

Geo-indistinguishability: A Principled Approach to Location Privacy

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Location-Based Systems

A **location-based system** is a system that uses geographical information in order to provide a service.

- ▶ Retrieval of Points of Interest (POIs).
- ▶ Mapping Applications.
- ▶ Deals and discounts applications.
- ▶ Location-Aware Social Networks.



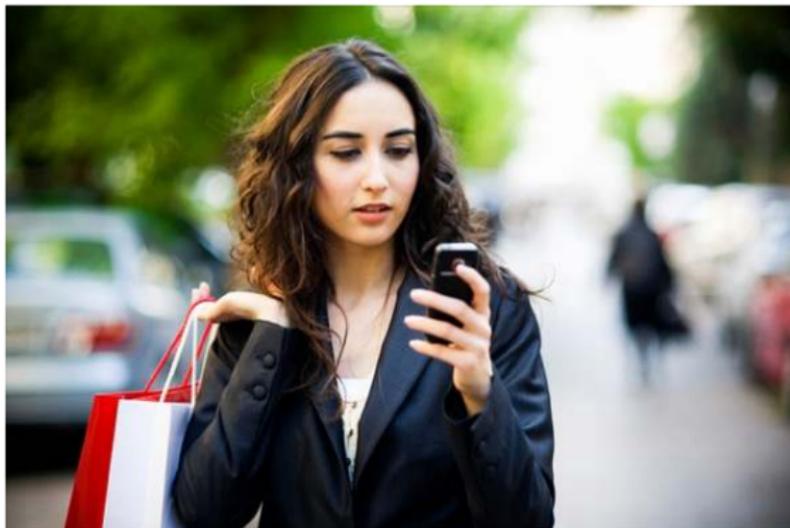
Location-Based Systems

- ▶ **Location information is sensitive.** (it can be linked to home, work, religion, political views, etc).
- ▶ Ideally: we want to **hide our true location.**
- ▶ Reality: we need to **disclose some information.**

