as if *array* was completed by as many useless nodes as necessary until a power of 2 is reached.

This choice was made to keep a space efficient representation and to avoid dynamic allocations of nodes.

**Warning:**

Although the product tree returned is actually a pointer to an `mpz_tree_t` structure (i.e. an `mpz_array_t`), the elements of the array should NOT be modified later on since the memory used is allocated in one huge block to prevent overhead from multiple `malloc` calls. So the allocated memory of the `mpz_t`'s in the array can NOT be increased...

**Parameters:**

← *array* Pointer to the `mpz_array_t` containing the `mpz_t` integers to multiply.

**Returns:**

A pointer to a newly allocated `mpz_tree_t` holding the computed product tree.

**5.40.4.4 mpz\_tree\_t\* prod\_tree\_mod (const mpz\_array\_t \*const array, const mpz\_t n)**

Computes the product tree of some `mpz_t` integers modulo a positive integer.

Similar to `prod_tree` but each node is reduced mod *n*.

**Warning:**

*n* should be strictly positive or results will be unpredictable.

**See also:**

The function `prod_tree(const mpz_array_t* const array)`.

**Parameters:**

- ← *array* Pointer to the `mpz_array_t` containing the `mpz_t` integers to multiply.
- ← *n* The positive modulo.

**Returns:**

A pointer to a newly allocated `mpz_tree_t` holding the computed product tree.

**5.40.4.5 `mpz_tree_t* prod_tree_ui(const uint32_array_t *const array)`**

Computes the product tree of some `uint32_t` integers.

Computes the product tree of the `uint32_t` integers given by `array` and returns it as a newly allocated `mpz_tree_t`.

**Note:**

The product tree is implemented as a single `mpz_array_t` `tree` with the usual compact representation: `tree->data[2i+1]` and `tree->data[2i+2]` are the children of the node `tree->data[i]`.

Hence, in order to avoid useless nodes (i.e nodes with value 1), it is recommended to have `array->length` equals to a power of 2. If this is not the case, the product tree will be computed as if `array` was completed by as many useless nodes as necessary until a power of 2 is reached.

This choice was made to keep a space efficient representation and to avoid dynamic allocations of nodes.

**Warning:**

Although the product tree returned is actually a pointer to an `mpz_tree_t` structure (i.e. an `mpz_array_t`), the elements of the array should NOT be modified later on since the memory used is allocated in one huge block to prevent overhead from multiple `malloc` calls. So the allocated memory of the `mpz_t`'s in the array can NOT be increased...

**Parameters:**

- ← *array* Pointer to the `uint32_array_t` containing the `mpz_t` integers to multiply.

**Returns:**

A pointer to a newly allocated `mpz_tree_t` holding the computed product tree.

**5.40.4.6 `mpz_tree_t* rem_tree(const mpz_t z, const mpz_tree_t *const ptree)`**

Computes a remainder tree.

Computes the remainder tree of `z` by the `mpz_t` integers whose product tree is given by `ptree` and returns it as a newly allocated `mpz_tree_t`. If `rtree` is the returned remainder tree, then one has: `rtree->data[i] = z mod ptree->data[i]`.

**Note:**

The remainder tree is implemented as a single `mpz_array_t` `tree` with the usual compact representation: `tree->data[2i+1]` and `tree->data[2i+2]` are the children of the node `tree->data[i]`.

**Warning:**

Although the remainder tree returned is actually a pointer to an `mpz_tree_t` structure (i.e. an `mpz_array_t`), the elements of the array should NOT be modified later on since the memory used is allocated in one huge block to prevent overhead from multiple `malloc` calls. So the allocated memory of the `mpz_t`'s in the array can NOT be increased...

**Parameters:**

- ← `z` The integer to divide.
- ← ***ptree*** Pointer to the `mpz_tree_t` containing the product tree of the `mpz_t` integers to divide `z` by.

**Returns:**

A pointer to a newly allocated `mpz_tree_t` holding the computed remainder tree.

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