

Supervisory Control for Modal Specifications of Services

Philippe Darondeau — Jérémy Dubreil — Hervé Marchand

N° 7247

April 2010

Thème COM



*Rapport
de recherche*

Supervisory Control for Modal Specifications of Services

Philippe Darondeau , Jérémy Dubreil , Hervé Marchand

Thème COM — Systèmes communicants
Équipes-Projets S4, Comète and VerTeCs

Rapport de recherche n° 7247 — April 2010 — 14 pages

Abstract: In the service oriented architecture framework, a modal specification, as defined by Larsen in [6], formalises how a service should interact with its environment. More precisely, a modal specification determines the events that the server may or must allow at each stage in an interactive session. Therefore, techniques to enforce a modal specification on a system would be useful for practical applications. In this paper, we investigate the adaptation of the supervisory control theory of Ramadge and Wonham to enforce a modal specification (with final states marking the ends of the sessions) on a system modelled by a finite LTS. We prove that there exists at most one most permissive solution to this control problem. We also prove that this solution is regular and we present an algorithm for the effective computation of the corresponding controller.

Key-words: discrete event systems, supervisory control, modal specifications, services, partial observation.

Synthèse de contrôleurs pour des services décrits par des spécifications modales

Résumé : Dans le cadre d'une architecture orientée services, une spécification modale décrit les interactions possibles ou nécessaires entre un service et l'environnement utilisateur de ce service. Plus précisément, une spécification modale détermine les actions que le serveur peut ou doit permettre à son utilisateur à chaque étape d'une session interactive. Développer des techniques de supervision permettant de forcer la conformité d'un système à une spécification de service s'avère utile. Dans cet article, nous cherchons à adapter les techniques de synthèse de contrôleurs afin de forcer la conformité de systèmes finis à des spécifications modales (avec des états marquant les fins de sessions). Nous montrons que ce problème de contrôle a une plus grande solution. Nous montrons également que cette solution est régulière et donnons un algorithme pour la calculer.

Mots-clés : systèmes à événements discrets, théorie du contrôle, spécifications modales, services, observation partielle.

1 Introduction

In [11, 12, 13], Ramadge and Wonham laid the foundations of the theory of supervisory control for discrete event systems and proposed solutions to the Basic Supervisory Control Problem, or BSCP, that may be stated as follows. Let G be a finite automaton, with a subset of final (or marked) states, over a set of events Σ with two independent partitions $\Sigma = \Sigma_c \cup \Sigma_{uc}$ and $\Sigma = \Sigma_o \cup \Sigma_{uo}$. The automaton G represents a plant. The plant's events in Σ_o and Σ_c may be observed and controlled, respectively, from the environment of the plant. Let L_{max} be a regular language over Σ . BSCP is the problem whether there exists some proper controller C such that the language $\mathcal{L}(C/G)$ of the controlled system satisfies the relation $\mathcal{L}(C/G) \subseteq L_{max}$. The plant and the controller produce joint runs, in which the controller acts by disabling at each step a subset of events of the plant. The set of disabled events must be a function of the subsequence of events currently observed. A proper controller should be admissible (it never disables uncontrollable events) and non-blocking (it always leaves a possibility to reach some final state of the plant). Ramadge and Wonham's theory characterizes the existence of proper controllers and proposes algorithms for computing the maximally permissive controller C under the assumption $\Sigma_c \subseteq \Sigma_o$.

Ramadge and Wonham's theory aims chiefly at enforcing *safety* properties on autonomous or semi-autonomous systems, e.g. automated manufacturing systems, but it takes special care of the property of nonblocking (w.r.t. final states), which is a particular form of progress or liveness. An extension of the supervisory control theory taking *liveness* properties into full account was proposed in [17]. Two other types of general properties often expected from systems are *security* and *conformance to specified service*. Several works, e.g. [14, 2, 3, 15, 16] recently addressed the problem of adapting supervisory control in order to enforce *opacity*, a formal notion that covers a variety of more specific security properties [1]. Our goal in this paper is to adapt the theory and algorithms of supervisory control for enforcing on a plant G the conformance to the modal specifications of a service.

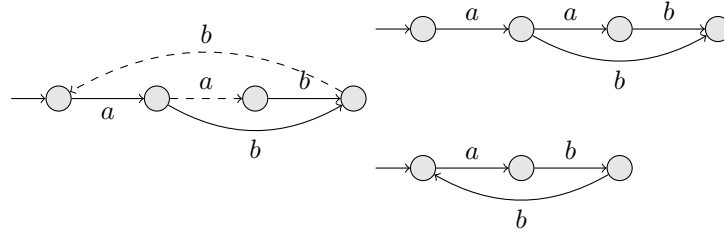
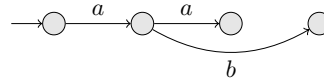
We assume that the plant is described by a finite automaton G over Σ , with a set of final states Q_F , and the service expected from the plant is specified by a modal automaton \mathcal{S} over Σ_o , with a set of final states S_F . We assume moreover that $\Sigma_c \subseteq \Sigma_o$. We want to compute a proper and maximally permissive controller C under which the controlled system C/G conforms to \mathcal{S} , i.e., it provides the specified service. This means in particular that under the considered control C , both sets of final states Q_F and S_F stay forever jointly reachable so that any interactive session can terminate.

Modal specifications, also called modal transition systems, were introduced in [6] in the form of transition systems $(S, \Sigma, \rightarrow_{\square}, \rightarrow_{\diamond}, s_0)$, with two modal transition relations: the *must* transitions denoted \rightarrow_{\square} and the *may* transitions denoted \rightarrow_{\diamond} , such that $\rightarrow_{\square} \subseteq \rightarrow_{\diamond}$. Every modal transition system MTS determines a corresponding family \mathcal{M} of labelled transition system (LTS) which are called the models of MTS . Intuitively, an LTS is a model of MTS if there exists a relation \models between their respective sets of states S and Q such that \models holds between the initial states and whenever $s \models q$, all *must* transitions from s are simulated by transitions from q , all transitions from q are simulated by *may* transitions from s and \models is preserved under simulation of transitions in both directions. We denote $G \models MTS$ the fact that G is an LTS that is a model of MTS .

Example 1 *The modal specification depicted in Figure 1, where the relations \rightarrow_{\square} and \rightarrow_{\diamond} are represented with plain arrows and dashed arrows respectively, expresses the fact that the presence of the first transition a is mandatory while the second one is not, and that after any a the system must be able to trigger a b . Finally, the presence of a transition b returning to the initial state is optional.*

The two LTSs on the right hand side of Figure 1 are models of the specification, whereas the one depicted in Figure 2 is not. Indeed, after the sequence aa , the specification imposes a transition labelled by b which is not present in this LTS. \diamond

It is worthwhile noticing that a language generated by an LTS G which is a model of a specification MTS belongs to a language interval $[L_{min}, L_{max}]$ whose endpoints L_{min} and L_{max} are the languages of the labelled transition systems $(S, \Sigma, \rightarrow_{\square}, s_0)$ and $(S, \Sigma, \rightarrow_{\diamond}, s_0)$, respectively. However, not all the languages in the interval $[L_{min}, L_{max}]$ are languages generated by models of MTS . Consider for instance

Figure 1: A modal specification *MTS* and some associated modelsFigure 2: A labelled transition system that is not a model of *MTS*

the modal transition system *MTS* depicted in Fig. 1. then $L_{min} = \{\epsilon, a, ab\}$ and L_{max} is the prefix-closure of $(a(ab + b)b)^*$. However, for $L = \{\epsilon, a, ab, aa\}$, there exists no LTS G generating L such that $G \models MTS$.