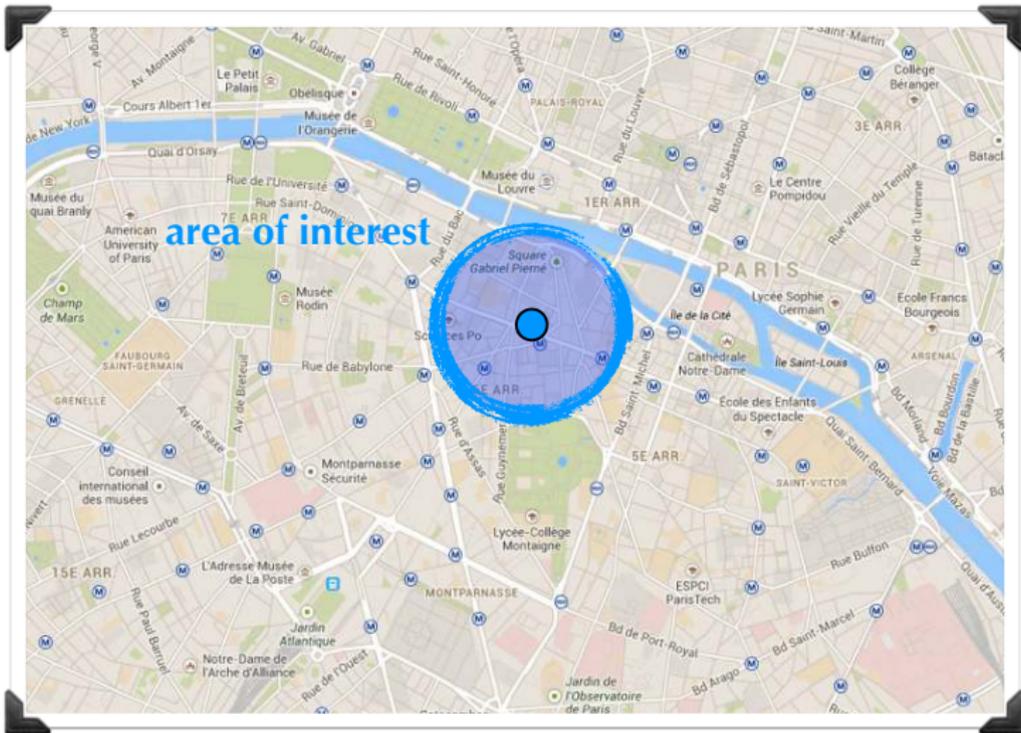


Example

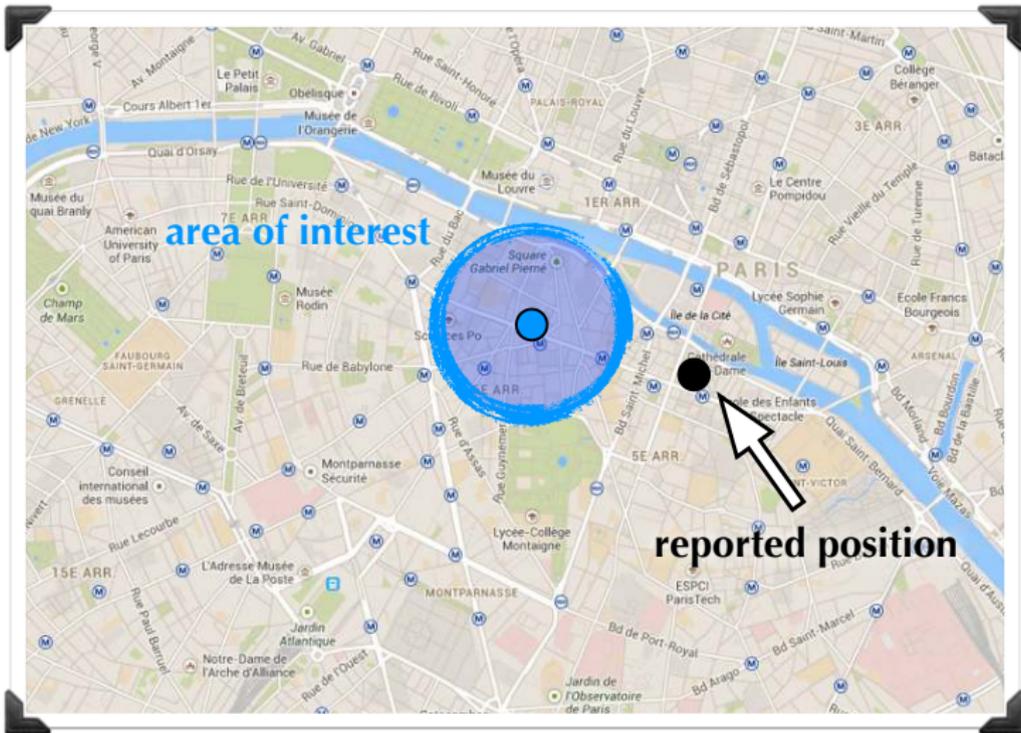
- ▶ Find restaurants within 300 meters.
- ▶ Hide location, **not identity**.
- ▶ Provide **approximate location**.



