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Anonymity: particular case of Privacy

- To prevent information from becoming known to unintended agents ٠ or entities
 - Protection of private data (credit card number, personal info etc.)
 - Anonymity: protection of identity of an user performing a certain action
 - Unlinkability: protection of link between information and user
 - Unobservability: impossibility to determine what the user is doing

More properties and details at www.freehaven.net/anonbib/cache/terminology.pdf

Anonymity

- Hide the identity of a user performing a given action
- The action itself might be revealed
- Many applications
 - Anonymous web-surfing
 - Anonymous posting on forums
 - Elections ٠
 - Anonymous donation
- Protocols for anonymity often use randomization

The dining cryptographers

- A simple anonymity problem
- Introduced by Chaum in 1988
- Chaum proposed a solution satisfying the socalled "strong anonymity"



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Anonymity of the protocol

- How can we define the notion of anonymity?
- First we have to fix the notion of observable:
 - The anonymity property change depending on who is the observer / what actions he can see
 - An external observer can only see the declarations
 - One of the cryptographers can also see some of the coins

Correctness of the protocol

- The protocol is correct for any (connected) network graph
- The key idea is that all coins are added twice, so the cancel out
- Only the extra 1 added by the payer (if there is a payer) remains
- Note: this protocol could be extended to broadcast data anonymously, but the problem is that there in no distributed, efficient way to ensure that there is only one agent communicating the datum at each moment.

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Notion of anonymity Once we have fixed the observables, the protocol can be seen as a channel identity **Observables** (info to be protected) 01 a Protocol •• On **a**_m Output Input Paris, 17 December 2007 MPRI Course on Concurrency 12









Notions of strong anonymity

In the following, a, a' are hidden events, o is an observable

- I. [Halpern and O'Neill like] for all a, a': p(a|o) = p(a'|o)
- 2. [Chaum], [Halpern and O'Neill]: for all a, o: p(a|o) = p(a)
- 3. [Bhargava and Palamidessi]: for all a, a', o: p(o|a) = p(o|a')
- (2) and (3) are equivalent. Exercise: prove it
- (1) is equivalent to (2),(3) plus p(a) = p(a') for all a, a'
- the condition for all a, a' p(a) = p(a') depends on the input's distribution rather than on the features of the protocol

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Expressing the protocol in probabilistic (value passing) CCS

Advantage: use model checker of probabilistic CCS to compute the conditional probabilities automatically

 $Master = \bigoplus_{i=0}^{2} p_i \, \bar{m}_i \langle 1 \rangle . \bar{m}_{i+1} \langle 0 \rangle . \bar{m}_{i+2} \langle 0 \rangle . \mathbf{0}$ $\oplus p_m \, \bar{m}_0 \langle 0 \rangle . \bar{m}_1 \langle 0 \rangle . \bar{m}_2 \langle 0 \rangle . \mathbf{0}$

$$Crypt_i = m_i(x).c_{i,i}(y).c_{i,i+1}(z).\overline{out}\langle x+y+z\rangle.\mathbf{0}$$

$$Coin_i = p_h \, \bar{c}_{i,i} \langle 0 \rangle . \bar{c}_{i-1,i} \langle 0 \rangle . \mathbf{0} \oplus p_t \, \bar{c}_{i,i} \langle 1 \rangle . \bar{c}_{i-1,i} \langle 1 \rangle . \mathbf{0}$$

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$$DC = (\nu \vec{m})(Master \mid (\nu \vec{c})(\Pi_{i=0}^2 Crypt_i \mid \Pi_{i=0}^2 Coin_i))$$

- For an external observer the only observable actions are sequences of agree/disagree (daa, ada, aad, ...)
- Strong anonymity: different payers produce the observables with equal probability

 $p(daa | C_0 pays) = p(daa | C_1 pays)$ $p(daa | C_0 pays) = p(daa | C_2 pays)$ $p(ada | C_0 pays) = p(ada | C_1 pays)$

• This is equivalent to requiring that

 $p(C_i \text{ pays}) = p(C_i \text{ pays} \mid o_0 o_1 o_2)$

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Anonymity of the protocol

- If the coins are unfair this is no longer true
- For example, if p(heads) = 0.7

	daa	ada	aad	ddd
Co	0.37	0.21	0.21	0.21
C 1	0.21	0.37	0.21	0.21
C ₂	0.21	0.21	0.37	0.21

• Now if we see daa, we know that c1 is more likely to be the payer

Anonymity of the protocol

• Assuming fair coins, we compute these probabilities

	daa	ada	aad	ddd
Co	1/4	1/4	1/4	1/4
<i>C</i> ₁	1/4	1/4	1/4	1/4
C2	1/4	1/4	1/4	1/4

• Strong anonymity is satisfied

Anonymity of the protocol

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- Even if we don't know the fact that the coins are unfair, we could find out using statistical analysis
- Exercise: suppose we see almost all the time one of the following announcements

ada aad daa

- what can we infer about the coins?
- then can we find the payer?
- Now if we see daa, we know that C₀ is more likely to be the payer

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Weaker notions of anonymity

- There are some problems in which it is practically impossible to achieve strong anonymity
- We need to define weaker notions

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• In general, we need to give a quantitative characterization of the degree of protection provided by a protocol

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Degree of protection: an Information-theoretic approach

• The entropy *H*(*A*) measures the uncertainty about the anonymous events:

$$H(A) = -\sum_{a \in \mathcal{A}} p(a) \log p(a)$$

- The conditional entropy H(A|O) measures the uncertainty about *A* after we know the value of *O* (after the execution of the protocol).
- The mutual information *I*(*A*; *O*) measures how much uncertainty about *A* we lose by observing *O*:

$$I(A; O) = H(A) - H(A|O)$$

We can use (the converse of) the mutual information as a measure of the degree of protection of the protocol

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Open problems

- Information protection is a very active field of research. There are many open problems. For instance:
 - Make model-checking more efficient for the computation of conditional probabilities
 - Active attackers: how does the model of protocol-as-channel change?
 - Inference of the input distribution from the observers

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