The expressive power of modal specifications added over language specifications comes precisely from the possibility they offer to formulate service requirements in a conditional way, e.g. *if the system serves an a request, then the next b request will be served*. This feature makes modal specifications very convenient for describing the interface between a partially observed plant (service provider) and its environment (service requester). For instance, after a coin has been inserted into a coffee machine, the client should always get a cup of coffee or the coin back but there is no guarantee that coins can always be entered, which depends on unobservable phenomena inside the machine.

In [6], determinism was required neither from the labelled transition relations \rightarrow_{\square} and \rightarrow_{\diamond} of modal transition systems, nor from the labelled transition relations \rightarrow of their transition system models. In this paper, for simplicity, we shall limit ourselves to deterministic transition systems and to deterministic modal transition systems.

However, we shall extend modal transition systems in another respect since we will introduce a satisfaction relation \models between LTS's over Σ (modelling the plant) and MTS's over $\Sigma_o \subseteq \Sigma$ (specifying the expected service as observed from the environment of the plant). The proposed extension is based on the assumption that the plant interacts fairly with its environment, i.e. it does not refuse possible interactions forever. Consequently, infinite unobservable behaviours are considered impossible.

We shall also extend modal transition systems in a second direction by providing them with marked or final states, thus obtaining modal automata. In modal specifications of services, final states serve to represent the potential points of termination of a session from the service requester's perspective. In a similar way, we replace labelled transition systems with automata for modelling plants, where final states represent the potential points of termination of a session from the service provider's perspective. We end up thus with final states in G (the plant) and S (the specification), whose joint reachability is to be taken care of in the search for non-blocking controllers C such that $C/G \models MTS$. There, G is an automaton over Σ , S is a modal specification over $\Sigma_o \subseteq \Sigma$, and C is a labelled transition system over Σ_o that includes Σ_c (the set of controllable events).

An earlier adaptation of the theory of supervisory control to modal specifications was proposed in [4]. In that work, *total observation* was assumed and *nonblocking* was not considered. The contribution of the present paper is to lift these two limitations. The working assumptions of [4] are retrieved in the particular case where $\Sigma = \Sigma_o$ and all states of the plant automaton and the modal specification are final states.

The remaining sections of the paper are organized as follows. We recall in Section 2 some basic concepts and notations concerning automata, supervisory control and modal specifications of services. In Section 3, we investigate the supervisory control problem for modal specifications. We show that when there exists a solution to this problem, there exists a unique supremal controller enforcing the given modal specification and we show in a non-constructive way that this optimal supervisor is finite state. We present in Section 4.5 an algorithm to compute this supervisor. When there is no solution to the control problem, the algorithm produces an empty supervisor.

2 Background

We recall in this section basic definitions and results about transition systems and supervisory control.

2.1 Transition Systems and Automata

A deterministic *labelled transition system* (or LTS) over Σ is a 4-tuple $LTS = (Q, \Sigma, \delta, q_0)$ where Q is a finite set of states, $q_0 \in Q$ is an *initial state*, and δ is a partial map from $Q \times \Sigma$ to Q , called the *labelled transition map*. This map is extended inductively to $\delta : Q \times \Sigma^* \rightarrow Q$ by setting $\delta(q, \varepsilon) = q$ (where ε is the empty word), and $\delta(q, wa) = \delta(\delta(q, w), a)$ for all $q \in Q$, $w \in \Sigma^*$ and $a \in \Sigma$. A state $q \in Q$ is *reachable* (from q_0) if $\delta(q_0, w) = q$ for some word $w \in \Sigma^*$. An LTS is *finite* if Q and Σ are finite; it is *reduced* if all states in Q are reachable and every event $a \in \Sigma$ is enabled at some state q , i.e. $\delta(q, a)$ is defined for the considered state q . In the sequel, we always consider reduced transition systems unless explicitly stated otherwise. The *language* of LTS is the set of words $\mathcal{L}(LTS) = \{w \in \Sigma^* \mid \delta(q_0, w) \text{ defined}\}$.

Given labelled transition systems $LTS = (Q, \Sigma, \delta, q_0)$ and $LTS' = (Q', \Sigma', \delta', q'_0)$, their *product* is the (reachable restriction of the) labelled transition system $LTS \times LTS' = (Q \times Q', \Sigma \cup \Sigma', \delta \times \delta', (q_0, q'_0))$ where $(\delta \times \delta')((q, q'), a)$ is defined as $(\delta(q, a), q')$ for $a \in \Sigma \setminus \Sigma'$, $(q, \delta'(q', a))$ for $a \in \Sigma' \setminus \Sigma$, and $(\delta(q, a), \delta'(q', a))$ for $a \in \Sigma \cap \Sigma'$.

A deterministic *automaton* over Σ is a labelled transition system with final states, i.e. $A = (Q, \Sigma, \delta, q_0, Q_F)$ with $Q_F \subseteq Q$. The *labelled transition system underlying* A is $\mathcal{U}(A) = (Q, \Sigma, \delta, q_0)$. The *language* of the automaton A is $\mathcal{L}(A) = \{w \in \Sigma^* \mid \delta(q_0, w) \in Q_F\}$. Thus, $\mathcal{L}(A) \subseteq \mathcal{L}(\mathcal{U}(A)) \subseteq \Sigma^*$. In the sequel, we sometimes consider also (for technical convenience) automata $A = (Q, \Sigma, \delta, Q_0, Q_F)$ with a set Q_0 of final states.

Given a language $L \subseteq \Sigma^*$, its *prefix-closure* is $\bar{L} = \{u \in \Sigma^* \mid \exists v \in \Sigma^* : uv \in L\}$. A language L is *prefix-closed* if $L = \bar{L}$. A prefix-closed language L induces a (possibly infinite) transition system $\mathcal{LTS}(L) = (L, \Sigma, \delta, \varepsilon)$ where $\delta(u, a) = ua$ for every word $ua \in L$ with $a \in \Sigma$.

2.2 Supervisory Control

The presentation given here has been adapted from [3]. Let $\Sigma_o \subseteq \Sigma$ and $\Sigma_c \subseteq \Sigma$ be the sets of *observable* and *controllable* events, respectively.