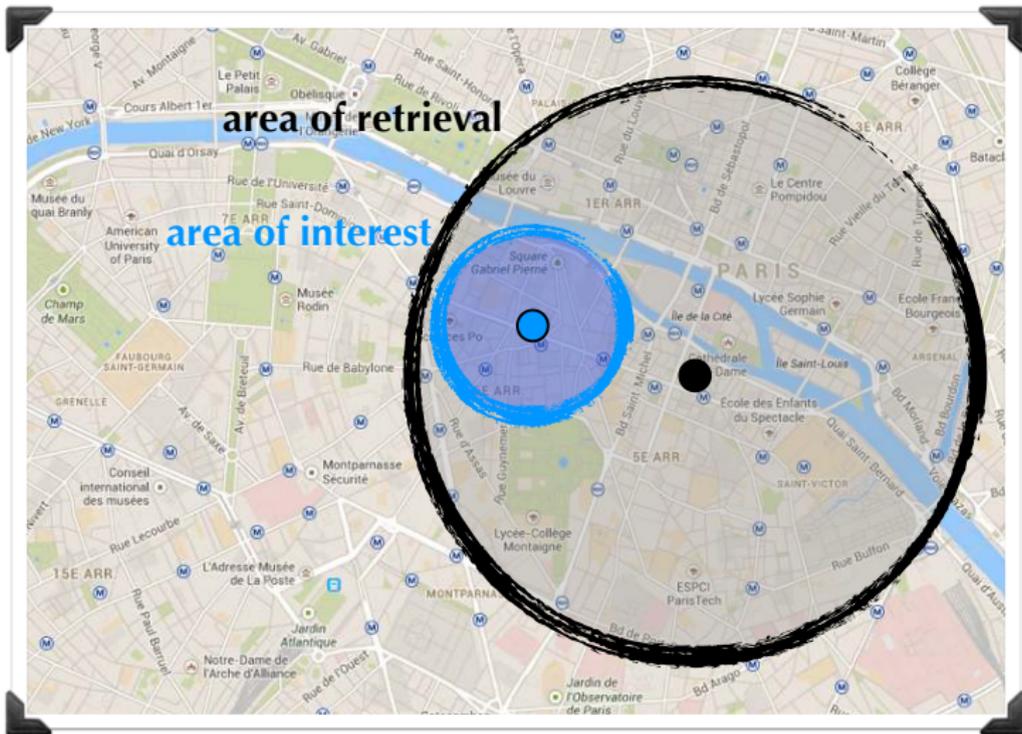
Obfuscation



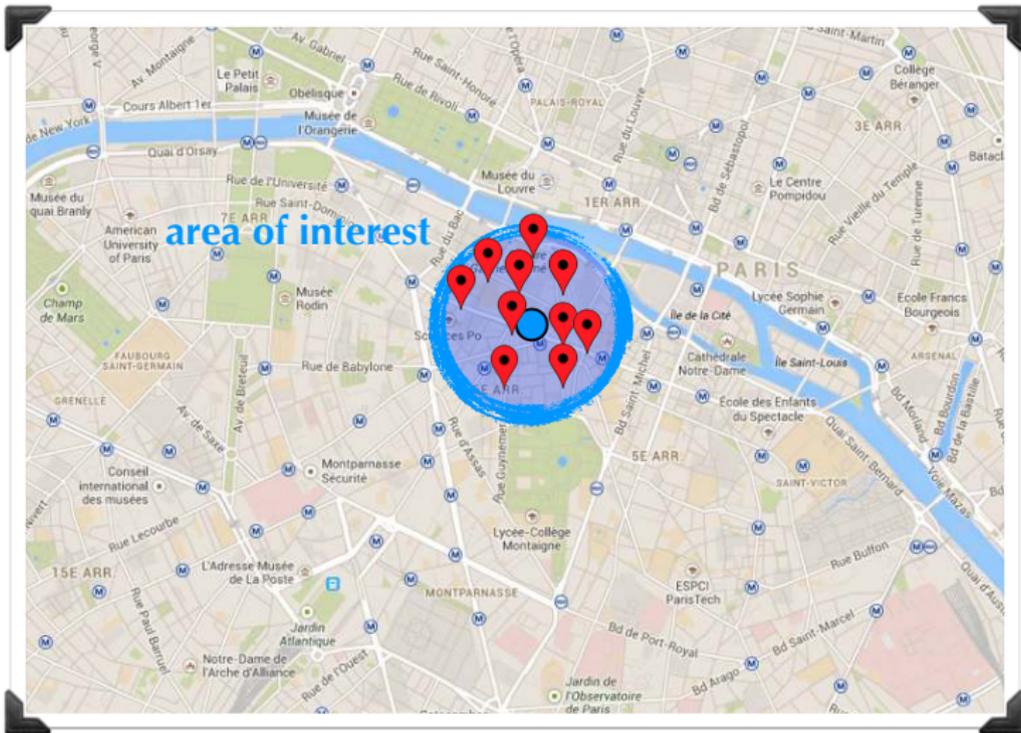
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Obfuscation



The Goals

- ▶ We want an **obfuscation mechanism**.
- ▶ Formal privacy definition, **independent from prior information**.
- ▶ **Easy to compute**, independently of the number of locations.
- ▶ No need of a trusted third-party.

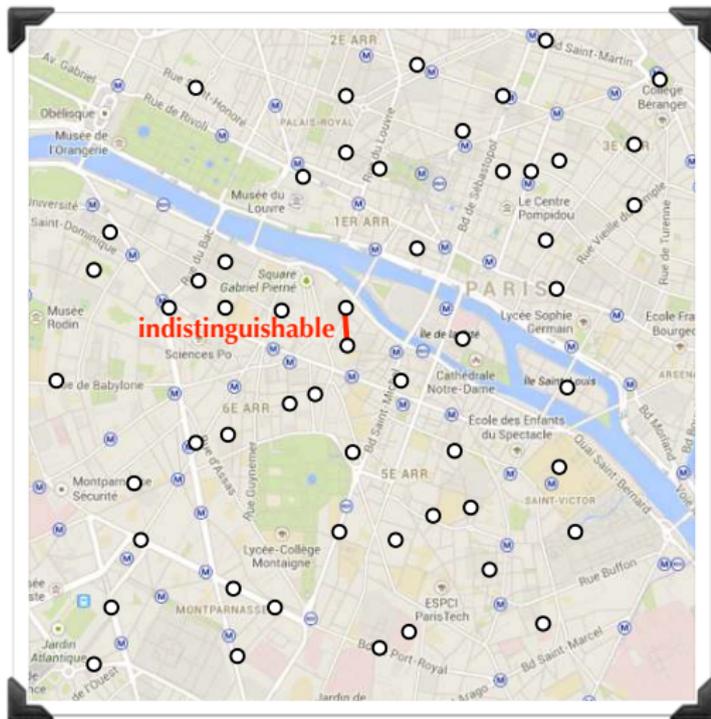
Towards a Definition

- ▶ Secrets are **locations**.
- ▶ Attacker's goal: **distinguish** location x from x' .
- ▶ The closer two locations are, the more indistinguishable they should be.



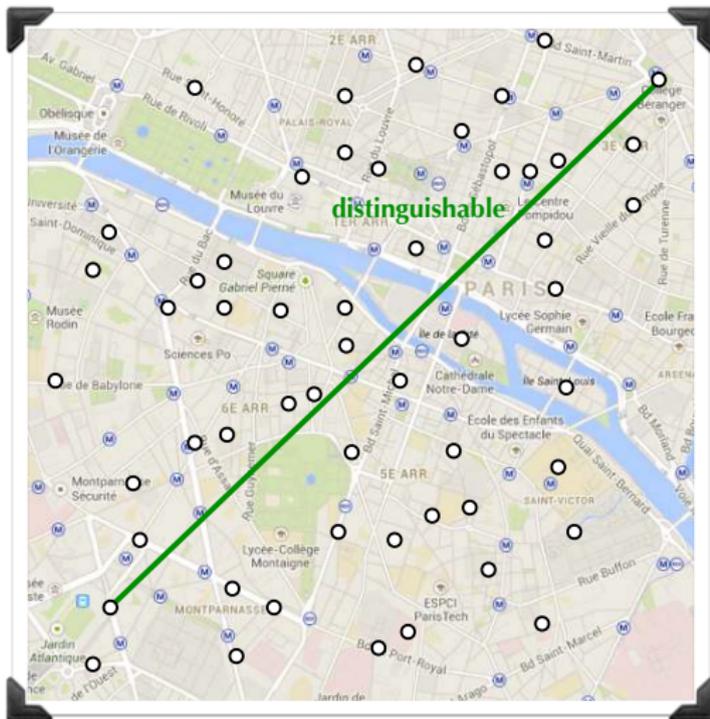
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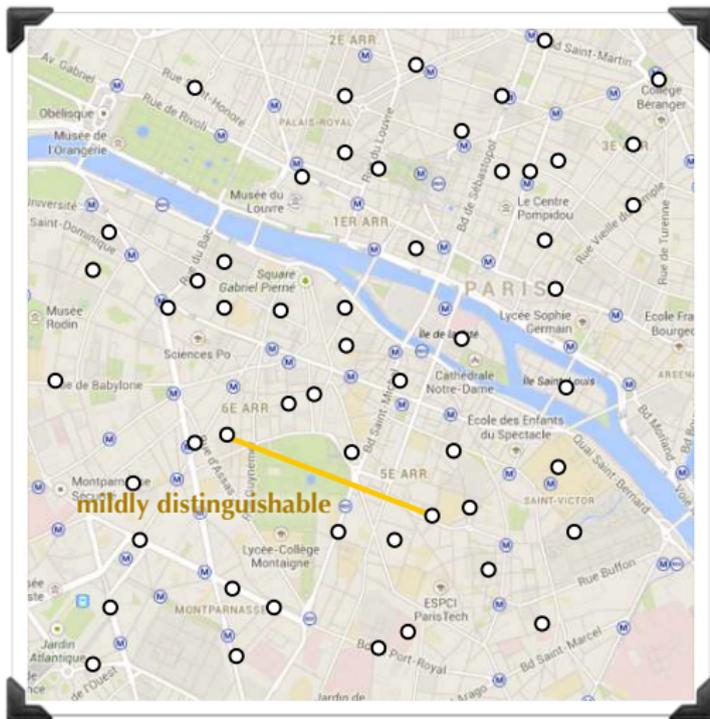
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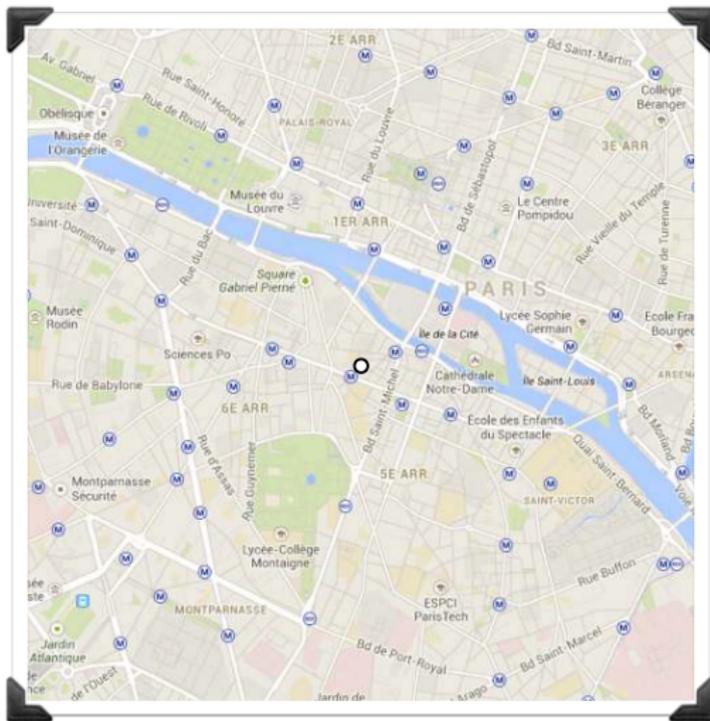
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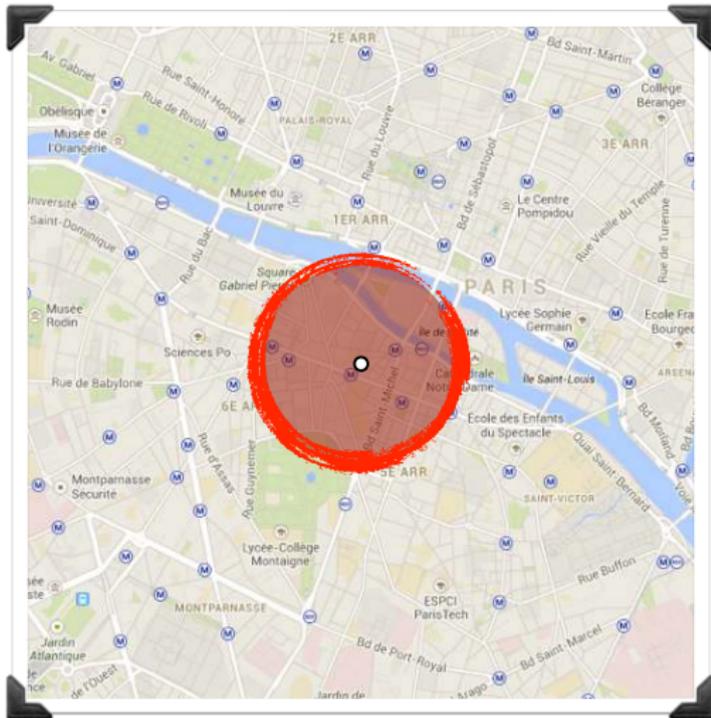