A *run* of a *plant* automaton $G = (Q, \Sigma, \delta, q_0, Q_F)$ is a sequence $\rho = q_0, a_1, q_1, a_2, \dots, q_{n-1}, a_{n-1}, q_n$ such that $n \geq 0$ and $\delta(q_{i-1}, a_{i-1}) = q_i$ for all $i \leq n$. The run is *accepted* if $q_n \in Q_F$. The *trace* of the run is the (possibly empty) word $a_1 a_2 \dots a_{n-1}$. The *observable trace* of the run (w.r.t. Σ_o) is the *natural projection* of $a_1 a_2 \dots a_{n-1}$ on Σ_o^* , defined inductively with $\pi_o(\varepsilon) = \varepsilon$ and

- $\pi_o(a_1 a_2 \dots a_i) = \pi_o(a_1 a_2 \dots a_{i-1}) a_i$ if $a_i \in \Sigma_o$,
- $\pi_o(a_1 a_2 \dots a_i) = \pi_o(a_1 a_2 \dots a_{i-1})$ otherwise.

An *admissible control* w.r.t. $\Sigma_c \subseteq \Sigma$ is a map $f : \Sigma_o^* \rightarrow 2^\Sigma$ such that all values taken by this map are supersets of $\Sigma \setminus \Sigma_c$. Applying the control f to G means disabling after a trace w all events which do not belong to $f(\pi_o(w))$. The induced restrictions of $\mathcal{L}(G)$ and $\mathcal{L}(\mathcal{U}(G))$ under the control f are denoted $\mathcal{L}(f/G)$ and $\mathcal{L}(f/\mathcal{U}(G))$, respectively. The control f is *non-blocking* if $\mathcal{L}(f/\mathcal{U}(G))$ is equal to

the prefix-closure of $\mathcal{L}(f/G)$, i.e. every run of G under the control f can be extended to an accepted run compatibly with f . An admissible and non-blocking control is said to be a proper control.

Given a control f , let C be any (possibly infinite) LTS such that the language of C is equal to $\mathcal{L}(f/\mathcal{LTS}(\Sigma^*))$. Then $\mathcal{L}(f/\mathcal{U}(G)) = \mathcal{L}(\mathcal{U}(G) \times C)$ and $\mathcal{L}(f/G) = \mathcal{L}(G \times C)$ where the final states of $G \times C$ are all pairs (q, s) with q final in G . Moreover, if one considers exclusively the *maximal* control maps f such that $\mathcal{L}(f/G) = \mathcal{L}(G \times C)$, where $f \leq f'$ if $f(\omega) \subseteq f'(\omega)$ for all $\omega \in \Sigma_o^*$, then f and C determine each other up to the above equality relation. For this reason, C is called a *controller*, and $G \times C$ and $\mathcal{U}(G) \times C$ are rewritten C/G and $C/\mathcal{U}(G)$ to stress this view.

In order to characterize the behaviours that may be enforced on a given plant by supervisory control, Ramadge and Wonham introduced two central concepts.

Definition 1 A prefix-closed language $K \subseteq \mathcal{L}(\mathcal{U}(G))$ is controllable w.r.t. Σ_c if $K \cdot (\Sigma \setminus \Sigma_c) \cap \mathcal{L}(\mathcal{U}(G)) \subseteq K$.

Definition 2 A prefix-closed language $K \subseteq \mathcal{L}(\mathcal{U}(G))$ is observable w.r.t. Σ_o and Σ_c if, for any $w, w' \in K$ with identical observations $\pi_o(w) = \pi_o(w')$ and for any controllable event $a \in \Sigma_c$, $(wa \in \mathcal{L}(\mathcal{U}(G)) \wedge w'a \in K) \Rightarrow wa \in K$.

A classical Ramadge and Wonham's theorem states that, given a prefix-closed sublanguage $K \subseteq \mathcal{L}(\mathcal{U}(G))$, $K = \mathcal{L}(f/\mathcal{U}(G))$ for some control f if and only if K is controllable and observable. Similarly, if K is a sublanguage of $\mathcal{L}(G)$, then $K = \mathcal{L}(f/G)$ for some non-blocking control f if and only if $K = \overline{K} \cap \mathcal{L}(G)$ and \overline{K} is controllable and observable.

In the particular case where every controllable event is observable, i.e. $\Sigma_c \subseteq \Sigma_o$, a prefix-closed language $K \subseteq \mathcal{L}(\mathcal{U}(G))$ is observable if and only if it is *normal* according to the following definition.

Definition 3 A prefix-closed language $K \subseteq \mathcal{L}(\mathcal{U}(G))$ is normal w.r.t. Σ_o if $\pi_o^{-1} \circ \pi_o(K) \cap \mathcal{L}(\mathcal{U}(G)) \subseteq K$.

Prefix-closedness, controllability and normality are preserved under arbitrary unions of languages. Therefore, if K is a prefix-closed sublanguage of $\mathcal{L}(\mathcal{U}(G))$, then there exists a supremal prefix-closed, controllable and normal sublanguage K^\dagger of K . Similarly, if K is a sublanguage of $\mathcal{L}(G)$, then there exists a supremal sublanguage K^\dagger of K such that $\overline{K^\dagger}$ is controllable and normal. In both situations, Ramadge and Wonham have shown that the induced control f^\dagger such that $K^\dagger = \mathcal{L}(f^\dagger/\mathcal{U}(G))$ or $K^\dagger = \mathcal{L}(f^\dagger/G)$ is regular, i.e. $K^\dagger = \mathcal{L}(C/\mathcal{U}(G))$ or $K^\dagger = \mathcal{L}(C/G)$ for some finite state controller C , and they have given algorithms for computing C . In the particular case where $\Sigma_c \subseteq \Sigma_o$, such a controller is said to be maximally permissive because $\mathcal{L}(C'/G) \subseteq \mathcal{L}(C/G)$ for any other proper controller C' such that $\mathcal{L}(C'/G) \subseteq K$. Moreover in that case, one may assume w.l.o.g. that $\delta(r, a) = r$ in $C = (R, \Sigma, \delta, r_0)$ for all $r \in R$ and for all $a \in (\Sigma \setminus \Sigma_o)$, hence one may as well consider C as an LTS over Σ_o . This is the kind of supervisors we shall consider in the sequel. Note that when $\Sigma_c \subseteq \Sigma_o$, if a supervisor C is given as an LTS over Σ_o , then $\mathcal{L}(C/G)$ is normal by construction with respect to Σ_o and $\mathcal{L}(G)$ and thus it is observable.

2.3 Modal Specifications of Services

In this section, we propose to specify services using an extended form of Larsen's modal specifications [6]. The extension is twofold. On the one hand, service specifications express requirements about the behaviour of the service seen from the environment (service requester), hence they may abstract from some unobservable events of the service provider. Given modal specifications over a set of observable events Σ_o , we shall therefore consider as an associated class of models a family of LTS's over a larger alphabet of events $\Sigma \supseteq \Sigma_o$ (drawing some inspiration from Hüttel and Larsen's *observable refinements* which were introduced for a similar but different purpose in [7]). On the other hand, we shall provide modal specifications with final states, and similarly for their LTS models (service providers), so that the ability to terminate interactive sessions can be taken into account as a main requirement in the definition of the satisfaction relation.