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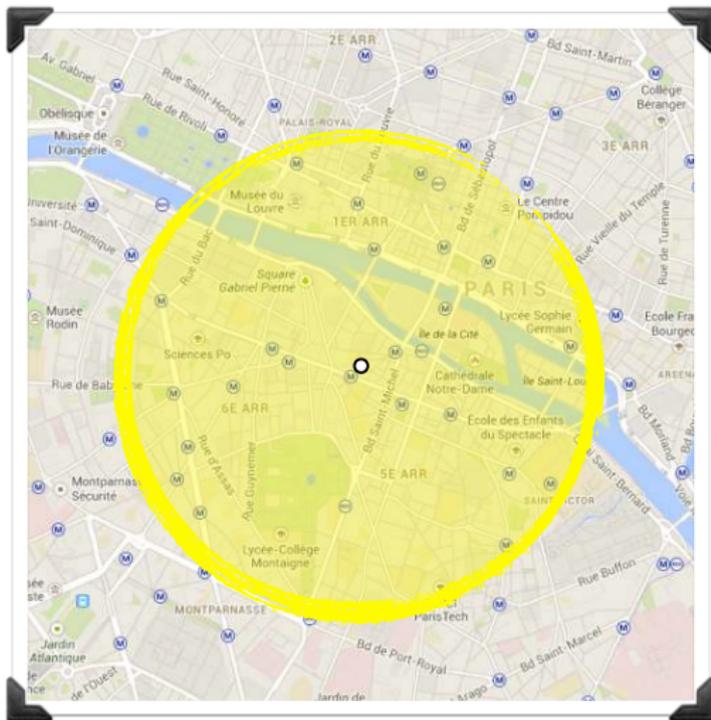
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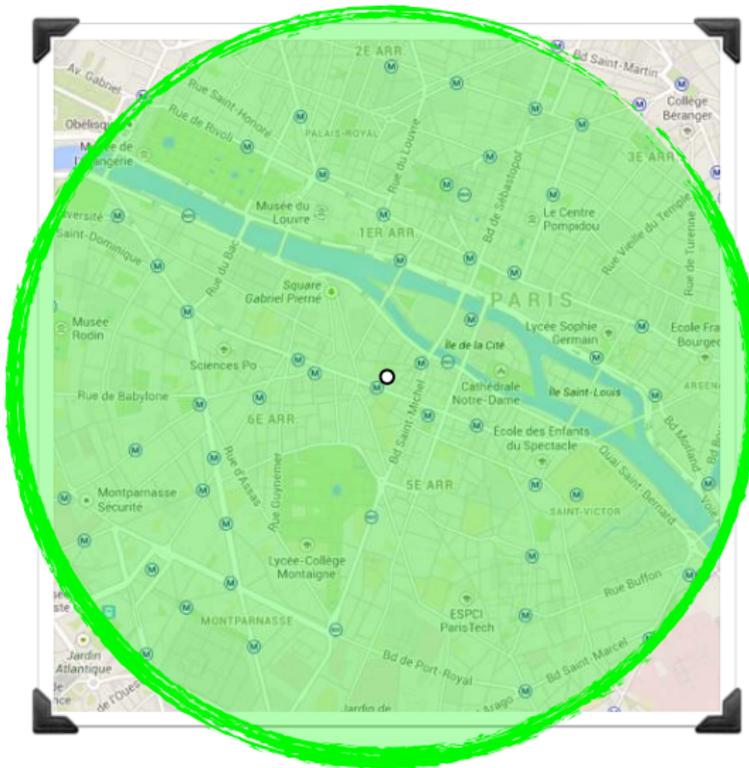
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Geo-Indistinguishability

- ▶ We can consider the **set of possible locations** as the set of secrets, and the **Euclidian distance** as the metric.

A location obfuscation mechanism M provides ϵ -geo-indistinguishability if:

$$\mathcal{D}_p(M(x), M(x')) \leq \epsilon d(x, x') \quad \forall x, x'$$

Where $d(x, x')$ is the Euclidean distance between x and x' .

[Pierce et al., ICFP 2010]

[Chatzikokolakis et al, PETS 2013]

Line of work

[PETS'13] privacy under general metrics

[CCS'13] application to location privacy, planar Laplace

[CCS'14] mechanisms of optimal utility

[PETS'14] protecting location traces

[ongoing] privacy metrics adapted to the semantics of the map

The Planar Laplace Mechanism

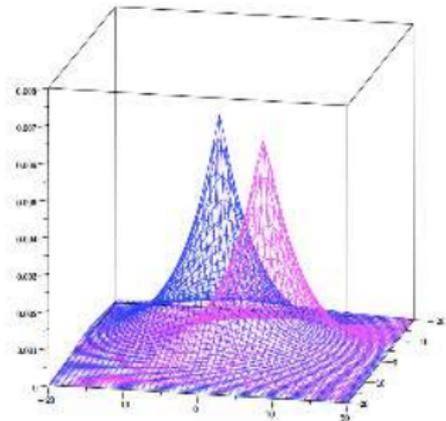
A way to achieve geo-indistinguishability is to add noise from a 2-dimensional Laplace distribution.

Computationally efficient.

Scales very well.

Independent from the set of locations and the user.

Utility may not be optimal.



Utility of a mechanism

We measure the (inverse of) utility

π : user's prior
 d_Q : quality metric

Utility measure:

$QL(K) =$ **Expected distance of K (wrt π and d_Q)**

Utility depends on the user!

Goal

Guarantee geo-indistinguishability.

- Pre-fixed privacy level ϵ .
- Independent from the user and adversary's prior.

Optimize utility.

- For a given set of locations.
- Depends on the user's prior π .

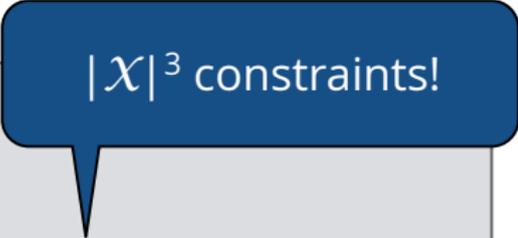
The d_X -optimal mechanism

K is OPTQL wrt ϵ , π , d_X and d_Q iff:

From all mechanisms that provide geo-indistinguishability with level at least ϵ , K is the one with the best utility.

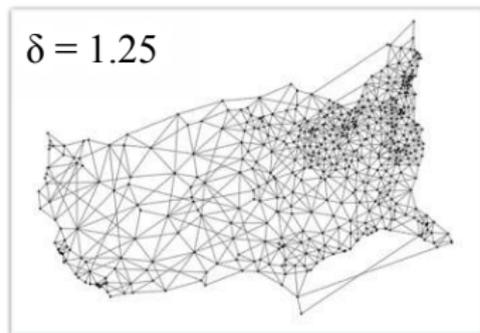
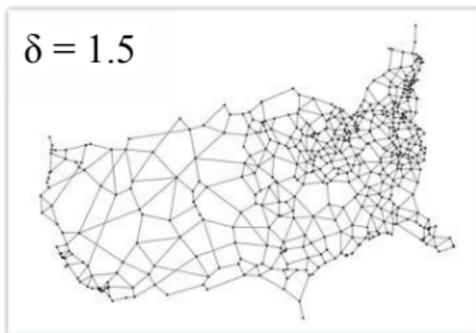
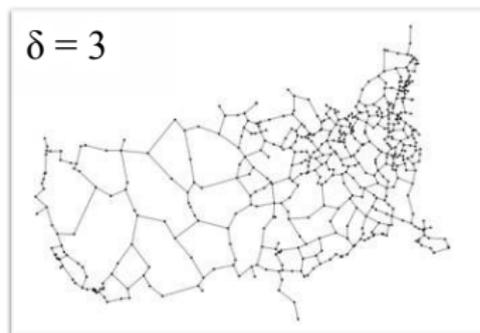
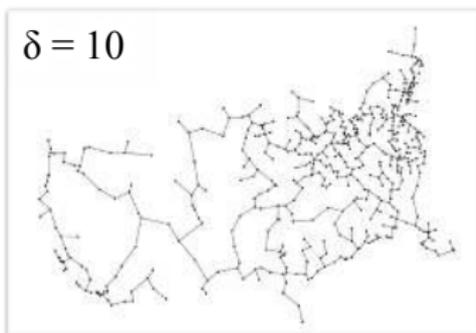
The $d_{\mathcal{X}}$ -optimal mechanism

We get K by solving a linear optimization problem:

Choose:	K	
To minimize:	$QL(K)$	
Subject to:	$k_{xz} \leq e^{\epsilon d_{\mathcal{X}}(x,x')} k_{x'z}$	

Because we need to consider the privacy constraints for all x, x' .

Spanners



Protecting location traces

- ▶ Secrets are now tuples

$$\mathbf{x} = (x_1, \dots, x_n)$$

- ▶ Distance between tuples:

$$d_{\infty}(\mathbf{x}, \mathbf{x}') = \max_i d(x_i, x'_i)$$

- ▶ Use ϵd_{∞} -privacy



Independent Mechanism

apply noise to each point

$n \in \mathbb{N}$ d_∞ -private

- ▶ works on **any** trace (including random teleporting)
- ▶ budget is linear on n



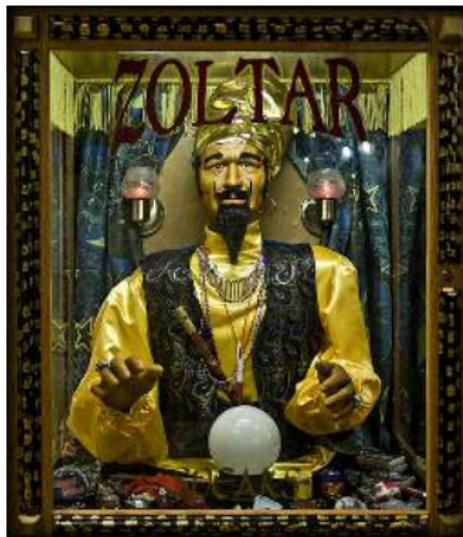
Predictive Mechanism

prediction function

- ▶ based on **public** info
- ▶ obtain point \tilde{z}_i

is \tilde{z}_i close to x_i ?