In the sequel, Σ and Σ_o are two fixed finite sets of events, with $\Sigma_o \subseteq \Sigma$, and we let $\Sigma_{uo} = \Sigma \setminus \Sigma_o$. Given an automaton $A = (Q, \Sigma, \delta, q_0, Q_F)$, we say that a subset of states $P \subseteq Q$ is *closed under unobservable transitions* if $\delta(P, \Sigma_{uo}^*) \subseteq P$.

Definition 4 A *deterministic modal transition system* (or *MTS*) is a 5-tuple $MTS = (S, \Sigma_o, \delta^\square, \delta^\diamond, s_0)$ where $\delta^\square : S \times \Sigma_o \rightarrow S$ and $\delta^\diamond : S \times \Sigma_o \rightarrow S$ are two partial maps, called the *strong and weak labelled transition maps*, respectively, subject to the constraint that δ^\square is a restriction of δ^\diamond . A *deterministic modal automaton or modal specification over Σ_o* is a modal transition system with final states, i.e. $\mathcal{S} = (S, \Sigma_o, \delta^\square, \delta^\diamond, s_0, S_F)$ with $S_F \subseteq S$. The plain transition system underlying \mathcal{S} is $\mathcal{U}(\mathcal{S}) = (S, \Sigma_o, \delta^\diamond, s_0)$.

We use $s \xrightarrow{\square} s'$ and $s \xrightarrow{\diamond} s'$ as abbreviations respectively for $\delta^\square(s, a) = s'$ and $\delta^\diamond(s, a) = s'$. This notation is extended inductively from letters $a \in \Sigma_o$ to words $\omega \in \Sigma_o^*$.

Definition 5 An automaton $A = (Q, \Sigma, \delta, q_0, Q_F)$ satisfies a modal specification $\mathcal{S} = (S, \Sigma_o, \delta^\square, \delta^\diamond, s_0, S_F)$ (noted $A \models \mathcal{S}$) if $Q_0 \models s_0$ where $Q_0 = \delta(q_0, \Sigma_{uo}^*)$ and \models is the largest relation between subsets of states P closed under unobservable transitions and states of \mathcal{S} such that $P \models s$ entails the following properties for all $a \in \Sigma_o$ and $q \in P$:

1. $\delta(q, a)$ defined $\Rightarrow s \xrightarrow{\diamond} s'$ and $P' \models s'$ for $P' = \delta(P, a\Sigma_{uo}^*)$,
2. $s \xrightarrow{\square} s' \Rightarrow \delta(q, \Sigma_{uo}^* a) \neq \emptyset$,
3. $Q_F \times S_F$ can be reached from (q, s) in $A \times \mathcal{U}(\mathcal{S})$.

According to the above definition, A satisfies \mathcal{S} if the fair abstraction of A w.r.t. the unobservable transitions satisfies \mathcal{S} with the definition given in [6] and moreover, any interactive session in which A is used as specified in \mathcal{S} can be completed (the service provider and the service requester can always reach final states jointly). An illustration of the use of modal automata for specifying services is proposed below.

Example 2 Consider the modal specification \mathcal{S} depicted in Figure 3. \mathcal{S} defines the service offered by a (special) coffee-machine¹. The initial state is s_0 . The final states are s_0 and s_5 . Initially, the user must

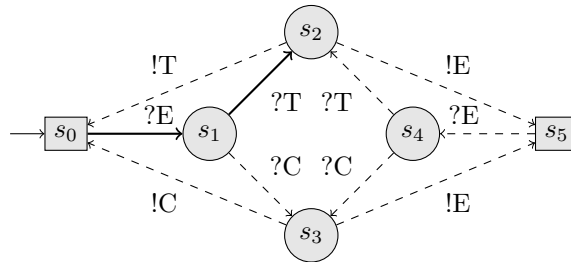
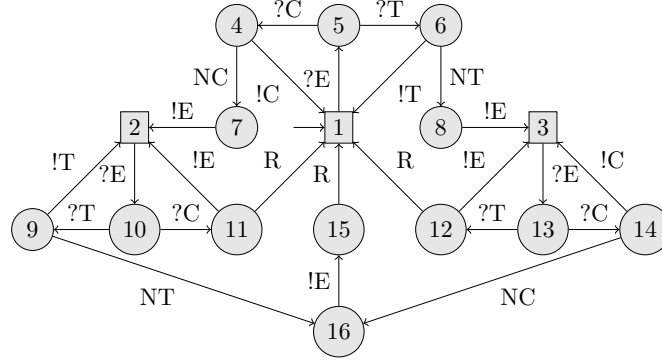


Figure 3: Specification \mathcal{S} of a coffee-machine

be enabled to insert a coin ($?E$) in the machine and further to order a tea ($?T$). He may also have the possibility to order a coffee ($?C$), but this is optional. Afterwards, the machine may deliver the requested beverage ($!C$ or $!T$) or return the coin ($!E$) and the service may then end (in state s_0 or s_5). If the coin is returned, there is no guarantee that the user can insert a new coin and order a coffee or a tea (all these transitions are optional). However, if the user succeeds to have his beverage, then he must be enabled to insert a new coin and order a tea.

The automaton A of Figure 4 represents a possible coffee-machine plant, where $\Sigma_{uo} = \{NC, NT, R\}$ (NC (resp. NT) means no coffee (resp. no tea) and R stands for Reset) and $Q_F = \{1, 2, 3\}$. It is easy to check that the coffee-machine plant A fulfills properties 1. and 2. of Definition 5 w.r.t. \mathcal{S} whereas requirements 3. is not satisfied. Indeed, after the observation $?E?C!E?E?C$, \mathcal{S} is in state s_3 and A is either in states 11 or 1, i.e. $P = \{11, 1\}$ and in $A \times \mathcal{U}(\mathcal{S})$, the state $(1, s_3)$ is a deadlock state. So there is no possibility for A and \mathcal{S} to reach final states jointly. Note that state 1 is not a blocking state of A considered alone, since it is a final state. \diamond

¹The transitions \rightarrow_{\square} and \rightarrow_{\diamond} are respectively represented with plain arrows and dashed arrows

Figure 4: A possible implementation A of the coffee-machine

Modal specifications of services diverge notably from the *operating guidelines for services* introduced in [8] and further studied in [9], although they have much in common. Operating guidelines abstract from unobservable events, and they take final states into account for guaranteeing the absence of deadlock in the closed system formed by the service provider and the service requester. However, operating guidelines do not guarantee that this closed system is free of dead-ends, i.e. global states which are not deadlocks but from which global final states cannot be reached. For the rest, operating guidelines are technically closer to acceptance automata [5] than to modal automata [6]. In the absence of final states, modal automata are less expressive than acceptance automata, see [10] for a comparison. Nevertheless, this weakness seems to be overcompensated by the provision of a satisfaction relation for modal specifications which guarantees the absence of deadends.

3 Any service specification has an optimal finite state supervisor

In the rest of the paper, $\Sigma_c \subseteq \Sigma_o \subseteq \Sigma$, where Σ_o and Σ_c are the subsets of observable and controllable events, respectively. We let $\Sigma_{uo} = \Sigma \setminus \Sigma_o$, respectively $\Sigma_{uc} = \Sigma \setminus \Sigma_c$ denote the subset of unobservable, respectively uncontrollable events. We consider a *plant* $G = (Q, \Sigma, \delta_Q, q_0, Q_F)$, or service provider, and a modal specification of the expected service $\mathcal{S} = (S, \Sigma_o, \delta_S^\square, \delta_S^\diamond, s_0, S_F)$. The control problem, we want to solve is the following:

Problem 1 *Given a plant G and an expected service as above, we search for the optimal (i.e. maximally permissive) supervisor $C = (R, \Sigma_o, \delta_R, r_0)$ such that $C/G \models \mathcal{S}$ and C is an admissible controller for G w.r.t. Σ_c .*

Let us recall that C/G denotes the reachable restriction of the automaton $(Q \times R, \Sigma, \delta_{Q \times R}, (q_0, r_0), Q_F \times R)$ where $\delta_{Q \times R}((q, r), a) = (\delta_Q(q, a), \delta_R(r, a))$ if $a \in \Sigma_o$ and $\delta_{Q \times R}((q, r), a) = (\delta_Q(q, a), r)$ otherwise (assuming that the right members of these equations are defined).

By definition, in order that C be an admissible controller for G w.r.t. (Σ_o) and Σ_c , the following condition should hold for any state (q, r) of C/G and for any uncontrollable event $a \in \Sigma_{uc} \cap \Sigma_o$:

- $\delta_Q(q, a)$ defined $\Rightarrow \delta_R(r, a)$ defined.

Note that as previously mentioned, as C is defined over Σ_o , the language of C/G is automatically normal w.r.t. Σ_o and G .

In view of Definition 5, in order that $C/G \models \mathcal{S}$, it is moreover necessary that $(Q_0, r_0) \models s_0$ where $Q_0 = \delta_Q(q_0, \Sigma_{uo}^*)$ and \models is the largest relation on $(2^Q \times R) \times S$ such that, whenever $(P, r) \models s$, the following properties hold for all $a \in \Sigma_o$ and $q \in P$:

1. $\delta_Q(q, a)$ defined and $\delta_R(r, a)$ defined \Rightarrow
 $s \xrightarrow{a} s'$ and $(P', r') \models s'$ for $P' = \delta_Q(P, a\Sigma_{uo}^*)$ and $r' = \delta_R(r, a)$,

2. $s \xrightarrow{a}_{\square} s' \Rightarrow \delta_Q(q, \Sigma_{uo}^* a) \neq \emptyset$ and $\delta_R(r, a)$ defined,
3. $(Q_F \times R) \times S_F$ can be reached from $((q, r), s)$ in $(\mathcal{U}(G) \times C) \times \mathcal{U}(S)$.

It is important to note that the above characterization applies unchanged to $G' = (Q, \Sigma, \delta_Q, Q_0, Q_F)$, where $Q_0 = \delta_Q(q_0, \Sigma_{uo}^*)$, i.e. to the original plant automaton G in which the initial state q_0 has been replaced with its unobservable reach Q_0 .

The state oriented and therefore co-inductive characterization of the admissible supervisors C such that $C/G \models \mathcal{S}$ which we have presented above is not always convenient. Alternatively, a non-inductive characterization of these supervisors may be given in terms of their languages $\mathcal{L}(C)$, as follows.

Given any non-empty prefix-closed language $K \subseteq \Sigma_o^*$, let $C = \mathcal{LTS}(K)$ and hence $K = \mathcal{L}(C)$, then C is an admissible supervisor for G if and only if

$$\begin{aligned} \forall a \in \Sigma_{uc} \cap \Sigma_o \forall \omega \in K \forall w \in \mathcal{L}(\mathcal{U}(G)) : \\ \omega = \pi_o(w) \wedge wa \in \mathcal{L}(\mathcal{U}(G)) \Rightarrow \omega a \in K \end{aligned}$$

With the same definition as above, $C/G \models \mathcal{S}$ if and only if the following properties hold for all $a \in \Sigma_o$, for all $\omega \in K$, for all $s \in S$ such that $s_0 \xrightarrow{\omega}_{\diamond} s$ in $\mathcal{U}(S)$, and for all $w \in \mathcal{L}(\mathcal{U}(G))$ such that $\omega = \pi_o(w)$:

1. $wa \in \mathcal{L}(\mathcal{U}(G))$ and $\omega a \in K \Rightarrow s \xrightarrow{a}_{\diamond} s'$ for some $s' \in S$,
2. $s \xrightarrow{a}_{\square} s' \Rightarrow \exists u \in \Sigma_{uo}^* : wua \in \mathcal{L}(\mathcal{U}(G))$ and $\omega a \in K$,
3. $\exists v \in \Sigma_o^* \exists \nu \in \Sigma_o^* : wv \in \mathcal{L}(G) \wedge \nu = \pi_o(v) \wedge \omega\nu \in K \wedge s \xrightarrow{\nu}_{\diamond} s'$ for some $s' \in S_F$.

The two characterizations are equivalent since one may pass from the former to the latter by replacing q with $\delta_Q(q_0, w)$ and r by $\delta_R(r_0, \omega)$, and vice-versa. Therefore, in the latter characterization, after applying universal quantification over $w \in \mathcal{L}(\mathcal{U}(G))$ subject to $\pi_o(w) = \omega$, one gets three conditions that depend exclusively upon $P = \delta_Q(q_0, \pi_o^{-1}(\omega))$, $r = \delta_R(r_0, \omega)$ and s . From now on, let \mathcal{K} denote the family of the non-empty prefix closed languages $K \subseteq \Sigma_o^*$ that satisfy the conditions stated in the second characterization, and let $K^\dagger = \cup \mathcal{K}$. It is straightforward to show that K^\dagger belongs to \mathcal{K} . Therefore, if $\mathcal{K} \neq \emptyset$, there exists a unique solution to problem 1.

In the rest of the section we prove that, if there exists an admissible supervisor C such that $C/G \models \mathcal{S}$, then there exists such an optimal and moreover finite-state supervisor C^\dagger . Further, we show that $R = 2^Q \times S$ may be chosen as the set of states of C^\dagger .

Given any non-empty prefix-closed language $K \subseteq \Sigma_o^*$, let $C = \mathcal{LTS}(K)$. Then C is an admissible supervisor and $C/G \models \mathcal{S}$ if and only if $K \in \mathcal{K}$. As K^\dagger is the supremal element of \mathcal{K} , it follows clearly that, unless $\mathcal{K} = \emptyset$, $\mathcal{LTS}(K^\dagger)$ is an optimal supervisor. However, this supervisor may have an infinite number of states. We prove below that K^\dagger is a regular language, showing that $K^\dagger = \mathcal{L}(C^\dagger)$ for some finite state supervisor C^\dagger .