- ▶ yes: report \tilde{z}_i
- ▶ no: add new noise to x_i



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(In)Distinguishability Metric

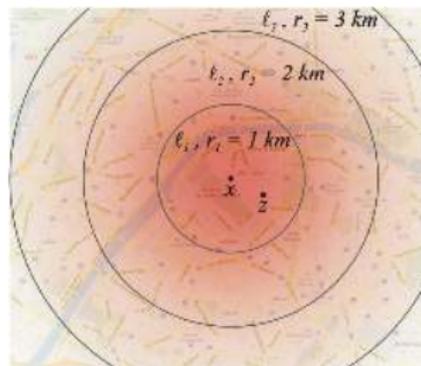
What is it that you want to
be similar to?

(and how much?)



Euclidean Metric

- ▶ **space** provides privacy
- ▶ scaled by ϵ

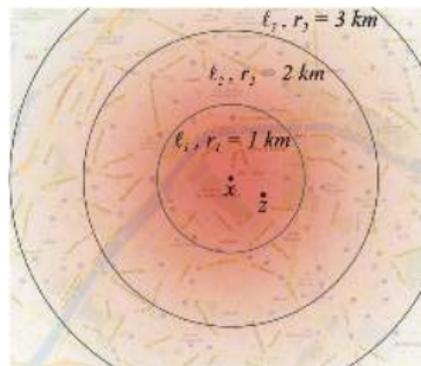


Euclidean Metric

- ▶ **space** provides privacy
- ▶ scaled by ϵ

but...

- ▶ space is not **equally valuable everywhere**
- ▶ **POI/population/...** also provide privacy
- ▶ we can achieve better privacy/utility by **adapting the noise to the map**



Building a custom metric

- ▶ divide the space in cells (eg grid 100m x 100m)
- ▶ privacy **weight** of each cell
 - ▶ from POI/population/... (eg by querying OSM)
 - ▶ from the cell's area
- ▶ build a **metric d** satisfying the **requirement f** :