Proposition 1 K^\dagger is a regular language.

Proof For any $\omega \in K^\dagger$, let $\rho(\omega) = \{\nu \in \Sigma_o^* \mid \omega\nu \in K^\dagger\}$ (thus $\rho(\omega)$ is a right derivative of K^\dagger), and let $\xi(\omega) = (P, s)$ with $P = \delta_Q(q_0, \pi_o^{-1}(\omega))$ and $s_0 \xrightarrow{\omega}_{\diamond} s$. By Myhill and Nerode's theorem, in order to show that K^\dagger is regular, it suffices to construct $\bar{\rho} : 2^Q \times S \rightarrow \mathcal{P}(\Sigma_o^*)$ such that $\rho(\omega) = \bar{\rho} \circ \xi(\omega)$ for all $\omega \in K^\dagger$. We show that this relation is satisfied with $\bar{\rho}(P, s) = \cup\{\rho(\omega) \mid \xi(\omega) = (P, s)\}$. Let $\omega, \omega' \in K^\dagger$ such that $\xi(\omega) = \xi(\omega')$. By Lemma 1 given below, $\rho(\omega) = \rho(\omega')$, and therefore $\rho(\omega) = \bar{\rho} \circ \xi(\omega)$. \square

Lemma 1 For any $\omega \in K^\dagger$, let $K^\dagger \triangleright \omega = \{\nu \in \Sigma_o^* \mid \omega\nu \in K^\dagger\}$ ($= \rho(\omega)$), and let $\mathcal{S} \triangleright \omega = (S, \Sigma_o, \delta_S^\square, \delta_S^\diamond, s_o \triangleright \omega, S_F)$ and $G \triangleright \omega = (Q, \Sigma, \delta_Q, q_0 \triangleright \omega, Q_F)$ be defined with $s_0 \xrightarrow{\omega}_{\diamond} (s_o \triangleright \omega)$ and $q_0 \triangleright \omega = \delta_Q(q_0, \pi_o^{-1}(\omega))$. Then $K^\dagger \triangleright \omega$ is the language of an admissible controller enforcing the modal specification $\mathcal{S} \triangleright \omega$ on the plant $G \triangleright \omega$, and moreover it is the largest language with this property.

Proof When specialized to words $\omega\omega' \in K^\dagger$, the conditions specified in the characterization of \mathcal{K} in order that K^\dagger should be an admissible controller enforcing \mathcal{S} on G are the same as the conditions required in order that $K^\dagger \triangleright \omega$ should be an admissible controller enforcing $\mathcal{S} \triangleright \omega$ on $G \triangleright \omega$. The second assertion may be established by contradiction. If $K^\dagger \triangleright \omega$ was not the largest solution to the derived control problem, then $K^\dagger \cup \omega(K^\dagger \triangleright \omega)$ would be a solution to the original control problem strictly larger than K^\dagger , which is impossible. \square

4 An iterative algorithm for computing an optimal finite state supervisor

With Proposition 1, we have obtained a non-constructive proof of the regularity of K^\dagger . In this section, we propose an algorithm for constructing from G and \mathcal{S} an optimal finite state supervisor C^\dagger or deciding that no supervisor can enforce \mathcal{S} on G . It will be proved in Section 4.5 that the proposed decision and synthesis algorithm is correct: if it does not yield any supervisor, then $K^\dagger = \emptyset$, and in the converse case, $K^\dagger = \mathcal{L}(C^\dagger)$. Not surprisingly, the set of states of C^\dagger is a subset of $2^Q \times S$ (Q and S are the respective sets of states of G and \mathcal{S}). As usual in supervisor synthesis, the algorithm starts with an expansion stage (A), in which an abstraction of the reachable part of $\mathcal{U}(G) \times \mathcal{U}(\mathcal{S})$ is built inductively, and it proceeds with reduction stages, performed in rounds until a fixpoint is reached. A particularity lays in the (non-strict) alternation between two types of reduction stages, on the one hand stages (B) that eliminate states inconsistent with modal transitions, and on the other hand stages (C) that eliminate states from which joint termination is not possible. The algorithm has the control pattern A;(B;C)*.

4.1 The expansion stage A

Given $\mathcal{U}(G) = (Q, \Sigma, \delta_Q, q_0)$ and $\mathcal{U}(\mathcal{S}) = (S, \Sigma_o, \delta_S^\diamond, s_0)$, let $r_0 = (\delta_Q(q_0, \Sigma_{uo}^*), s_0)$ where $\Sigma_{uo} = \Sigma \setminus \Sigma_o$ and let $C^0 = (R, \Sigma_o, \delta_R, r_0)$ be the LTS defined inductively as follows. $R \subseteq 2^Q \times S$ and $\delta_R : R \times \Sigma_o \rightarrow R$ are the least set and partial function, respectively, such that $r_0 \in R$ and for any $(P, s) \in R$ and $a \in \Sigma_o$, $\delta_R((P, s), a) = (P', s') \in R$ with $P' = \delta_Q(P, a\Sigma_{uo}^*)$ and $s' = \delta_S^\diamond(s, a)$, unless $\delta_S^\diamond(s, a)$ is undefined or $(\forall q \in P) \delta_Q(q, a) = \emptyset$ or $\delta_S^\square(s, a)$ is defined and $(\exists q \in P) \delta_Q(q, \Sigma_{uo}^*) = \emptyset$. As R is a subset of the finite set $2^Q \times S$, this inductive construction is finite.

4.2 The reduction stage B

Given $C^i = (R, \Sigma_o, \delta_R, r_0)$ where i is an even number, one computes C^{i+1} from C^i by removing iteratively from C^i all states and transitions which are found inconsistent with the requirements expressed by the modal transitions in \mathcal{S} . This is done by applying the classical Ramadge-Wonham algorithm for state based supervisory control, with $\Sigma_{uc} = \Sigma \setminus \Sigma_c$ as the set of uncontrollable events.

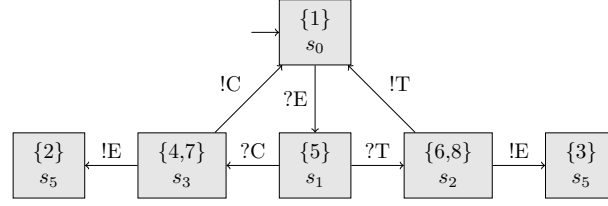
Declare *inconsistent w.r.t. controllability or modalities* any state $(P, s) \in R$ such that at least one of the following two properties hold:

- $\exists a \in \Sigma_{uc} \cap \Sigma_o \exists q \in P : \delta_Q(q, a) \text{ defined} \wedge \delta_R((P, s), a) \text{ undefined,}$
- $\exists a \in \Sigma_o : \delta_S^\square(s, a) \text{ defined} \wedge \delta_R((P, s), a) \text{ undefined}$

Whenever some state (P, s) is found inconsistent, this state is removed from R and from the image of the partial function δ_R , which may lead to new inconsistencies w.r.t. controllability or modalities. Note that the inconsistencies w.r.t. δ_S^\diamond have already been considered in the construction of C^0 and new inconsistency of this type may be introduced by restricting R and δ_R . As R is a finite set, this iterative cleaning procedure terminates (possibly with $R = \emptyset$). The result does not depend upon the order in which the states and transitions are removed.

4.3 The reduction stage C

Given $C^i = (R, \Sigma_o, \delta_R, r_0)$ where i is an odd number, one computes C^{i+1} from C^i by removing iteratively from C^i all states and transitions that cannot lead to joint termination w.r.t. the final states of G and

Figure 6: C^3

4.5 Correctness of the algorithm: $\mathcal{L}(C^\dagger) = K^\dagger$

In this section, we show that the finite state LTS C^\dagger constructed in section 4 realizes K^\dagger , thus in particular C^\dagger has an empty set of states if and only if K^\dagger is an empty language.

For all $i \geq 0$, let $H^i = \mathcal{U}(G) \times C^i$. Three observations about the LTS's H^i and $H^i \times \mathcal{U}(S)$ are fundamental for the propositions established below. First, every state of H^i is of the form $(q, (P, s))$ with $q \in P$ and P closed under unobservable transitions in G . Second, every reachable state of $H^i \times \mathcal{U}(S)$ is of the form $((q, (P, s)), s)$, where the same state $s \in S$ occurs twice. Third, for $i \geq 1$, H^i is isomorphic, as an LTS over Σ , to the expansion $Exp(C^i)$ of C^i defined as follows.

Definition 6 Given $C^i = (R, \Sigma_o, \delta_R, r_0)$, let $Exp(C^i) = (Exp(R), \Sigma, \delta^i, E_0)$ where the set of expanded states is $Exp(R) = \{(q, (P, s)) \mid (P, s) \in R \wedge q \in P\}$, the initial state is $E_0 = (q_0, (\delta_Q(q_0, \Sigma_{uo}^*), s_0))$, and the transition function $\delta^i : Exp(R) \times \Sigma \rightarrow Exp(R)$ is defined as follows:

- for $a \in \Sigma_{uo}$, let $\delta^i((q, (P, s)), a) = (\delta_Q(q, a), (P, s))$,
- for $a \in \Sigma_o$, let $\delta^i((q, (P, s)), a) = (\delta_Q(q, a), (\delta_Q(P, a\Sigma_{uo}^*), \delta_S^\diamond(s, a)))$ unless $\delta_Q(P, a) = \emptyset$.

Remark 2 H^0 is not necessarily isomorphic to $Exp(C^0)$ because in this particular case there may exist $(P, s) \in R$, $q, q' \in P$ and $a \in \Sigma_o$ such that $\delta_S^\diamond(s, a)$ defined, $\delta_Q(q, a)$ defined, and $\delta_Q(q', \Sigma_{uo}^*) = \emptyset$, and then $\delta_R((P, s), a)$ is undefined in C^0 (see stage A of the synthesis algorithm).

Proposition 2 If C^\dagger has a non-empty set of states, then C^\dagger is an admissible controller and $C^\dagger/G \models \mathcal{S}$.

Proof Suppose for a contradiction that C^\dagger is not an admissible controller, and let $C^\dagger = C^i$ with $i \geq 2$, thus $C^\dagger/G = H^i$. In view of the isomorphism between H^i and $Exp(C^i)$, the following situation is met for some $a \in \Sigma_{uc} \cap \Sigma_o$ and for some reachable state $(q, (P, s))$ of $Exp(C^i)$:

- $\delta_Q(q, a)$ is defined and $\delta^i((q, (P, s)), a)$ is undefined, but in this case, $\delta_Q(P, a) \neq \emptyset$ since $q \in P$, hence $\delta_S^\diamond(s, a)$ must be undefined, and therefore (P, s) is an inconsistent state of C^i (w.r.t. controllability), which is impossible.

Now suppose for a contradiction that C^\dagger/G does not satisfy the modal specification \mathcal{S} . In view of Definition 5 and the isomorphism between H^i and $Exp(C^i)$, at least one of the following situations is met for some $a \in \Sigma_o$ and for some reachable state $(q, (P, s))$ of $Exp(C^i)$:

- $\delta^i((q, (P, s)), a)$ is defined and $\delta_S^\diamond(s, a)$ is undefined, but this is not possible because the first assumption implies that $\delta_R((P, s), a)$ is defined in C^i and hence in C^0 , entailing that $\delta_S^\diamond(s, a)$ is defined,
- $s \xrightarrow{a} s'$ and $\delta^i((q, (P, s)), \Sigma_{uo}^* a) = \emptyset$, then by definition of δ^i , one of the following two situations is met (recall that $q \in P$ and P is closed under unobservable transitions):
 - $\delta_Q(q, a\Sigma_{uo}^* a) = \emptyset$, but in this case, $\delta_R((P, s), a)$ would have been left undefined in C^0 (see Stage A of the synthesis algorithm), hence (P, s) would have been removed from R in C^1 at Stage B of the synthesis algorithm, showing a contradiction;

– $\delta_Q(P, a) \neq \emptyset$ and $(\delta_Q(P, a\Sigma_{uo}^*), \delta_S^\diamond(s, a))$ is not a state of C^i , but then (P, s) in an inconsistent state of C^i (w.r.t. modalities), which is impossible.

- one cannot reach any state $(q', (P', s'))$ with $q' \in Q_F$ and $s' \in S_F$ from $(q, (P, s))$ in $Exp(C^i)$, but then (P, s) in an inconsistent state of C^i (w.r.t. termination), which is impossible.

As all cases have been examined, the proposition obtains. \square

Proposition 3 *If $K^\dagger \neq \emptyset$, then $\mathcal{L}(C^\dagger) = K^\dagger$.*

Proof For any $\omega \in \Sigma_o^*$, let $\xi(\omega) = (\delta_Q(q_0, \pi_o^{-1}(\omega)), \delta_S^\diamond(s_o, \omega))$. By Lemma 1, $\xi(\omega) = \xi(\omega') \Rightarrow K^\dagger \triangleright \omega = K^\dagger \triangleright \omega'$ and moreover, $K^\dagger \triangleright \omega$ is the language of an admissible controller enforcing $\mathcal{S} \triangleright \omega$ on $G \triangleright \omega$. Thus, if $\omega \in K^\dagger$ and $\xi(\omega) = (P, s)$, then for all $a \in \Sigma_o$ such that $\delta_S^\square(s, a)$ is defined, $\delta_Q(q, \Sigma_{uo}^*a)$ is non-empty for all $q \in P (= \delta_Q(q_o, \pi_o^{-1}(\omega)))$. Therefore, the prefix closed language K^\dagger may be generated by a sub-system of C^0 , that is to say, by the induced restriction of C^0 on specific subsets of states and transitions. In particular, $K^\dagger \subseteq \mathcal{L}(C^0)$.