$$\text{weight}(B_r^d(x)) \geq f(r) \quad x, r$$

Building a custom metric

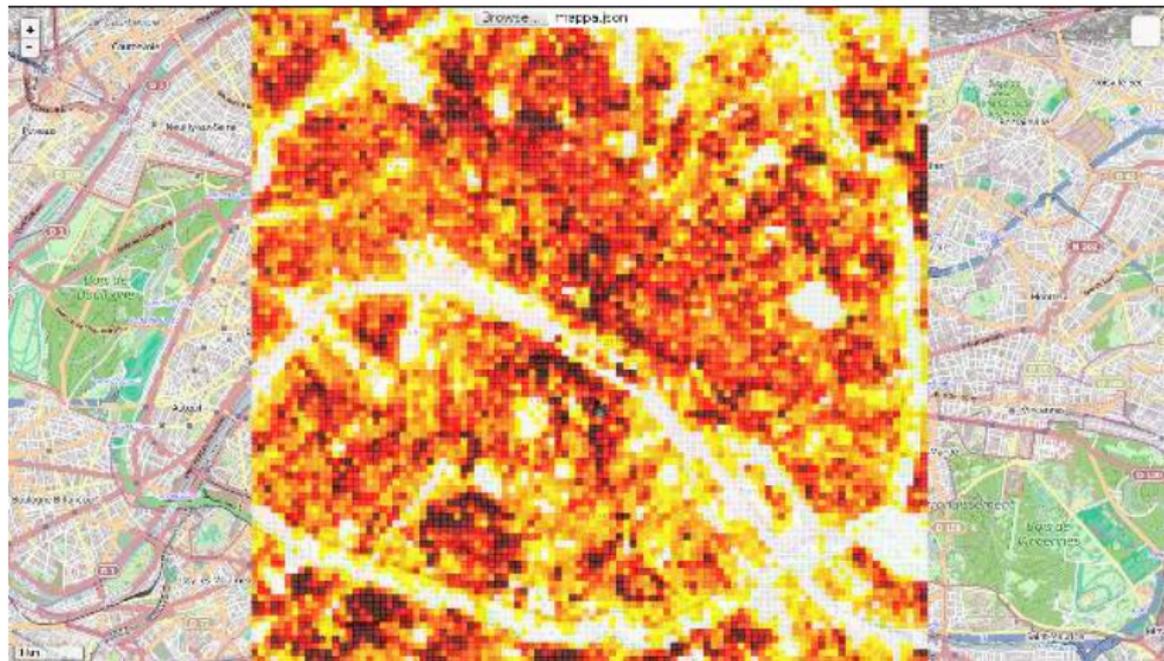
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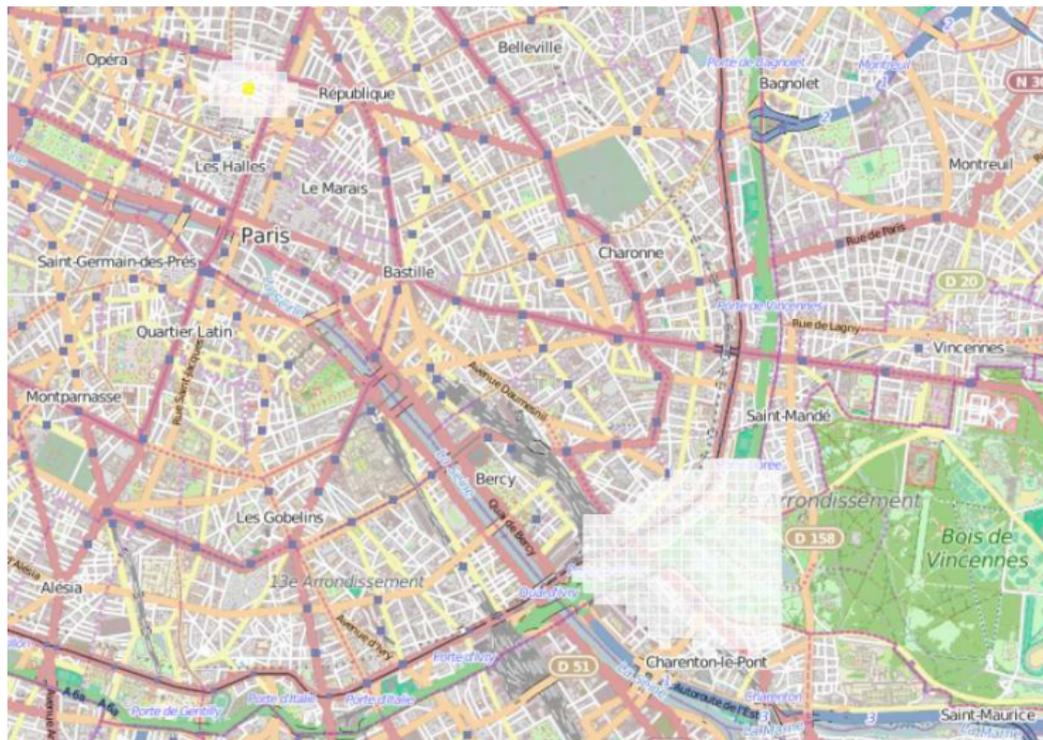
Exponential Mechanism

constructed from any metric d

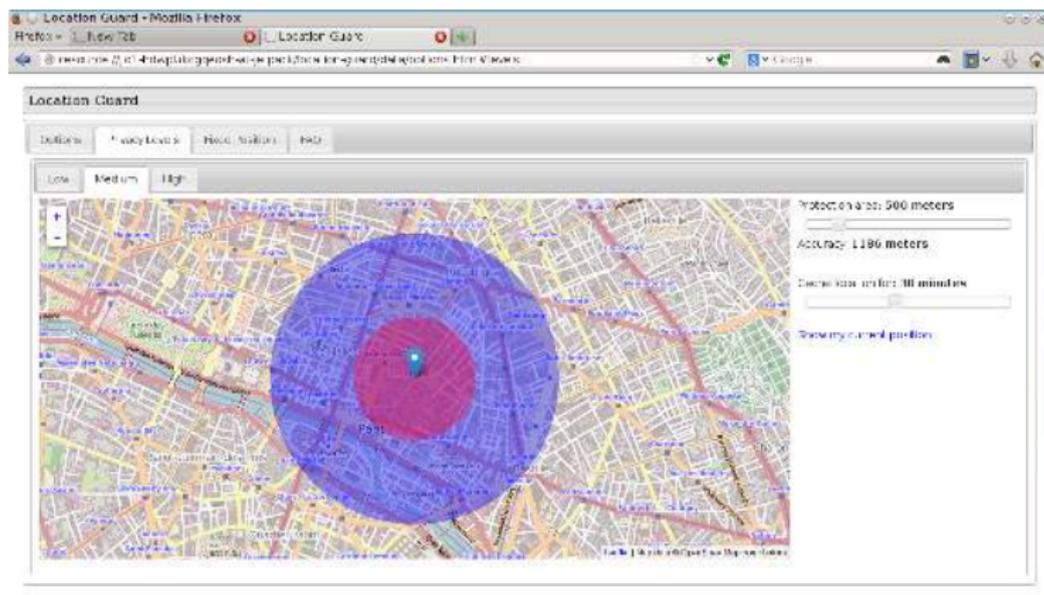
Privacy weights



Obtained Mechanism



Location Guard for Chrome and Firefox



<https://github.com/chatziko/location-guard>
4700+ daily users

Future work

Privacy guarantees under (un)correlation conditions between the points in the trace.

Questions?