Assume by induction on $i \geq 0$ that $K^\dagger \subseteq \mathcal{L}(C^i)$.

- If $C^i = C^{i+2}$ then $C^\dagger = C^i$ and by Proposition 2, $\mathcal{L}(C^\dagger) \subseteq K^\dagger \subseteq \mathcal{L}(C^\dagger)$, showing the result.
- In the converse case, C^i is not an admissible controller or C^i/G does not satisfy \mathcal{S} . By the proof of Proposition 2, C^i contains inconsistent states (P, s) . Therefore, C^{i+2} has a strictly smaller set of states. We claim that no reachable sub-system of C^i containing a state missing in C^{i+2} can generate a language in \mathcal{K} . Therefore, necessarily $K^\dagger \subseteq \mathcal{L}(C^{i+2})$, and the proposition obtains by the induction on i .

The claim may be established by an induction on the set of inconsistent states successively removed, using at each step the isomorphism between C/G and $Exp(C)$ for any reachable sub-system C of C^i for $i \geq 1$. \square

5 Conclusion

In this paper, we have investigated the application of the supervisory control theory to enforce the modal specification of a service on a given plant automaton. We have established that this control problem has at most one solution and that this solution can be represented as a finite state supervisor. Finally, we have shown how to compute this supervisor. In this paper, we have made the assumption that the set of events that are observed by the controller is the set of events involved in the modal specification of the service. In order to obtain a more general framework, it would be interesting to investigate the control problem for modal specifications in the different setting where the controller's view of the system is not directly related with the interactive user's view. In the context of computer security, modal specifications could also serve to express additional availability constraints. For that reason, it would be interesting to define a common extension of this work and the one in [3] and then to consider a wide range of security properties mixing integrity constraints given by safety properties, confidentiality properties given by opacity predicates and availability properties given by modal specifications. Modal specifications are a simple but powerful description of the functional service that a user expects from an implementation. Among the set of controlled systems satisfying the specification, some implementations may be preferred to others because, e.g., the average elapsed time between the requests and the answers is shorter. It would be interesting to add quantitative criteria to help a selection among the non necessarily maximally permissive solutions of the control problem for modal specifications.

References

- [1] J.W. Bryans, M. Koutny, L. Mazaré, P.Y.A. Ryan: Opacity Generalized to Transition Systems. *Int. Journal of Computer Security*, vol. 7(6), 2008, pp 421-435.
- [2] J. Dubreil, P. Darondeau, H. Marchand: Opacity Enforcing Control Synthesis. Proc. of the 9th Int. Workshop on Discrete Event Systems, WODES, 2008, pp 28-35.

- [3] J. Dubreil, P. Darondeau, H. Marchand: Supervisory Control for Opacity. *IEEE Trans. Automatic Control*, 2009, to appear.
- [4] G. Feuillade, S. Pinchinat: Modal Specifications for the Control Theory of Discrete Event Systems. *Discrete Event Dyn Syst*, vol. 17, 2007, 211-232.
- [5] M. Hennessy: Acceptance Trees. *J. ACM*, vol. 32, 1985, 896-928.
- [6] K.G. Larsen: Modal Specifications. in: *Automatic Verification Methods for Finite State Systems*, Springer-Verlag, LNCS vol. 407, 1990, pp 232-246.
- [7] H. Hüttel and K. G. Larsen. The use of static constructs in a modal process logic. In *Logic at Botik*, pages 163–180, 1989.
- [8] N. Lohmann, P. Massuthe, K. Wolf: Operating Guidelines for Finite-State Services. Proc. ICATPN, Springer-Verlag, LNCS vol. 4546, 2007, pp. 321-341.
- [9] N. Lohmann, K. Wolf: Petrifying Operating Guidelines for Services. Proc. ACSO, IEEE Computer Society, 2009, pp. 80-88.
- [10] J.B. Raclet: Residual for Component Specifications. *ENTCS* vol. 215, 2008, pp. 93-110.
- [11] P.J. Ramadge, W.M. Wonham: Supervisory Control of a Class of Discrete Event Processes. *SIAM Journal of Control and Optimization*, vol. 25, 1987, pp 206-230.
- [12] P.J. Ramadge, W.M. Wonham: On the Supremal Controllable Language of a Given Language. *SIAM Journal of Control and Optimization*, vol. 25, 1987, pp 637-659.
- [13] P.J. Ramadge, W.M. Wonham: The Control of Discrete Event Systems. *Proc. of the IEEE, Special Issue on Dynamics of Discrete Event Systems*, vol. 77, 1989, pp 81-98.
- [14] S. Takai, Y. Oka: A formula for the supremal controllable and opaque sublanguage arising in supervisory control. *SICE Journal of Control, Measurement, and System Integration* vol. 1(4), 2008, pp 307-312.
- [15] A. Saboori and C.N. Hadjicostis: Opacity-Enforcing Supervisory Strategies for Secure Discrete Event Systems. Proceedings of CDC 2008, the 47th IEEE Conference on Decision and Control, Cancun, Mexico, 2008.
- [16] S. Takai, R. Kumar: Verification and Synthesis for Secrecy in Discrete-event Systems. Proc. of the American Control Conference, 2009, pp 4741-4746.
- [17] J.G. Thistle, W.M. Wonham: Supervision of Infinite Behavior of Discrete-Event Systems. *SIAM J. Control Optim.* vol. 32(4), 1994, pp 1098-1113.



Centre de recherche INRIA Rennes – Bretagne Atlantique
IRISA, Campus universitaire de Beaulieu - 35042 Rennes Cedex (France)

Centre de recherche INRIA Bordeaux – Sud Ouest : Domaine Universitaire - 351, cours de la Libération - 33405 Talence Cedex
Centre de recherche INRIA Grenoble – Rhône-Alpes : 655, avenue de l'Europe - 38334 Montbonnot Saint-Ismier
Centre de recherche INRIA Lille – Nord Europe : Parc Scientifique de la Haute Borne - 40, avenue Halley - 59650 Villeneuve d'Ascq
Centre de recherche INRIA Nancy – Grand Est : LORIA, Technopôle de Nancy-Brabois - Campus scientifique
615, rue du Jardin Botanique - BP 101 - 54602 Villers-lès-Nancy Cedex
Centre de recherche INRIA Paris – Rocquencourt : Domaine de Voluceau - Rocquencourt - BP 105 - 78153 Le Chesnay Cedex
Centre de recherche INRIA Saclay – Île-de-France : Parc Orsay Université - ZAC des Vignes : 4, rue Jacques Monod - 91893 Orsay Cedex
Centre de recherche INRIA Sophia Antipolis – Méditerranée : 2004, route des Lucioles - BP 93 - 06902 Sophia Antipolis Cedex

Éditeur
INRIA - Domaine de Voluceau - Rocquencourt, BP 105 - 78153 Le Chesnay Cedex (France)
<http://www.inria.fr>
ISSN 0249-6399